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(Article begins on next page)

Essays in Financial Economics

A dissertation presented

by

Samuel Arthur Kruger

to

The Department of Business Economics

in partial fulfillment of the requirements

for the degree of

Doctor of Philosophy

in the subject of

Business Economics

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Abstract

This dissertation consists of three independent essays. Chapter 1, "The Effect of Mortgage Securitization on Foreclosure and Modification," assesses the impact of mortgage securitization on foreclosure and modification. My primary innovation is using the freeze of private mortgage securitization in the third quarter of 2007 to instrument for the probability that a loan is securitized. I find that privately securitized mortgages are substantially more likely to be foreclosed and less likely to be modified. Chapter 2, "Disagreement and Liquidity," analyzes how disagreement between investors affects the relationship between trading, liquidity, and asymmetric information. Traditional models predict that asymmetric information should destroy trade and liquidity. In contrast, I document empirical evidence that asymmetric information increases trading volumes in stock, corporate bond, and option markets. To resolve this puzzle, I propose a model of overconfident disagreement trading in which private information enhances trading and liquidity. Chapter 3, "Is Real Interest Rate Risk Priced? Theory and Empirical Evidence," asks whether investors demand compensation for holding assets whose returns covary with real interest rate shocks. Empirically, there is little evidence that real interest rate risk is priced in the cross section of stocks or across asset classes. Theoretically, interest rate risk can be positively or negatively priced depending on whether interest rate changes are due to time preference shocks or consumption growth shocks.

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To Mary and Matthew.

Chapter 1

The Effect of Mortgage Securitization on Foreclosure and Modification

1.1 Introduction

Since the start of the financial crisis, 4.4 million U.S. homes have been foreclosed, inflicting losses on mortgage investors, causing turmoil in the lives of mortgagors, and damaging surrounding communities. Roughly half of these foreclosures stemmed from privately securitized mortgages, prompting policy makers and economists to worry that securitization impedes mortgage modification and leads to unnecessary foreclosures. Unfortunately, evaluating the impact of securitization on foreclosures is challenging because securitization is an endogenous decision, and securitized mortgages likely differ from mortgages held on bank balance sheets even after controlling for observable characteristics.

I estimate the causal effect of securitization on foreclosure and modification by exploiting the sudden and unexpected freeze of private mortgage securitization in the third quarter of 2007.¹ Jumbo mortgages originated shortly before the freeze were disproportionately stuck

¹Purnanandam (2011) also documents and exploits loans being stuck on bank balance sheets in 2007. Purnanandam exploits cross sectional differences in bank exposure to originate-to-distribute lending to estimate the impact of securitization on origination quality. In contrast, I exploit time series variation in loan origination to estimate the impact of securitization on mortgage servicing.

on bank balance sheets even though many of them were intended for private securitization at the time they were originated. Because the freeze was unanticipated, loans originated shortly before the freeze are similar to loans originated earlier in 2007. I further control for changes to the lending environment over time using a difference-in-differences methodology with non-jumbo loans, which are primarily securitized by Fannie Mae and Freddie Mac and were unaffected by the private securitization freeze.

The results are striking. Relative to portfolio loans held directly on bank balance sheets, private securitization increases the probability of foreclosure initiation within six months of a mortgage's first serious delinquency by 8.0 ppt (12% of the mean foreclosure initiation rate). Similarly, securitization increases the probability of foreclosure completion by 4.7 ppt (35% of the mean) and decreases the probability of modification by 3.6 ppt (69% of the mean). My instrumental variables (IV) strategy is critical for estimating these effects. For foreclosure initiation and completion, IV estimates are twice as large as corresponding ordinary least squares (OLS) estimates. These results suggest that securitization significantly exacerbated the foreclosure crisis and needs to be considered in any policy response. Taken at face value, they imply that over 500,000 of the 4.4 million foreclosures experienced since the start of the financial crisis were caused by securitization.

In part motivated by the high foreclosure rates of privately securitized mortgages, the federal government enacted the Home Affordable Modification Program (HAMP) in February of 2009 to incentivize modifications and make modification practices more uniform across mortgages. My methodology does not provide a way to test whether HAMP succeeded in reducing foreclosures, but I can test the uniformity of foreclosure and modification practices across securitized and portfolio loans before and after HAMP. I find that private securitization increased foreclosure probability and decreased modification probability throughout the 2007 to 2011 time period, suggesting that HAMP did little to make foreclosure and modification practices more consistent across securitized and portfolio loans.

In addition to their relevance for foreclosure policy, these results speak to the debate

about securitization more generally. The tradeoffs of securitized financing include liquidity creation, increased availability of financing, decreased lending standards, and securitization's role in the financial crisis.² Securitization's impact on how assets are managed has received less attention but is also important, especially where management practices have externalities, as they likely do in the case of foreclosures (cf., Campbell, Giglio, and Pathak, 2011).

Securitization's impact on foreclosures and modifications illustrates one of the central precepts of corporate finance: separation of ownership and control matters. The importance of ownership structure and managerial incentives is universally accepted as a basic premise.³ Yet, empirical applications remain controversial. Are managers of public companies overpaid? Do compensation and governance provisions affect firm performance? Are private firms managed better than public firms? These questions are unsettled because empirical identification is often difficult if not impossible. My setting offers a rare laboratory for well-identified assessment of the effects of adding a layer of delegated management through securitization.

Similarly, mortgage securitization is a good example of incomplete contracts. The incomplete contracts theory of Grossman and Hart (1986) and Hart and Moore (1990) is well-established, but empirical research with actual contract details is rare. Mortgage securitization is a good setting for analyzing incomplete contracts because the relationship between the parties is clear (mortgage trusts passively own the mortgages, and servicers manage them) and the contracts are publicly disclosed.

The institutional details of mortgage servicing (described in Section 5) suggest that current loans and pending foreclosures are mechanical to service whereas loss mitigation (including modification) for delinquent loans involves significant discretion. In the language

²Gorton and Metrick (2011) address liquidity creation and the financial crisis. Loutskina (2011), Loutskina and Strahan (2009), and Mian and Sufi (2009) address financing availability. Keys, et al. (2010) and Rajan, Seru, and Vig (2012) address loan quality.

³The idea that incentives matter is as old as economics itself. Modern applications to managerial incentives date to at least Jensen and Meckling (1976).

of Grossman and Hart (1986), loss mitigation decisions represent non-contractible residual rights. These residual rights are universally held by mortgage servicers, effectively making the servicer the “owner” of a mortgage even though the trust holds the legal title and most of the cash flow rights.⁴ The disconnect between control and marginal cashflows creates two problems. First, servicers have an incentive to underinvest in loss mitigation. Second, when servicers do pursue loss mitigation, they may employ practices that enhance servicing income at the expense of principal and interest payments to the trust. This is essentially a multitasking problem, akin to Holmstrom and Milgrom (1991). Efforts to limit the underinvestment problem by incentivizing loss mitigation would be expensive and would exacerbate the multitasking problem.

In my examination of securitization contracts, I find that servicing agreements do little to overcome the underinvestment problem. Servicers are required to follow accepted industry practices, but servicing agreements provide no explicit incentives for loss mitigation. The agreements actually do the opposite. By universally reimbursing foreclosure expenses but not loss mitigation expenses, servicing agreements create an extra incentive to pursue foreclosure instead of loss mitigation. Ex-post renegotiation is precluded by trust passivity and investor dispersion (as in Bolton and Scharfstein, 1996). Thus, incomplete servicing contracts have real effects. Privately securitized loans are modified less and foreclosed more than they would be if they were held as portfolio loans. Contractual modification restrictions likely account for some of this bias, but they are too rare and insufficiently binding to explain the full bias. Most of securitization’s impact on foreclosures and modifications comes from misaligned incentives.

1.2 Existing Evidence

Posner and Zingales (2009) were early advocates of the view that securitization impedes loan modifications and causes foreclosures. Three previous studies test this hypothesis by

⁴Grossman and Hart (1986) define ownership as control of residual rights.

regressing foreclosure and modification probability on securitization status using OLS or logit regressions. Piskorski, Seru, and Vig (2010) consider mortgages originated in 2005 and 2006 that became seriously delinquent, defined as a delinquency of at least 60 days. Compared to portfolio mortgages, privately securitized mortgages had foreclosure rates that were 4-7 ppt higher after controlling for observable loan characteristics.⁵ Using a similar approach, Agarwal, et al. (2011) estimate that privately securitized mortgages that became seriously delinquent in 2008 were 4.2 ppt less likely to be renegotiated within 6 months relative to comparable portfolio mortgages.⁶ In contrast, Adelino, Gerardi, and Willen (2011b) find that differences in twelve-month loan modification rates between privately securitized mortgages and comparable portfolio mortgages were small for mortgages that were originated after 2004 and became seriously delinquent by September of 2007.⁷ The conflicting results of these papers appear to be mainly a function of the outcome variables and samples analyzed.⁸

The main limitation of the existing evidence is that causal interpretation requires the assumption that securitization status is randomly assigned conditional on observed loan characteristics. This is a problematic assumption because origination and securitization are endogenous decisions, and both are made based on a larger set of information than the observed characteristics econometricians can control for, thereby introducing omitted variable bias.

Can we at least determine the direction of the bias? The answer is no. First, privately securitized loans could be lower or higher quality than observably similar portfolio loans.

⁵See Table 3 of Piskorski, Seru, and Vig (2010).

⁶See Table 3, Panel A of Agarwal et al. (2011).

⁷Adelino, Gerardi, and Willen (2011b) estimate that if anything, privately securitized loans were modified slightly more frequently (0.6 to 2.1 ppt) than portfolio loans. See Panel B of their Table VI.

⁸Securitization has a larger impact on foreclosure than it does on modification. I find this in my analysis, and Agarwal, et al. (2011) find the same thing in their Appendix A. This explains why Piskorski, Seru, and Vig (2010) find large foreclosure effects while Adelino, Gerardi, and Willen (2011b) do not find significant modification effects in a largely equivalent sample. Agarwal, et al. (2011) focus on a later time period than the other two papers, which may explain why their modification results differ from Adelino, Gerardi, and Willen (2011b).

Originator adverse selection and screening moral hazard push in the direction of securitized loans being lower quality.⁹ On the other hand, mortgage backed security (MBS) sponsors also have access to unobserved information, which they could use to select higher quality loans.¹⁰ Second, the impact of loan quality on foreclosure and modification decisions conditional on delinquency is ambiguous. Some quality dimensions favor foreclosure, while others favor modification or inaction. For example, borrower resilience discourages foreclosure because a resilient borrower is likely to regain his financial footing and repay his mortgage. By contrast, borrower reliability encourages foreclosure because a reliable borrower must have suffered a large shock before becoming delinquent on his loan.

The existing literature recognizes the potential bias presented by unobserved quality. Yet, all three papers discussed above ultimately adopt causal interpretations of their evidence for or against securitization affecting servicing decisions. Their first rationale for a causal interpretation is that conditioning on serious delinquency mitigates the unobserved quality problem. Market participants may have unobserved information about the probability of delinquency or loan quality conditional on delinquency. If unobserved information is solely about the probability of delinquency, conditioning on delinquency gets rid of the problem. Unfortunately, there is no reason to believe that unobserved information is solely, or even primarily, about delinquency probability. There is actually good reason to believe the opposite because FICO scores (which are one of the most important observable quality measures) predict only the probability of a negative credit event, not the losses associated with the event. The second rationale the papers advance is that their results are similar for high quality loans (e.g., loans with high FICO scores and full income documentation),

⁹Using evidence from credit score cutoffs, Keys, et al. (2010) propose that originators employ less diligent screening for loans that are likely to be securitized. Bubb and Kaufman (2013) question the credit score cutoff evidence. Purnandam (2010) finds that banks with higher exposure to originate-to-distribute lending were stuck holding loans intended for securitization when securitization froze in 2007 and subsequently suffered higher delinquency rates and charge offs, consistent with securitization decreasing loan origination quality.

¹⁰Jiang, Nelson, Vytlačil (2010) present evidence that screening moral hazard is more than offset by selection of higher quality loans for securitization. The selection is in part facilitated by information that emerges during the time period between origination and securitization. Similarly, Agarwal, Chang, and Yavas (2012) show that for prime loans default risk is lower for GSE securitized loans than for portfolio loans.

which should have less potential for unobserved quality differences.¹¹ Though not clearly documented, smaller unobserved quality differences for high quality loans seem likely on an unconditional basis. However, the relevant unobserved difference is quality conditional upon delinquency, and this could be just as large for high quality loans as for low quality loans.

Finally, Piskorski, Seru, and Vig (2010) analyze a quasi-experiment for securitization status. They note that early payment default (EPD) clauses require some originators to buy back loans that become delinquent within 90 days of securitization. Loans that become delinquent shortly before and after this 90-day threshold differ in their probability of remaining securitized but are otherwise similar. The authors exploit this discontinuity by comparing loans that became delinquent shortly before 90 days and were bought back and kept by the originator to loans that became delinquent shortly after 90 days and remained securitized. Importantly, Piskorski, Seru, and Vig do not use instrumental variables or fuzzy regression discontinuity tools. Instead, they directly compare the two groups described above. This contaminates the plausibly orthogonal variation in securitization probability (timing of delinquency relative to the 90 day threshold) with endogenous decisions (whether the loan is bought back by the originator and whether it remains on the originator's balance sheet). Because repurchases are based on factors other than delinquency status (for example, a loan could unobservably violate another representation or warranty) and originators decide whether to retain or re-securitize repurchased loans, the resulting comparison is subject to omitted variable bias. Piskorski, Seru, and Vig argue that repurchase decisions are less endogenous than securitization decisions, but it is not clear this is the case. Adelino, Gerardi, and Willen (2011a) discuss this issue more fully and argue that early payment default is not a good instrument even if it is implemented using traditional tools.

¹¹Piskorski, Seru, and Vig (2010) and Agarwal, et al. (2011) use high quality loans as a robustness test. Adelino, Gerardi, and Willen (2011b) avoid this approach and argue that unobserved heterogeneity may actually be greater for loans that appear to be high quality because these loans were not securitized by the GSEs for some unobserved reason.

1.3 Data and Methodology

1.3.1 Loan Performance Data

My data on mortgage loans comes from Lender Processing Services (LPS).¹² The dataset consists of detailed monthly data on individual loans provided by large mortgage servicers, including at least seven of the top ten servicers. As of 2007, the dataset included 33 million active mortgages, representing approximately 60% of the U.S. mortgage market. Importantly, the dataset spans all mortgages serviced by the participating servicers, including portfolio loans, loans securitized by Fannie Mae and Freddie Mac (the Government Sponsored Entities, GSEs), and privately securitized loans.

My analysis focuses on first lien loans originated between January and August of 2007. To avoid survivor bias, I only consider loans that enter the LPS dataset within four months of origination. I drop government sponsored loans like VA and FHA loans because these loans may have different servicers requirements and incentives. To eliminate outliers and focus on reasonably typical prime (or near prime) loans I further restrict the sample to loans with origination FICO scores between 620 and 850, origination loan-to-value ratios of less than 1.5, and terms of 15, 20, or 30 years that are located in U.S. metropolitan statistical areas (MSAs) outside of Alaska and Hawaii. Finally, I drop a small set of loans that are at some point transferred to a servicer that doesn't participate in the LPS data because the data doesn't always reveal how delinquencies were ultimately resolved for these loans. Other than my exclusion of low FICO score loans and inclusion of GSE loans, these restrictions are largely consistent with Piskorski, Seru, and Vig (2010), Agarwal, et al. (2011), and Adelino, Gerardi, and Willen (2011b). The resulting sample consists of 1.9 million loans.

Table 1.1 describes the sample. It includes 264,000 jumbo loans (i.e., loans over \$417,000, which are not eligible for GSE securitization)¹³ and 1.6 million non-jumbo loans. As of six months after origination, 70% of the jumbo loans were privately securitized. Almost all

¹²LPS data was previously known as McDash data.

¹³The conforming loan limit in 2007 was \$417,000 in all states except Alaska and Hawaii, which are excluded from my sample.

Table 1.1: Data Summary

Data comes from LPS. The sample consists of first-lien conventional loans originated between January and August of 2007 that enter the dataset within 4 months of origination, have origination FICO scores between 620 and 850, have origination loan-to-value ratios of less than 1.5, have terms of 15, 20, or 30 years, are located in U.S. MSAs outside of Alaska and Hawaii, and are not transferred to a non-LPS servicer. Jumbo loans are larger than the GSE conforming limit (\$417K). Portfolio loans are not securitized. Privately securitized loans are securitized in non-GSE mortgage backed securities. GSE loans are predominantly FHLMC and FNMA but also include some GNMA and Federal Home Loan Bank loans. Delinquency is 60+ day delinquency. Foreclosure initiation is the referral of a mortgage to an attorney to initiate foreclosure proceedings. Foreclosure completion is identified by post-sale foreclosure or REO status. Modifications are identified based on observed changes to loan terms. Redefault is a return to 60+ day delinquency after a modification cures an initial delinquency.

	All Loans		Baseline Sample (Delinquent in First Year)		Full Sample (Delinquent Before 2012)	
	Jumbo	Non-Jumbo	Jumbo	Non-Jumbo	Jumbo	Non-Jumbo
Number	263,544	1,644,346	15,985	61,242	93,379	425,543
Size (mean)	\$691,219	\$210,294	\$653,155	\$230,861	\$650,601	\$230,892
FICO (mean)	733	726	700	686	712	699
LTV (mean)	0.73	0.72	0.79	0.81	0.77	0.79
Ownership						
Portfolio	27.4%	9.2%	33.2%	16.4%	25.4%	11.3%
Private Security	70.2%	9.4%	63.8%	18.6%	71.5%	15.9%
GSE	1.7%	80.9%	1.6%	64.5%	2.2%	72.4%
Delinquency						
Within 1 year	6.1%	3.7%				
Within 5 years	36.4%	26.6%				
Foreclosure Initiation						
Within 6 months			69.5%	60.1%	48.8%	49.9%
Within 1 year			80.7%	72.2%	60.7%	62.1%
Within 3 years			90.3%	86.2%	78.9%	78.9%
Foreclosure Completion						
Within 6 months			13.5%	12.4%	5.7%	6.6%
Within 1 year			36.9%	29.3%	17.9%	18.4%
Within 3 years			58.1%	54.7%	36.9%	42.0%
Modification						
Within 6 months			5.2%	3.0%	7.1%	7.3%
<i>interest decrease</i>			0.4%	0.6%	2.4%	4.7%
<i>term extension</i>			0.2%	0.7%	2.7%	3.5%
<i>principal decrease</i>			0.1%	0.0%	0.4%	0.3%
<i>principal increase</i>			4.8%	2.2%	3.6%	2.9%
Within 1 year			8.5%	6.3%	13.6%	15.5%
Within 3 years			12.3%	13.9%	23.5%	26.5%
Redefault						
Within 1 year			71.5%	73.2%	30.2%	27.5%

of the rest (27%) were held as portfolio loans. By contrast, 81% of non-jumbo loans were securitized by the GSEs. Delinquency is common in both sub-samples. 6% of jumbo loans became seriously (60+ days) delinquent within 1 year, and 36% became seriously delinquent within five years. Similarly, 4% of non-jumbo loans became seriously delinquent within 1 year and 27% became seriously delinquent within 5 years.

All of my analysis is conditional on mortgages becoming seriously delinquent, which I define as delinquencies of at least 60 days. I split the sample based on when a loan first became seriously delinquent. The baseline sample consists of loans that became seriously delinquent within twelve months of origination. I use the twelve month delinquency cutoff to focus on a time period before significant government intervention in the mortgage market.¹⁴ The baseline sample has 16,000 jumbo loans and 61,000 non-jumbo loans. The full sample, which consists of all loans that became seriously delinquent before the end of 2011, has 93,000 jumbo loans and 426,000 non-jumbo loans. The jumbo and non-jumbo loans clearly differ in size. Jumbo loans also tend to have slightly higher FICO scores. Loan-to-value (LTV) ratios are almost identical across jumbo and non-jumbo loans.

Identifying delinquencies is straight-forward because LPS includes data on payment status. Consistent with previous studies, I use the Mortgage Bankers Association's (MBA) definition of 60+ day delinquency. Foreclosures are also identified in the LPS data. I consider both foreclosure initiation, the referral of a loan to an attorney for foreclosure, and foreclosure completion, indicated by postsale foreclosure or real estate owned (REO) status. Piskorski, Seru, and Vig (2010) and Adelino, Gerardi, and Willen (2011b) study foreclosure completion, which has the nice property of being a final resolution. On the other hand, foreclosure initiation is a more direct servicer decision and is more common within my six-month window of analysis. As reported in Table 1.1, in the baseline sample foreclosure is initiated within six months of first serious delinquency for 70% of jumbo loans and completed for 14%. Foreclosure rates are slightly lower for non-jumbo loans and

¹⁴The twelve month cutoff combined with a six month analysis window ends the analysis in February of 2009, before the Home Affordable Modification Program (HAMP) was implemented.

decrease over time, driving down foreclosure rates in the full sample.

Identifying loan modifications is more complicated because they are not directly recorded in the LPS data. Nonetheless, modifications can be imputed from month-to-month changes in interest rates, principal balances, and term lengths. For example, an interest rate reduction on a fixed rate mortgage must be due to a mortgage modification. My algorithm for identifying loan modifications, described in Appendix A, is essentially the same as the algorithm employed by Adelino, Gerardi, and Willen (2011b). Broadly, I consider two (potentially overlapping) types of modifications: concessionary modifications that reduce monthly payments by decreasing interest rates, decreasing principal balances, or extending loan terms; and modifications to make loans current by capitalizing past due balances. The loan modification algorithm looks for evidence of either of these patterns.

A limitation of the loan modification algorithm is that it does not identify modifications that do not change interest rates, term to maturity, or principal balances. In particular, it does not capture temporary payment plans or principal forbearance. In order to work, the algorithm requires monthly data on interest rates, term to maturity, and principal balances. This is universally available for interest rates and principal balances. Monthly term to maturity data, on the other hand, is only available for about half of the loans in my sample. I limit my modification analysis to these loans.

In my baseline jumbo sample, 5.2% of seriously delinquent jumbo loans were modified within six months. These modifications were overwhelmingly principal-increasing as opposed to concessionary. In the full sample, the six-month jumbo modification rate was 7.1% and included interest rate reductions (2.4%), term extensions (2.7%), and principal increases (3.6%).

1.3.2 Instrumental Variables Methodology

I exploit the sudden and unexpected freeze of private mortgage securitization in the third quarter of 2007 to identify private securitization. Loans originated shortly before the freeze are similar to loans originated earlier in the year but were significantly less likely to be

securitized. My identification strategy is analogous to Bernstein's (2012) instrument for public ownership. Bernstein exploits the fact that NASDAQ returns shortly after an IPO announcement are uncorrelated with firm prospects but predict whether the IPO will be completed. In both Bernstein's setting and my own, ownership structure is endogenous but is influenced by effectively random shocks to related asset markets.

Purnanandam (2011) also documents and exploits loans being stuck on bank balance sheets in 2007. Using bank-level call report data, Purnanandam shows that banks with heavy exposure to originate-to-distribute lending were stuck holding loans that were intended for sale. These banks subsequently suffered higher delinquency rates and charge offs than other banks, consistent with originate-to-distribute loans being lower quality than other loans. In contrast, I exploit time series variation in securitization rates by loan origination month to control for origination quality differences and estimate the impact of securitization on mortgage servicing.

Mortgage securitization comes in two forms. Most residential mortgages are securitized by Fannie Mae or Freddie Mac (the Government Sponsored Entities, GSEs). However, not all mortgages qualify for GSE securitization. A loan may fail to conform to GSE standards either because it fails their underwriting standards (subprime loans) or because it exceeds their loan limits (jumbo loans). Starting in the 1990s and growing rapidly in the early 2000s, liquid private markets arose to securitize subprime and jumbo loans. In 2006, \$1.1 trillion of private mortgage backed securities (MBS) were issued, including \$200 billion backed by jumbo mortgages.¹⁵

Private mortgage securitization abruptly halted in the third quarter of 2007 and has essentially remained frozen since then. Figure 1.1 plots prime securitization volume from 2000 to 2011. Jumbo prime MBS issuance topped \$55 billion dollars in quarters 1 and 2 of 2007 then crashed to \$38 billion in Q3 and \$18 billion in Q4, followed by almost no issuance after 2007. The private securitization freeze was simultaneous with the August 2007 collapse of asset-backed commercial paper, previously a \$1.2 trillion market that was

¹⁵Source: Inside Mortgage Finance.

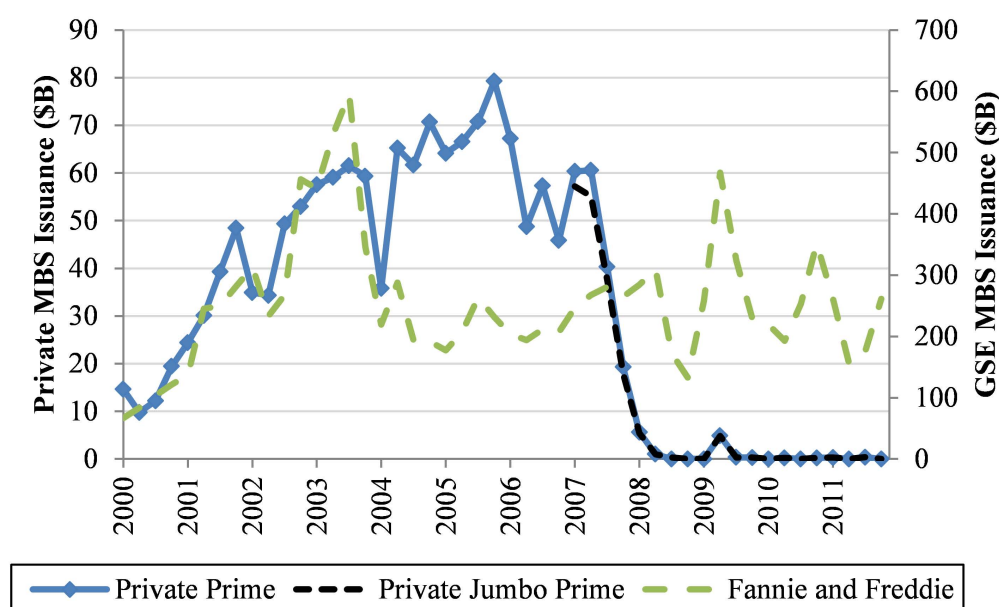


Figure 1.1: MBS Issuance

Prime mortgage backed security (MBS) issuance volume by quarter. Private issuance is plotted on the left axis. Fannie Mae and Freddie Mac (GSE) issuance is plotted on the right axis.

heavily invested in MBS. Both freezes were unanticipated and appear to have been caused by sudden increases in investor apprehension of mortgage backed securities, particularly subprime MBS.¹⁶ Consistent with this view, ABX price indices for AAA subprime MBS fell below unity for the first time shortly before the market freeze (see Figure 1.2).¹⁷ GSE credit guaranties prevented similar fears in the GSE MBS market, which continued to issue securities uninterrupted throughout 2007 and the rest of the financial crisis (see Figure 1.1).

I use the August 2007 private securitization freeze as a natural experiment for jumbo securitization. Because the freeze was unanticipated, it did not affect origination decisions until after it occurred. This is the exclusion restriction underlying my identification strategy. To confirm that it is a reasonable assumption, I plot monthly mortgage originations by

¹⁶Kacperczyk and Schnabl (2010) document the collapse of asset backed commercial paper and identify the July 31, 2007 bankruptcy filing two Bear Stearns hedge funds that invested in subprime mortgages and the August 7, 2007 suspension of withdrawals at three BNP Paribas funds as the catalysts of the collapse. Callem, Covas, and Wu (2011) and Fuster and Vickery (2012) discuss the private MBS issuance freeze, which they date to August 2007 and exploit as a liquidity shock to jumbo lending.

¹⁷Markit ABX indices track the prices of credit default swaps on underlying mortgage backed securities. See Stanton and Wallace (2011) for more information.



Figure 1.2: ABX Price Index

Daily prices of the Markit ABX.HE.06-1 AAA index, which consists of Credit Default Swaps (CDS) on AAA supprime MBS issued in the second half of 2005.

month in Figure 1.3. Jumbo originations tracked non-jumbo originations and stayed in the neighborhood of 30,000 originations per month until August of 2007. Jumbo lending then dramatically fell in September of 2007 while non-jumbo lending (which was largely unaffected by private securitization) remained steady. This is exactly the response we would expect from an unexpected freeze in private securitization. The appendix includes plots of loan characteristics by origination month. This evidence supports the origination volume data in Figure 1.3. Loan size, credit scores, loan-to-value ratios, and documentation levels were fairly stable from January to August of 2007, and jumbo and non-jumbo loans followed similar patterns. Jumbo interest rates tracked non-jumbo interest rates from January to August of 2007 and then increased in September relative to non-jumbo interest rates.

Though the freeze did not affect pre-freeze origination decisions, it did affect the probability that these mortgages were securitized. Assembling a pool of loans, selling them to an MBS sponsor, and closing on an MBS deal often takes a few months. Table 1.2 highlights this lag. Within my sample of January 2007 originations, only 12% of jumbo loans

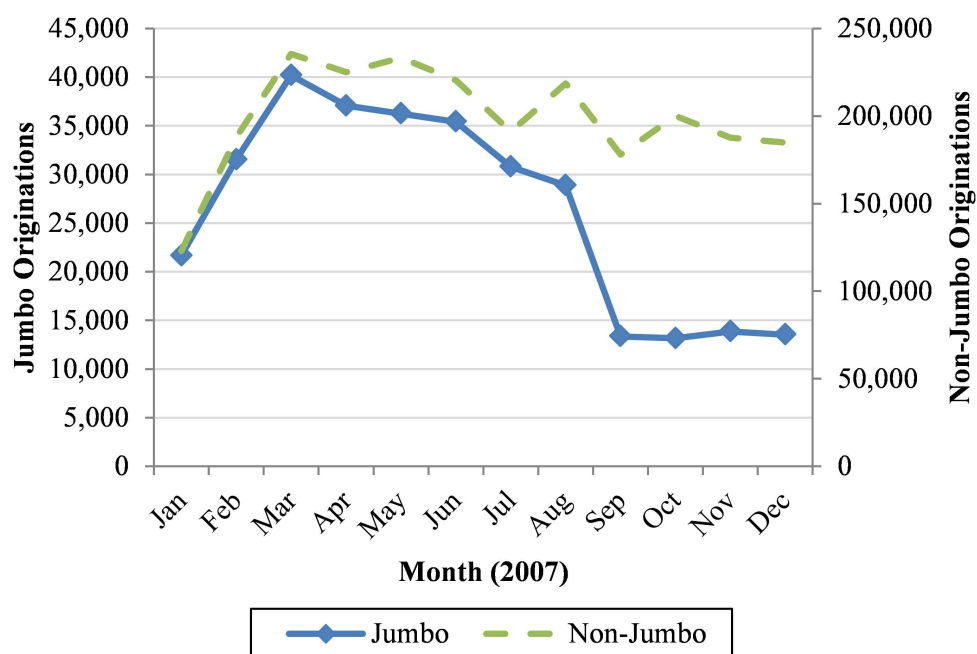


Figure 1.3: Mortgage Originations

Sample loan originations by month and size. Jumbo mortgages are loans over \$417K, the conforming limit for Fannie Mae and Freddie Mac.

Table 1.2: Securitization by Age for January Jumbo Loans

Data includes all jumbo sample loans that were originated in January of 2007. Age is months since origination. Loans are added to the LPS data over time and can change ownership. Number of loans and percent of loans privately securitized is reported by age.

Age (months)	Loans	% Privately Securitized
0	12,715	12%
1	18,208	43%
2	19,069	66%
3	20,338	75%
4	21,023	78%
5	21,558	79%
6	21,811	79%

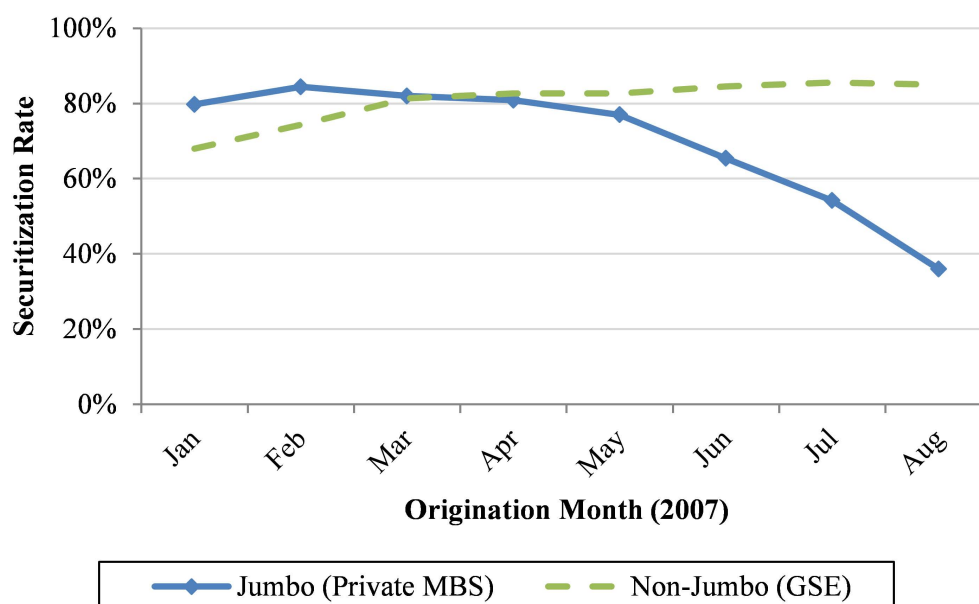


Figure 1.4: *Securitization Rates by Origination Month*

Percent of jumbo sample loans that are privately securitized and percent of non-jumbo sample loans that are securitized by Fannie Mae and Freddie Mac (the GSEs) by origination month. Securitization is measured as of six months after origination.

were privately securitized in their origination month. By two months after origination, 66% were privately securitized. Private securitization further increased to 79% by six months after origination.

As 2007 progressed, less and less time was available to securitize new originations before the freeze. As a result, the probability of securitization dropped dramatically in the summer of 2007. Figure 1.4 plots private securitization rates six months after origination for jumbo loans in my sample by origination month. This is essentially the first stage regression for my identification strategy. Jumbo private securitization rates were around 80% until April and then started to decline, with dramatic drops in the summer to 65% in June, 54% in July, and 36% in August. Over this time period, the volume of portfolio loans increased from 6,500 in April to 17,900 in August, consistent with lenders being stuck holding portfolio loans they had anticipated securitizing. By contrast, non-jumbo GSE securitization rates remained steady at around 85% throughout 2007.

My baseline empirical strategy is to estimate equations of the form:

$$Pr(Y_i | Delinquency_i) = \alpha + \gamma Sec_i + X_i \beta_3 + \varepsilon_i \quad (1.1)$$

using origination month indicator variables as instruments for private securitization (Sec_i). The regression is conditional upon loans becoming seriously delinquent. Y_i is an indicator for foreclosure or modification within six months of first serious delinquency.¹⁸ Sec_i is an indicator for a mortgage being privately securitized six months after origination. X_i is a vector of observable loan characteristics including MSA and delinquency month fixed effects. The implied linear probability model accommodates standard IV regression techniques and readily incorporates fixed effects without biasing coefficient estimates.¹⁹

Strictly speaking, the identification strategy only requires control variables to the extent that they are correlated with origination month. Delinquency month fixed effects are important because foreclosure and modification practices changed over time and delinquency month is correlated with origination month. Other control variables are less important.²⁰ Nonetheless, I include a rich set of observable loan characteristics in X_i to increase equation (1.1)'s explanatory power and make it more directly comparable to previous studies. I control for borrower credit worthiness with an indicator for origination FICO scores above 680. I include origination loan-to-value (LTV) ratio as well as an indicator for LTV of exactly 0.8 because mortgages with an LTV of 0.8 are more likely to have concurrent second-lien mortgages (Adelino, Gerardi, and Willen, 2011b). The loan terms I control for are origination amount (through its log), origination interest rate, an indicator for fixed rate mortgages, indicators for term lengths, an indicator for mortgage insurance, and an indicator for option

¹⁸I use a six month window so that my baseline analysis ends in February of 2009, before the Home Affordable Modification Program (HAMP) took effect.

¹⁹Angrist and Pischke (2009) advocate using linear IV (two stage least squares) even when the outcome and endogenous regressor are both binary, as they are here. The alternative is to estimate a bivariate probit model, which requires more restrictive distributional assumptions and cannot accommodate a large number of fixed effects (e.g., MSA fixed effects) without biasing results. As a robustness check, I estimate bivariate probit models and find that they produce similar results.

²⁰In the appendix I estimate a version of equation (1.1) without loan characteristics. Results are consistent with my baseline estimates.

ARM mortgages. I control for the quality of underwriting with indicators for low income documentation and no income documentation, and I control for loan purpose with indicators for refinancing, primary residence, and single family homes. I also control for MSA fixed effects.

Figure 1.5 plots baseline sample first stage and reduced form origination month fixed effects for equation (1.1).²¹ Jumbo foreclosure initiation (panel A), foreclosure completion (panel B), and modification (panel C) origination month fixed effects were fairly constant until April 2007. After April, jumbo foreclosure probability decreased and jumbo modification probability increased as jumbo private securitization probability (the first stage) decreased. The IV regressions in the next section add coefficient estimates and standard errors, but the basic relationships are clear from the reduced form plots. Private securitization increases the probability of foreclosure and decreases the probability of modification.

One potential concern with this identification strategy is that the mortgage lending environment may have changed over the course of 2007 resulting in differences between origination month cohorts even though the securitization freeze was unanticipated. Fortunately, I have a natural control group that was not affected by the securitization freeze. Prime non-jumbo loans are predominately securitized by the GSEs, and GSE securitization was uninterrupted throughout 2007. Figure 1.5 also plots the reduced form of equation (1.1) for non-jumbo loans. Non-jumbo foreclosure and modification origination month fixed effects were largely flat over the sample period, suggesting that any changes to the lending environment between January and August of 2007 did not have a major impact foreclosure and modification practices.

As a robustness check, I control for origination month fixed effects by estimating

²¹Figure 1.5 corresponds to the IV regressions reported in Table 1.4. The first stage is identical across the three regressions except that the modification regression is limited to loans that report term length data. This results in slightly different jumbo private securitization fixed effects in Panel C.

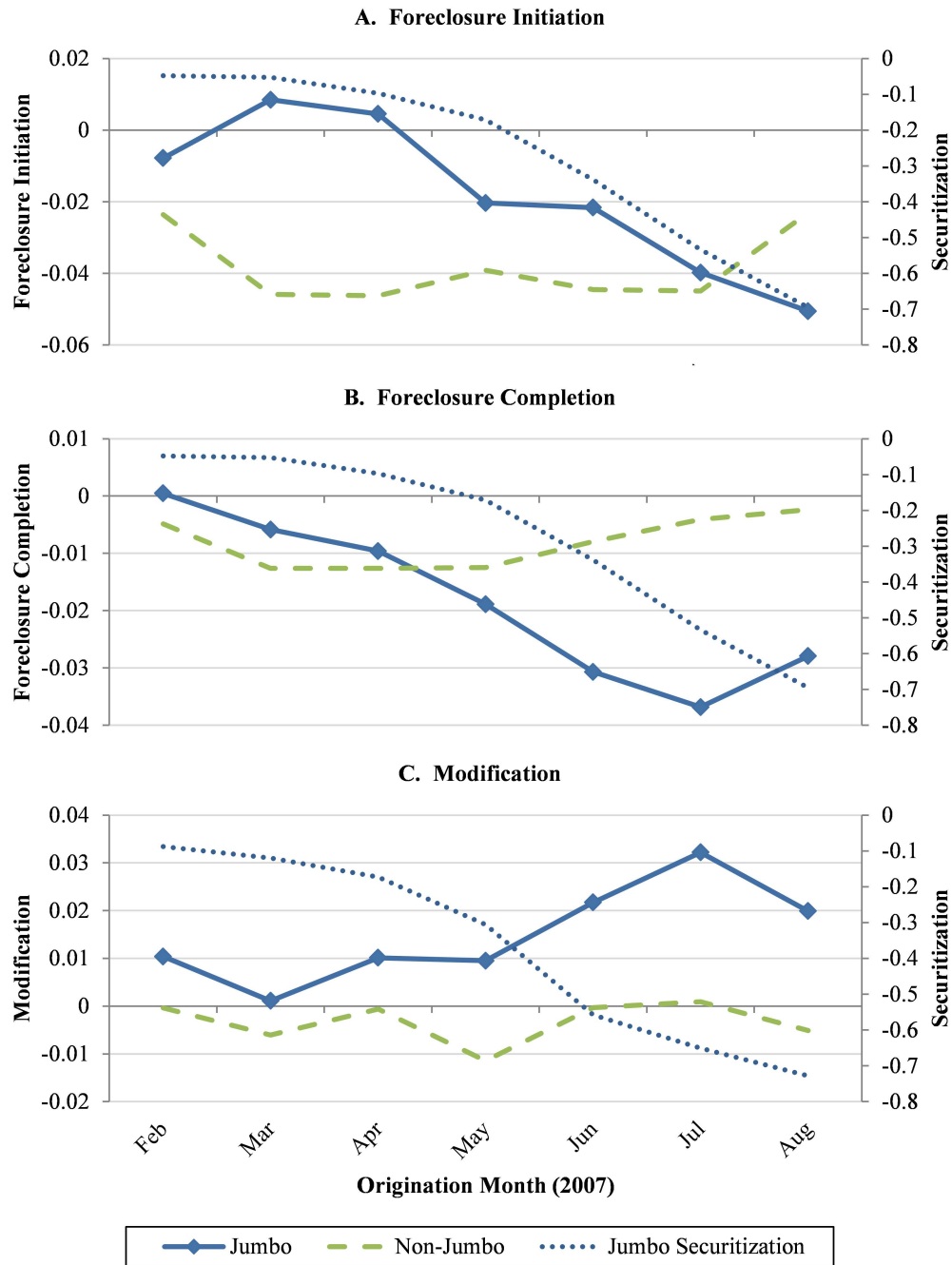


Figure 1.5: Reduced Form Regression Fixed Effects

Jumbo fixed effects are from the reduced form of the baseline IV regressions reported in Table 4. Non-jumbo fixed effects are for identical regressions estimated for non-jumbo loans. All fixed effects are relative to January.

equations of the form:

$$\begin{aligned} Pr(Y_i | Delinquency_i) = & \alpha + \gamma Sec_i + \beta_1 Jumbo_i + \beta_2 NonJumbo_i * Sec_i \\ & + OrigMonth_i \beta_3 + X_i \beta_4 + NonJumbo_i * X_i \beta_5 + \epsilon_i \end{aligned} \quad (1.2)$$

using $Jumbo_i * OrigMonth_i$ indicator variables as instruments for private securitization (Sec_i). As before, Y_i is an indicator for foreclosure or modification within six months of first serious delinquency, and Sec_i is an indicator for a mortgage being privately securitized six months after origination. $Jumbo_i$ is an indicator for jumbo status. $NonJumbo_i * Sec_i$ is the interaction between private securitization and non-jumbo status.²² $OrigMonth_i$ is a vector of origination-month dummy variables. X_i is a vector of the same loan characteristics and fixed effects included in equation (1.1). Conceptually, equation (1.2) estimates separate regressions for jumbo and non-jumbo loans except that the origination-month fixed effects estimated with non-jumbo loans are applied to the jumbo regressions. The reduced form of equation (1.2) is a difference in differences regression of Y_i (foreclosure or modification) on origination month exploiting differences between jumbo loans (the treated group) and non-jumbo loans (the control group).

The remaining concern is that something changed between January and August of 2007 differentially in the jumbo lending environment relative to the non-jumbo lending environment. I cannot fully rule this out, but the overall evidence suggests that jumbo lending was fairly stable and moved in parallel with non-jumbo lending until August of 2007. Even if there were time-series changes specific to jumbo lending, they are unlikely to rival the drop in jumbo private securitization from 80% in April to 36% in August.

²²Including the $NonJumbo_i * Sec_i$ interaction allows for the possibility that private securitization has a different impact on jumbo and non-jumbo loans. I include this interaction variable directly in the regression (i.e., without an instrument) even though it is endogenous. This is less of a problem because I am not interested in the β_2 coefficient. In the appendix, I estimate a version of equation (1.2) without $NonJumbo_i * Sec_i$ and obtain larger γ estimates, suggesting that equation (1.2) is a conservative specification.

1.4 Results

1.4.1 Baseline Results

I start by estimating the effect of private securitization on foreclosure and modification in my baseline sample of jumbo loans that became seriously delinquent within one year of origination. This time period is most directly comparable to previous studies and is relatively free of government policy interventions. Because the last originations in my sample are in August of 2007, the twelve-month delinquency window combined with my six-month analysis window ensures that the last month analyzed is February of 2009, which is before the Home Affordable Modification Program (HAMP) was implemented. Later, I consider all loans that became seriously delinquent before 2012 to assess whether the effect of securitization on foreclosure and modification changed over time.

Before implementing my instrumental variables strategy, I first estimate equation (1.1) with origination month fixed effects using OLS regressions. Coefficient estimates and standard errors (clustered by MSA) are reported in Table 1.3. After controlling for observable loan characteristics, seriously delinquent securitized loans are 3.9 ppt more likely to have foreclosure initiated, 2.2 ppt more likely to have foreclosure completed, and 3.1 ppt less likely to be modified within six months.²³ 97% of sample jumbo loans are privately securitized or held as portfolio loans so the coefficients estimate differences between these two groups. The samples for the three regressions are identical with one exception. As discussed in the previous section, I can only consistently identify modifications for loans that report their term to maturity on a monthly basis. This decreases the modification regression sample size by about 50%.

Like previous studies, my OLS regressions are not conducive to causal interpretation

²³The coefficients are slightly lower than Piskorski, Seru, and Vig's (2010) 4-7 ppt foreclosure bias estimate and Agarwal, et al.'s (2011) -4.2 ppt modification bias estimate. Given that I analyze only jumbo loans instead of all loans and that my sample covers a slightly different time period and uses a shorter analysis window than Piskorski, Seru, and Vig (2010), my OLS results are generally consistent with these previous findings. By contrast my results conflict with the approximately equal modification rates of Adelino, Gerardi, and Willen (2011b). This is likely due to the sample period since Adelino, Gerardi, and Willen (2011b) show that the modification gap between portfolio loans and privately securitized loans grew over time.

Table 1.3: OLS Regressions

The dependent variables are indicators for foreclosure initiation, foreclosure completion, and modification within six months of first serious (60+ days) delinquency. All regressions are OLS. Privately securitized is an indicator for private securitization as of six months after origination. The regressions analyze baseline sample jumbo loans, which became seriously (60+ days) delinquent within one year of origination. The modification regression is restricted to mortgages with term length data. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) OLS	(2) OLS	(3) OLS
	Foreclose Start	Foreclose	Modify
Mean	0.695	0.135	0.052
Privately Securitized	0.039*** (0.011)	0.022*** (0.008)	-0.031*** (0.005)
FICO >= 680	0.087*** (0.008)	0.032*** (0.008)	-0.044*** (0.006)
LTV Ratio	0.630*** (0.051)	0.046 (0.040)	0.018 (0.045)
LTV = 80	0.031*** (0.010)	0.018** (0.007)	-0.008* (0.004)
log(Origination Amount)	-0.0003 (0.013)	-0.028*** (0.011)	0.000 (0.008)
Origination Interest Rate	0.003 (0.002)	-0.001 (0.001)	-0.023*** (0.003)
Fixed Interest Rate	-0.095*** (0.012)	-0.067*** (0.009)	0.002 (0.007)
Term = 15 Years	-0.180*** (0.068)	-0.049 (0.036)	-0.042*** (0.013)
Term = 20 Years	-0.233 (0.157)	0.008 (0.107)	-0.007 (0.026)
Insurance	-0.091*** (0.018)	0.010 (0.009)	0.018 (0.011)
Refinancing Loan	-0.075*** (0.008)	-0.038*** (0.007)	-0.001 (0.005)
Option ARM	0.009 (0.012)	0.006 (0.007)	0.063*** (0.009)
Single Family Home	0.006 (0.010)	-0.013 (0.009)	-0.018*** (0.006)
Primary Residence	0.009 (0.016)	-0.001 (0.011)	-0.002 (0.008)
No Income Documentation	0.0001 (0.014)	0.009 (0.010)	-0.004 (0.008)
Low Income Documentation	-0.085*** (0.012)	-0.027*** (0.006)	0.005 (0.004)
Delinquency Month FE	Yes	Yes	Yes
Origination Month FE	Yes	Yes	Yes
MSA FE	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No
Observations	15,945	15,945	7,893
Adjusted R-Squared	0.083	0.030	0.089

because securitization status may be correlated with unobserved (and thus omitted) loan characteristics that explain part of the residual of equation (1.1). As discussed in the previous section, the direction of the omitted variable bias is theoretically ambiguous. Even assuming securitized loans are unobservably lower quality, the impact of loan quality on foreclosure and modification conditional on delinquency could be positive or negative. This ambiguity is apparent in the OLS control variable coefficient estimates. Some measures of quality increase foreclosure probability while others decrease it. For example, a high FICO score increases the probability of foreclosure initiation within six months by 8.7 ppt whereas a low loan-to-value ratio decreases the same probability (see column (1) of Table 1.3).

Table 1.4 addresses the omitted variable problem by using origination month to instrument for jumbo securitization status. Coefficients are estimated using two stage least squares. Standard errors are clustered by MSA. Control variables are the same as in the Table 1.3 OLS regression except that origination month is now used as an instrument for private securitization.

Column (1) reports the first stage regression of private securitization on origination month.²⁴ As discussed earlier, securitization probability decreased dramatically during the summer of 2007. The first stage regression shows the same pattern after controlling for observable loan characteristics. Origination month fixed effects decreased over the course of 2007 with a particularly sharp decline after April. The August origination month fixed effect is -69.5 ppt compared to loans originated in January. Origination month is a powerful predictor for securitization. The within-MSA adjusted R-squared for the first stage regression is 0.32, and the Kleibergen-Paap F statistic is 396. In short, weak identification is not a problem.

Columns (2) to (4) of Table 1.4 report instrumental variables estimates for equation (1.1). Conditional on serious delinquency, private securitization increases the six-month probability of foreclosure initiation by 8.0 ppt and foreclosure completion by 4.7 ppt.

²⁴The reported first stage results use the entire jumbo baseline sample, which is also used for the foreclosure initiation and foreclosure completion regressions. The modification regression uses a reduced sample and has slightly different first stage estimates, which are plotted in Figure 1.5.

Table 1.4: Baseline IV Regressions

The dependent variables are indicators for foreclosure initiation, foreclosure completion, and modification within six months of first serious (60+ days) delinquency. The regressions estimate linear probability models for these indicators using origination month indicators as instruments for private securitization status six months after origination. All observable loan characteristics shown in Table 3 are included as unreported controls. The regressions analyze baseline sample jumbo loans, which became seriously (60+ days) delinquent within one year of origination. The modification regression is restricted to mortgages with term length data. The weak identification test is a Kleibergen-Paap F statistic. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) OLS	(2) IV	(3) IV	(4) IV
	Privately Securitized	Foreclose Start	Foreclose	Modify
Mean	0.638	0.695	0.135	0.052
Privately Securitized		0.080*** (0.016)	0.047*** (0.012)	-0.036*** (0.009)
February Origination	-0.048*** (0.015)			
March Origination	-0.053*** (0.015)			
April Origination	-0.097*** (0.016)			
May Origination	-0.171*** (0.021)			
June Origination	-0.338*** (0.022)			
July Origination	-0.533*** (0.020)			
August Origination	-0.695*** (0.019)			
Loan Characteristic Controls	Yes	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes	Yes
Origination Month FE		No	No	No
MSA FE	Yes	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No	No
Observations	15,945	15,945	15,945	7,893
Adjusted R-Squared	0.324	0.082	0.029	0.090
Weak Identification F-stat	396			

Private securitization decreases the six-month probability of modification by 3.6 ppt. The coefficient estimates are all statistically significant (standard errors range from 0.9 ppt to 1.6 ppt). Moreover, they are economically large. As percentages of mean rates, the foreclosure initiation coefficient is 12%, the foreclosure completion coefficient is 35%, and the modification coefficient is 69%. Comparing columns (2) to (4) of Table 1.4 to Table 1.3 reveals the omitted variable bias of the OLS regressions. For foreclosure initiation and completion, the IV securitization coefficient estimates are about twice as large as their OLS counterparts. On the other hand, the OLS and IV estimates are similar for modification. It appears that unobserved quality differences between securitized and portfolio loans make securitized loans less likely to be foreclosed without having much effect on modification. As a result OLS underestimates the causal impact of securitization on foreclosure.

1.4.2 Interpreting the Results

The IV estimates of Table 1.4 estimate the Local Average Treatment Effect (LATE) of private securitization on foreclosure and modification. The securitization freeze instrument affected securitization probability for loans that would have been securitized after a delay. The IV methodology cannot estimate the impact of securitization on non-compliers, in this case mortgages that never would have been securitized and mortgages that were securitized quickly enough to avoid the freeze. Is LATE likely to differ from the Average Treatment Effect (ATE) of securitization on all loans? No. First, the instrument is very strong (e.g., the August first stage fixed effect is -69.5 ppt), suggesting that most mortgages are compliers. Second, there is no a priori reason to think that speed of securitization is correlated with the treatment effect. If the treatment effect does vary across loans, the loans and originators with the smallest treatment effect are likely the most inclined to securitization (because a smaller treatment effect makes securitization less costly). Thus, if anything LATE is likely conservative relative to ATE.

The treatment itself is also slightly nuanced in the IV regression. Specifically, the IV treatment is being stuck holding loans intended for securitization. If pre-planning aids

portfolio loan servicing or if the entities stuck holding the loans don't typically engage in portfolio lending, this treatment is slightly different from a planned change in securitization practices. To the extent that it matters, the lack of pre-planning likely decreases an owner's ability to differentially service portfolio loans, thereby making the IV estimates conservative.

A final issue of interpretation is how broadly to extrapolate the results. Strictly speaking, my baseline regressions estimate the impact of private securitization on foreclosure and modification of jumbo loans originated in 2007 that became delinquent within one year of origination. In later regressions, I show that similar results also hold for loans that became delinquent at other times. I focus on 2007 originations solely for identification purposes. As far as I know, there is nothing special about 2007 origination practices so my coefficient estimates should be valid for jumbo loans originated at other times. The estimates are also informative about private securitization of non-jumbo loans (e.g., subprime loans). Exact magnitudes may differ, but the same basic frictions of private securitization likely apply there as well. My results are less informative about GSE securitization because GSE securitization involves different contracts and leaves a single entity (the GSE) with full credit exposure for the underlying mortgages.

1.4.3 Robustness Checks

One difference between my empirical design and that of Piskorski, Seru, and Vig (2010) and Adelino, Gerardi, and Willen (2011b) is that I use a six month analysis window instead of considering loans for a longer period of time after delinquency.²⁵ The shorter window is desirable because it ends before HAMP, but it creates the possibility that I am picking up acceleration or deceleration in foreclosure and modification as opposed to changes to their ultimate probability. Columns (1) to (3) of Table 1.5, Panel A address this concern by replicating my baseline results with a twelve-month window instead of a six-month window. The coefficient estimates are consistent with my baseline results. The foreclosure start

²⁵Piskorski, Seru, and Vig (2010) consider all foreclosure actions up to the first quarter of 2008, which could be as much as three years after a loan becomes seriously delinquent. Adelino, Gerardi, and Willen (2011b) use a twelve-month analysis window.

Table 1.5: Robustness Checks

Regressions are the same as columns 2-4 of Table 4 except where noted. Columns 1-3 of Panel A consider foreclosure and modification within twelve months instead of six months. Columns 4-6 of Panel A analyze only loans originated between May and July of 2007. Columns 1-3 of Panel B control for origination-month fixed effects using non-jumbo loans. Columns 4-6 of Panel B estimate bivariate probit models without MSA fixed effects. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

<i>A. 12-month analysis window and restricted origination-month sample</i>						
	(1) IV	(2) IV	(3) IV	(4) IV	(5) IV	(6) IV
	Foreclose Start (12 mos.)	Foreclose (12 mos.)	Modify (12 mos.)	Foreclose Start (6 mos.)	Foreclose (6 mos.)	Modify (6 mos.)
Mean	0.807	0.369	0.085	0.669	0.109	0.061
Privately Securitized	0.081*** (0.013)	0.061*** (0.016)	-0.066*** (0.014)	0.078** (0.035)	0.042* (0.023)	-0.080*** (0.025)
Loan Characteristics	Yes	Yes	Yes	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes	Yes	Yes	Yes
Origination Month FE	No	No	No	No	No	No
MSA FE	Yes	Yes	Yes	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug	May-Jul	May-Jul	May-Jul
Include Non-Jumbo Loans	No	No	No	No	No	No
Observations	15,945	15,945	7,893	6,443	6,443	3,259
Adjusted R-Squared	0.045	0.072	0.100	0.074	0.017	0.066
<i>B. Non-jumbo origination month control regressions and bivariate probit models</i>						
	(1) IV	(2) IV	(3) IV	(4) Bivariate Probit	(5) Bivariate Probit	(6) Bivariate Probit
	Foreclose Start (6 mos.)	Foreclose (6 mos.)	Modify (6 mos.)	Foreclose Start (6 mos.)	Foreclose (6 mos.)	Modify (6 mos.)
Mean	0.695	0.135	0.052	0.695	0.135	0.052
Privately Securitized	0.097*** (0.019)	0.059*** (0.015)	-0.027** (0.012)	0.068*** (0.016)	0.041** (0.014)	-0.019 (0.012)
Loan Characteristics	Yes	Yes	Yes	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes	Yes	Yes	Yes
Origination Month FE	Yes	Yes	Yes	No	No	No
MSA FE	Yes	Yes	Yes	No	No	No
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	Yes	Yes	Yes	No	No	No
Observations	77,160	77,160	35,934	15,980	15,980	7,931
Adjusted R-Squared	0.083	0.037	0.073			

coefficient (8.1 ppt) is almost identical. The foreclosure completion coefficient is somewhat larger (6.1 ppt compared to 4.7 ppt). The modification coefficient is more significantly larger (-6.6 ppt compared to -3.6 ppt). The increases are likely due to the higher incidence of foreclosure completion and modification within the twelve-month window. In short, my baseline results appear to reflect permanent effects as opposed to changes in timing.

Another potential concern is that the jumbo lending environment changed between January and August of 2007 or that the securitization freeze was anticipated, particularly late in the sample. The best evidence against this concern is that the jumbo private securitization rate stayed stable in the 80-85% range from January to April and then dropped dramatically to 36% by August without a significant drop in originations until September (see Figures 1.3 and 1.4). Loan volume would have dropped sooner if the securitization freeze was anticipated, and other changes to jumbo lending this sudden and large are unlikely especially after controlling for observable characteristics. Nonetheless, I address the concern by restricting the sample and estimating origination-month fixed effects with non-jumbo loans.

The restricted sample focuses on loans originated between May and July of 2007. The probability of securitization dropped significantly over these three months from 77% in May to 54% in July, and ending the sample before August reduces the concern that securitization market changes may have been anticipated at the time of origination. Columns (4) to (6) of Table 1.5, Panel A show regression estimates for the restricted sample. Standard errors are larger, but the foreclosure coefficient estimates are nearly identical to my baseline results. The modification coefficient is larger in the restricted sample (-8.0 ppt compared to -3.6 ppt), suggesting that my baseline results are conservative.

To explicitly control for changes to the lending environment over time, I estimate equation (1.2) using interactions between origination month indicator variables and jumbo status as instruments for private securitization. As discussed earlier, this difference in differences strategy controls for origination month fixed effects using non-jumbo loans while using the interacted version of origination month to instrument for jumbo securitization.

Results are reported in Columns (1) to (3) of Table 1.5, Panel B. Foreclosure initiation (9.7 ppt), foreclosure completion (5.9 ppt), and modification (-2.7 ppt) coefficient estimates are all close to their baseline values.

In Columns (4) to (6) of Table 1.5, Panel B, I report marginal effect estimates from bivariate probit models. As discussed by Wooldridge (2002), this specification implements instrumental variables identification while bounding outcome (foreclosure or modification) and treatment (securitization) probabilities between 0 and 1 with probit functions. To avoid biases associated with a large number of fixed effects, I drop the MSA fixed effects. The marginal effects of private securitization on foreclosure initiation (6.8 ppt) and foreclosure completion (4.1 ppt) are close to my baseline estimates. The modification marginal effect (-1.9 ppt) is lower than my baseline estimate.

In the appendix, I consider three additional robustness tests: dropping loan characteristic control variables, estimating equation (1.2) without the $NonJumbo_i * Sec_i$ interaction term, and including mortgages that are transferred to non-LPS servicers. Results are consistent with my baseline estimates.

1.4.4 Full Sample Results

So far my analysis has focused on my baseline sample of loans that became seriously delinquent within twelve months of origination. The rationale for starting with this sample is that it ends the analysis in February of 2009, before significant government intervention into the mortgage market. The baseline sample time period (primarily 2007 and 2008) also represents the heart of the financial crisis and was a time when servicers may have been overwhelmed by a surge in delinquencies.

To assess whether my baseline results are specific to 2007 and 2008, I repeat my analysis on the full sample of all jumbo loans that became seriously delinquent before 2012. Table 1.6 reports the results. The full sample private securitization coefficient estimates are 12.4 ppt for foreclosure initiation, 2.8 ppt for foreclosure completion, and -5.1 ppt for modification (25%, 49%, and 72%, respectively, as a percent of mean rates). Compared to the baseline

Table 1.6: Full Sample IV Regressions

Regressions are the same as in Table 4 except that the sample is expanded to include all jumbo sample loans that became delinquent prior to 2012. The dependent variables are indicators for foreclosure initiation, foreclosure completion, and modification within six months of first serious (60+ days) delinquency. The regressions estimate linear probability models for these indicators using origination month indicators as instruments for private securitization status six months after origination. All observable loan characteristics shown in Table 3 are included as unreported controls. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) IV	(2) IV	(3) IV
	Foreclose Start	Foreclose	Modify
Mean	0.488	0.057	0.071
Privately Securitized	0.124*** (0.007)	0.028*** (0.003)	-0.051*** (0.005)
Loan Characteristic Controls	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes
Origination Month FE	No	No	No
MSA FE	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No
Observations	93,330	93,330	48,289
Adjusted R-Squared	0.119	0.049	0.022

sample (Table 1.4) results, the foreclosure initiation coefficient is larger both in absolute terms and as a fraction of the mean foreclosure initiation rate. The foreclosure completion coefficient is lower in absolute terms but is higher as a fraction of the mean foreclosure completion rate. The modification coefficient is larger on an absolute basis and about the same size as a fraction of the mean modification rate.

To incentivize mortgage modifications and make modification practices more uniform, the Obama administration enacted the Home Affordable Modification Program (HAMP) in February of 2009. The program was rolled out over the course of 2009 and was fully operational by the end of the year. Potential HAMP modifications are evaluated using a standardized NPV test. If the NPV test indicates that modification is more beneficial to the lender than foreclosure would be, the servicer employs a four-step waterfall to

reduce monthly payments to 31% of income by first capitalizing past-due balances, then reducing interest rates to as low as 2%,²⁶ then extending loan terms to up to 40 years from the modification date, and then forbearing principal. Servicers receive \$1000 of incentive compensation per HAMP modification and success fees of up to \$1000 per year for three years for performing modifications. Borrowers can also earn up to \$1000 in principal forgiveness per year for five years for keeping modified mortgages current. HAMP does not override specific contractual restrictions, but it does create safe harbors for servicers by deeming the HAMP NPV tests to be the appropriate measure of investor welfare and deeming the waterfall modification methodology to be standard industry practice. HAMP is a voluntary program, but all major servicers participate, and participating servicers are required to use HAMP modification guidelines for all qualifying mortgages, whether they are privately securitized or held as portfolio loans.

HAMP's efficacy is the subject of an ongoing debate.²⁷ My methodology does not provide a way to test whether HAMP succeeded in reducing foreclosures, but I can assess whether it made foreclosure and modification decisions more uniform across securitized and portfolio loans. Policy makers were particularly concerned about the perceived bias of securitized loans towards foreclosure and away from modification. Was HAMP successful at mitigating this bias?

To assess post-HAMP securitization biases, I repeat my empirical strategy on subsamples of jumbo loans split by the year in which they became delinquent. Table 1.7 reports the results. Foreclosure initiation coefficients (Panel A) had no clear trend over time. If anything, they were higher in 2010 and 2011 after HAMP was implemented, especially when considered as a fraction of mean foreclosure initiation rates, which declined over time. Foreclosure completion coefficients (Panel B) declined over time on an absolute basis but

²⁶Interest rate reductions are permanent unless they are reduced below prevailing interest rates, which establish an Interest Rate Cap. If interest rates are reduced below the cap, they stay at the reduced level for five years and then are gradually increased to the cap.

²⁷For example, Agarwal, et al. (2012a) argue that HAMP increased modifications but has fallen short of program goals because of mixed servicer compliance.

Table 1.7: IV Regressions by Delinquency Year

Regressions are the same as in Table 6 except that the sample is split by the year in which a mortgage first becomes seriously (60+ days) delinquent. The dependent variables are indicators for foreclosure initiation (panel A), foreclosure completion (panel B), and modification (panel C) within six months of first serious delinquency. The regressions estimate linear probability models for these indicators using origination-month indicators as instruments for private securitization status six months after origination. All observable loan characteristics shown in Table 3 are included as unreported controls. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

<i>A. Foreclosure initiation within six months</i>					
	(1) IV	(2) IV	(3) IV	(4) IV	(5) IV
Delinquency Year	2007	2008	2009	2010	2011
Mean	0.766	0.573	0.460	0.318	0.396
Privately Securitized	0.079*** (0.029)	0.125*** (0.016)	0.119*** (0.013)	0.167*** (0.018)	0.085*** (0.028)
Observations	7,647	27,520	32,514	15,937	9,537
Adjusted R-Squared	0.042	0.086	0.088	0.066	0.027
<i>B. Foreclosure completion within six months</i>					
	(1) IV	(2) IV	(3) IV	(4) IV	(5) IV
Delinquency Year	2007	2008	2009	2010	2011
Mean	0.173	0.064	0.036	0.035	0.048
Privately Securitized	0.062*** (0.022)	0.038*** (0.006)	0.013** (0.006)	0.036*** (0.009)	0.024** (0.010)
Observations	7,647	27,520	32,514	15,937	9,537
Adjusted R-Squared	0.002	0.032	0.013	0.022	0.031
<i>C. Modification within six months</i>					
	(1) IV	(2) IV	(3) IV	(4) IV	(5) IV
Delinquency Year	2007	2008	2009	2010	2011
Mean	0.045	0.064	0.068	0.078	0.105
Privately Securitized	-0.022* (0.013)	-0.070*** (0.009)	-0.042*** (0.010)	-0.021 (0.014)	-0.072** (0.033)
Observations	3,844	13,486	17,787	8,091	4,930
Adjusted R-Squared	0.112	0.041	0.026	0.010	0.024

increased as a fraction of mean foreclosure rates. Modification coefficients (Panel C) had no trend over time on an absolute basis and decreased moderately as a fraction of mean modification rates. With the sole exception of modification in 2010, private securitization increased foreclosure and decreased modification probability by statistically significant and economically meaningful amounts in all years. In short, there is no evidence that HAMP mitigated the bias of privately securitized loans toward foreclosure and away from modification.

Direct comparisons between pre-HAMP and post-HAMP coefficients are somewhat problematic because it is not clear exactly what the counterfactuals should be. Even aside from HAMP policy changes, the regressions consider different time periods and the loans analyzed have different ages. Nonetheless, the fact that the foreclosure and modification biases persisted after HAMP suggests that HAMP had little impact on them. At the very least we can conclude that HAMP did not fully eliminate the bias of privately securitized loans toward foreclosure and away from modification.

1.4.5 Long Term Impact

Private securitization increases the probability of foreclosure and decreases the probability of modification within six and twelve months of first serious delinquency. Do these effects also show up in longer term foreclosure and modification probabilities? How large are the long term effects? What is the total impact of private securitization on foreclosures?

To answer these questions, I estimate the impact of private securitization on foreclosure and modification over a three-year analysis window. The analyzed sample includes all jumbo loans that became seriously delinquent before 2010. Table 1.8 reports the results. Private securitization increases the three-year probability of foreclosure initiation by 8.7 ppt, increases three-year probability of foreclosure completion by 11.3 ppt, and decreases the three year probability of modification by 5.9 ppt. As a fraction of mean rates these represent impacts of 11% for foreclosure initiation, 31% for foreclosure completion, and -25% for modification.

Table 1.8: IV Regressions with a 3-Year Analysis Window (Full Sample)

Regressions are the same as in Table 6 except that the dependent variables are now foreclosure initiation, foreclosure completion, and modification within three years instead of six months. The sample is jumbo loans that became delinquent prior to 2010. The regressions estimate linear probability models using origination month indicators as instruments for private securitization status six months after origination. All observable loan characteristics shown in Table 3 are included as unreported controls. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) IV	(2) IV	(3) IV
	Foreclose Start (3 Years)	Foreclose (3 Years)	Modify (3 Years)
Mean	0.789	0.369	0.235
Privately Securitized	0.087*** (0.008)	0.113*** (0.012)	-0.059*** (0.010)
Loan Characteristic Controls	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes
Origination Month FE	No	No	No
MSA FE	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No
Observations	67,780	67,780	35,189
Adjusted R-Squared	0.082	0.149	0.085

Since September of 2008, 4.4 million homes have been foreclosed, half of which were privately securitized.²⁸ If private securitization increased the incidence of foreclosure by 31%, this means over 500,000 foreclosures are attributable to private securitization. Admittedly, this is a rough estimate. It requires extrapolation from jumbo private securitization to private securitization more generally, and it ignores the general equilibrium effects of curtailing private securitization. That said, 500,000 could actually be a conservative estimate. Subprime private securitization frictions may be even larger than jumbo frictions, and curtailing securitization may have increased loan quality, further decreasing delinquencies and foreclosures.

²⁸Foreclosure data is from the CoreLogic National Foreclosure Report, April 2013. Piskorski, Seru, and Vig (2011) and Mayer (2009) estimate that half of foreclosure initiations were privately securitized mortgages based on Federal Reserve reports and private market data.

1.4.6 Modification Details and Effectiveness

In addition to impacting the probability of modification, securitization also affects how loans are modified. Some securitized servicing contracts place limits on principal and interest reductions and modifications and term extensions. Further, servicers of securitized loans may have an incentive to keep delinquent loans alive longer through principal-increasing modifications that capitalize past due balances. Finally, servicers of securitized loans may have less incentive to invest in thoughtful screening and negotiation to give modifications the best chance of successfully preventing future default.

To assess the impact of securitization on modification terms, I employ my IV regression strategy on the subset of delinquencies that are modified. For this analysis I include all jumbo loans that became seriously delinquent before 2012 and were modified within six months. First, I consider indicators for different types of modifications as my dependent variables, thereby estimating the probability of a certain type of modification conditional on there being a modification of some kind. Except for the different sample and dependent variables, the regressions are identical to my previous IV regressions. Panel A of Table 1.9 reports the results. Securitization increases the incidence of interest modifications and principal increases, decreases the incidence of term modifications, and has no significant impact on the incidence of principal decreases.

I also consider how securitization affects net changes to interest rates, term lengths, principal balances, and monthly payments. Panel B of Table 1.9 reports results for regressions of net changes on the same variables considered in Panel A. Across all terms, privately securitized modifications are less concessionary. Even though a higher fraction of privately securitized modifications involve interest rate decreases, the average interest rate decrease is 39 bps lower for securitized mortgages. Similarly, term extensions and payment cuts are smaller and principal increases are larger for privately securitized mortgages.

Finally, I compare the effectiveness of securitized and portfolio modifications by analyzing the probability of redefault (return to 60+ day delinquency) in the twelve months following modifications that cured delinquencies. Table 1.10 reports the results. In column

Table 1.9: Modification Details (Full Sample)

All regressions are conditional on loans being modified. The dependent variables in Panel A are indicators for interest rate modification, term modification, principal decrease, and principal increase. Panel A regressions estimate linear probability models for these indicators. The dependent variables in Panel B are net changes to interest rates, term lengths, principal balances, and monthly payments. Private securitization status six months after origination is instrumented with origination-month indicators. All observable loan characteristics shown in Table 3 are included as unreported controls. The regressions analyze jumbo loans that became seriously delinquent before 2012 and are modified within six months of becoming seriously delinquent. The net change (Panel B) regressions exclude observations with extreme changes (rate changes over 10 ppt, term changes over 20 years, principal changes over 50%, and payment changes over 75%). R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

<i>A. Type of modification</i>				
	(1) IV	(2) IV	(3) IV	(4) IV
	Interest Modification	Term Modification	Principal Decrease	Principal Increase
Mean	0.343	0.375	0.058	0.509
Private Security	0.058** (0.023)	-0.427*** (0.030)	-0.021 (0.020)	0.448*** (0.039)
Loan Characteristic Controls	Yes	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes	Yes
Origination Month FE	No	No	No	No
MSA FE	Yes	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No	No
Observations	3,378	3,378	3,378	3,378
Adjusted R-Squared	0.642	0.322	0.021	0.244
<i>B. Net changes</i>				
	(1) IV	(2) IV	(3) IV	(4) IV
	Interest Change (ppt)	Term Change (mos.)	Principal Change (%)	Payment Change (%)
Mean	-2.792	25.733	0.259	-27.302
Privately Securitized	0.385** (0.161)	-68.693*** (5.555)	1.573** (0.717)	4.034** (2.047)
Loan Characteristic Controls	Yes	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes	Yes
Origination Month FE	No	No	No	No
MSA FE	Yes	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No	No
Observations	3,377	3,052	3,361	3,205
Adjusted R-Squared	0.240	0.334	0.028	0.205

Table 1.10: Modification Effectiveness (Full Sample)

All regressions are conditional on a loan being cured of initial delinquency with a loan modification. The dependent variable is an indicator for redefault, defined as a return to 60+ day delinquent status within one year of modification. The regressions estimate linear probability models using origination month indicators as instruments for private securitization status six months after origination. Indicators for modification type are included where indicated. All observable loan characteristics shown in Table 3 are included as unreported controls. The regressions analyze jumbo loans that were cured through modification before 2012 within six months of becoming seriously delinquent. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) IV	(2) IV
	Redefault	Redefault
Mean	0.302	0.302
Privately Securitized	0.076** (0.034)	0.042 (0.045)
Interest Decrease		-0.094*** (0.027)
Term Increase		-0.046 (0.031)
Principal Decrease		-0.096*** (0.032)
Principal Increase		0.048* (0.029)
Loan Characteristic Controls	Yes	Yes
Delinquency Month FE	Yes	Yes
Origination Month FE	No	No
MSA FE	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No
Observations	3,058	3,058
Adjusted R-Squared	0.199	0.210

(1), I estimate an IV regression of redefault on private securitization and standard controls in the full sample of jumbo loans. Redefault is 7.6 ppt higher for privately securitized loans (compared to a mean redefault rate of 30%). The difference is partially explained by the types of modifications employed. Column (2) includes controls for modification type. This decreases the private securitization coefficient to (a statistically insignificant) 4.2 ppt. Interest and principal decreases are associated with lower redefault rates. Principal increases are associated with higher redefault rates.²⁹

1.5 Mechanism

The preceding section established that privately securitized loans are foreclosed more and modified less than comparable portfolio loans. Why do servicers treat securitized loans and portfolio loans differently?

Servicing securitized mortgages is a classic principal-agent problem. Securitized mortgages are owned by trusts that are explicitly passive (in part for tax reasons) and managed by third party servicers. Servicing current mortgages is relatively straight-forward. Servicers bill mortgagors, collect and forward payments, and maintain records. These functions can be readily standardized and specified in servicing contracts. By contrast, servicing delinquent loans is highly discretionary. Collection, modification, and foreclosure involve unobservable actions and loan-specific decisions that are difficult to specify in advance.

As in other principal-agent settings, servicing practices can deviate from investor interests either because of contract rigidity or because servicer incentives differ from investor incentives. The most obvious case of contract rigidity is explicit prohibitions of certain practices, particularly modification. These restrictions are meant to protect investors but may end up hurting them in some situations. Incentive differences are primarily manifested in an incentive for servicers to underinvest in practices that could enhance a mortgage's value but would be costly to the servicer. Servicers may also have an incentive to not deviate

²⁹These results are qualitatively similar to Agarwal, et al.'s (2011) OLS estimate that redefault is 3.5% higher for securitized modifications relative to portfolio modifications.

from default practices. For example, if foreclosure is the default practice for delinquent loans, servicers may perceive that alternatives invite investor scrutiny and liability risk. In some principal-agent settings, deviations from the principal's preferred actions can be corrected with ex-post renegotiation. This is all but impossible for MBS because dispersed investors lack the ability and incentive to monitor servicers.³⁰ Amending servicing contracts is also a difficult process, requiring super-majorities of certificateholders.

Previous discussions have focused mainly on securitization impeding mortgage modification, often with an emphasis on contractual modification restrictions, and this spilling over into increased foreclosure rates. This is an incomplete view of how securitization impacts delinquent mortgage servicing. Binding contractual restrictions on modifications are rare, and spillovers from decreased modifications are only part of the bias of securitized loans towards foreclosure. We have already seen one piece of evidence to this effect. Securitization has a larger impact on foreclosure (8.0 ppt for foreclosure initiation and 4.7 ppt for foreclosure completion) than on modification (-3.6 ppt). If the foreclosure bias was solely a spillover from modification frictions, it should be smaller than the modification bias.

To better understand how securitization affects mortgage servicing, I examine the contractual terms of actual servicing agreements and link these terms to loan-level panel data on modifications and foreclosures. I find that reimbursement policies universally incentivize foreclosure over modification and other effort-intensive loss mitigation practices. In contrast, binding modification restrictions are rare and have only moderate impact on modification rates.

1.5.1 Servicing Practices

Before focussing on frictions associated with servicing securitized loans, it is important to understand the options available to servicers when dealing with delinquent loans. Foreclosure and modification are not binary responses to delinquency. Servicers also have a wide

³⁰MBS trusts have trustees that theoretically represent the interests of certificateholders, but the actual power and responsibility of trustees are limited, and servicers can only be removed in exceptional situations. Moreover, a trustee is just another agent for the underlying investors with its own conflicts of interest.

range of notification, collection, relief, and loss mitigation options. Securitization has the potential to bias whether and how all of these options are used.

Fannie Mae's 2006 Servicing Guide offers a window into the breadth of delinquency management practices available to servicers. Notification options include late payment notices, payment reminder notices, reminder phone calls, letters (preferably individually-written as opposed to form letters), and face-to-face interviews. If communication alone does not suffice, Fannie Mae has procedures for debt collection by attorneys, acceptance or rejection of partial payments, referral to counseling agencies, and direct delinquency counseling. In parallel with these efforts, servicers are to communicate with junior lienholders. If a temporary hardship is identified, servicers may offer special relief in the form of a 30-day grace period, longer forbearance agreement, or repayment plan to pay past-due balances over time on top of regular monthly payments. With Fannie Mae approval, servicers can also negotiate more formal "Loss Mitigation Alternatives," including loan modifications, short sales, deeds-in-lieu of foreclosure, assumptions of mortgages by new homebuyers, and assignment of mortgages to mortgage insurers.

Choosing among these options requires significant servicer discretion. Optimal practices depend on loan-specific soft information that is difficult to document and essentially impossible to contract on ex-ante. Moreover, most delinquency management practices involve personal interaction with borrowers, which makes them costly and dependent on unobservable effort. Modification is particularly challenging because it requires servicers to negotiate new mortgage terms, which have the potential to harm investors.

Levitin and Twomey (2011) contrast foreclosure with other delinquency management tools. Foreclosure is unique in that once undertaken it involves little discretion and can be largely outsourced and automated. For example, Levitin and Twomey describe a widely used software platform that automatically refers mortgages to approved local attorneys once certain delinquency benchmarks (e.g., 60 days past due) are reached. The software uploads required documents for the attorneys and generates specific instructions and timelines without any human contact.

All servicers face a decision as to how much they should automate delinquent loan servicing. At one extreme, decisions can be highly formulaic and push most delinquent borrowers into foreclosure. At the other extreme, servicing can be hands-on with significant personal interaction and solutions tailored to specific borrower circumstances. The basic trade-off is servicing cost versus higher recovery rates. Levitin and Twomey (2011), argue that faced with this tradeoff most servicers chose the scale efficiencies of heavy automation. They further argue that the tradeoff between automation and hands-on discretion changed as delinquency rates climbed in 2007 and 2008 but that servicers were ill-equipped to quickly ramp up non-foreclosure delinquency management capabilities.

Securitization introduces three additional elements into this tradeoff. First, because it involves less discretion, soft information, and unobservable effort, automation mitigates principal-agent conflicts. Second, because it is cheaper, securitized servicers will naturally choose automation. Overcoming the bias towards automation requires costly interventions such as incentive payments or contractual restrictions of servicer actions. These elements both make automation more ex-ante efficient for securitized servicing relative to portfolio servicing. The final element is that servicing agreements are locked in when a deal closes and are difficult, if not impossible, to alter in response to changing market conditions. Thus, automation is sticky for securitized servicing even if market conditions change to favor more hands-on discretion.

1.5.2 Servicing Agreements

Securitized mortgage servicing is governed by servicing agreements, which are incorporated into more general pooling and servicing agreements (PSAs). To understand how these agreements operate, I analyze the terms of actual PSAs. My sample consists of all prime MBS deals between January and August of 2007 that exceeded \$1B. 37 deals meet this criteria, which collectively represent \$70B, 48% of total prime MBS issuance during this

period.³¹ For deals that involve multiple servicing agreements, I describe the agreement that is relevant to the most loans. The sample covers nine deal sponsors and seven servicers.

The PSAs give servicers broad authority for managing loans coupled with responsibility to follow accepted industry practices. Servicers bear most costs of servicing the loans and are compensated with a servicing fee, which is typically around 25 bps annualized for prime mortgages. Servicing fees are payable from loan proceeds and (in case of default) from the trust more generally so they function as a senior interest only strip for the life of a loan. Servicers also retain late fees and other ancillary fee income. Servicers generally have discretion to pursue modifications and other loss mitigation alternatives, but they have little direct incentive to do so because these tools require unreimbursable expenses and may involve waiving fee income. By contrast, foreclosure expenses are fully reimbursed. As long as they comply with accepted industry practices, servicers have an incentive to shade their delinquency management practices away from modification and loss mitigation and toward foreclosure. This incentive is compounded by the fact that foreclosure is universally specified as a default practice for delinquent loans, which may make it less risky for servicers from an investor liability point of view. Some PSAs contractually prohibit certain modifications, but these restrictions are relatively uncommon.

Table 1.11 summarizes the incidence of specific PSA terms. Sample PSAs universally require servicers to follow accepted servicing practices, generally defined as the practices of other responsible mortgage lenders. One source of these practices is Fannie Mae servicing guidelines, which are explicitly incorporated into 38% of PSAs. 68% of PSAs also require that loans be serviced equivalently to portfolio loans, and in one case the PSA explicitly requires that servicing be in the best interest of certificateholders. In other PSAs this is implicit in general and sometimes an explicit standard for specific servicing decisions.

The PSAs also universally establish a default responsibility to foreclose on sufficiently

³¹Data on MBS issuance volumes comes from Inside Mortgage Finance. Classifications of individual MBS deals come from Inside Mortgage Finance and review of prospectuses and rating agency reports for individual deals. In addition to the 37 deals in my sample, Inside Mortgage Finance identifies another 10 deals as prime that are described as Alt-A by the ratings agencies.

Table 1.11: Summary of PSA Terms

The sample consists of all prime non-agency MBS deals in excess of \$1B closed between January and August of 2007. 37 MBS deals with a total of value of \$70B meet this criteria. These deals represent 48% of total January - August 2007 prime non-agency MBS volume. For deals with multiple pooling and servicing agreements (PSAs) (e.g., deals involving multiple originators or servicers), the sample includes the agreements relevant to the most loans. The sample includes nine sponsors and seven servicers.

	Number of PSAs	Percent of PSAs
Representations and Warranties:		
Early payment default warranty	0	0%
Loan schedule is accurate	37	100%
Loans are current	31	84%
Loans had only limited past delinquency	22	59%
Servicing:		
General servicing responsibilities:		
Accepted industry practices	37	100%
Equivalent to portfolio loans	25	68%
Best interest of certificateholders	1	3%
Fannie Mae Servicing Guide	14	38%
Obligation to foreclose	37	100%
Foreclosure reimbursement	37	100%
Obligation to modify	0	0%
Obligation to consider modification	7	19%
Modification reimbursement:		
From trust	0	0%
From mortgagor	8	22%
Payment advances:		
Must advance delinquent monthly payments	37	100%
If principal or interest deferred, must advance difference	22	59%
Modification restrictions:		
Must be in default or default is foreseeable	23	62%
Must expect modification value to exceed foreclosure proceeds	8	22%
May not permanently decrease principal or interest rate	8	22%
May not extend term beyond term of certificates	1	3%
May not extend term beyond maturity of last-maturing loan	4	11%
Amendment:		
Without consent:		
Cure/correct terms	37	100%
Alter without adversely affecting certificateholders	12	32%
Required consent for other changes:		
Overall majority consent	37	100%
Overall supermajority (over 66%) consent	10	27%
Majority or supermajority consent in all affected classes	26	70%
Prohibition on decreasing or delaying payments without universal consent	37	100%

delinquent loans and provide reimbursement for foreclosure expenses. PSAs allow foreclosure to be postponed or avoided altogether if it is not in the best interest of certificateholders (for example if modification is more valuable or if hazardous materials make foreclosure more expensive than the property's value), but these are always exceptions to the general rule of foreclosure.

By contrast, modification and other loss mitigation practices are never explicitly required and are not reimbursed through regular loan payments or by the trust. Instead, servicers "may" pursue these alternatives and modify loans under certain conditions. The closest the PSAs come to requiring modification is a term in seven deals that requires the servicer to "consider" alternatives to foreclosure. In lieu of reimbursement from the trust, servicers are allowed to charge borrowers a modification fee. This is explicit in 22% of PSAs and implicit in the other PSAs by virtue of Fannie Mae's 2006 servicing guide allowing servicers to charge borrowers a \$500 modification fee and some modification-related expenses. 59% of PSAs also disincentivize modification by requiring servicers to advance deferred or forgiven principal and interest payments for any modification that alters mortgage payments. These advances will eventually be reimbursed out of the loan's future proceeds or from the trust more generally, but in the mean time they constitute interest-free loans from the servicer to the trust.³²

Of all the terms summarized in Table 1.11, modification restrictions vary the most and are of most interest. Some of these terms appear to be innocuous. 62% of PSAs explicitly prohibit principal, interest, or term modifications unless a mortgage is in default or default is foreseeable. This restriction is unlikely to bind (it certainly does not bind for the seriously delinquent loans I analyze) and is probably implicit in accepted servicing practices even where it is not explicitly included. 22% of PSAs require the expected value of modified loans to exceed the expected value of foreclosure proceeds. This is also unlikely to bind and is implied by accepted industry practices.

³²Servicers similarly advance scheduled principal and interest payments while a loan is in default until the advances are deemed uncollectable.

Binding modification restrictions come in the form of limitations on principal forgiveness, interest reductions, and term extensions. 22% of PSAs prohibit modifications that decrease principal balances or permanently decrease interest rates. 14% of PSAs prohibit modifications that increase loan maturity beyond the maturity of other loans in the trust or the maturity of the trusts' certificates. Because loans in a deal almost always have similar maturities (typically 30 years), this effectively prohibits term extensions. Importantly, these restrictions are uncommon compared to the universal incentive differences described above, and they still permit many kinds of modifications. For example, temporary interest rate reductions and principal forbearance are permitted under all PSAs.

Finally, amendment is difficult under all of the PSAs. General amendments require at least a majority approval of certificateholders, and in all but one PSA they require either a supermajority of certificateholders or a majority vote within each class of affected certificateholders.³³ Moreover, all PSAs expressly outlaw any amendment that would decrease or delay payments without the universal consent of all certificateholders. Any amendment inducing modification or other loss mitigation activity over foreclosure would presumably trigger this prohibition. If a PSA is substantively modified, this would necessitate an 8-K filing with the SEC. I observed no such filing for any of the 37 deals I investigated.

This is the largest survey of PSA terms that I am aware of and the only one that focuses on prime MBS. It also describes a wider range of PSA terms than any previous study. Three other studies survey subprime PSAs with consistent results. Hunt (2009) surveyed 20 subprime deals in 2006 and found that 67% limit modifications to loans in default or where default is foreseeable or imminent and 10% prohibit modifications altogether. Credit Suisse (2007) surveyed 31 deals between 2004 and 2007 and found that nearly all PSAs permit modification of loans in default or where default is reasonably foreseeable and 60% had no other modification restrictions. A Bear Stearns study described by Bajaj (2007) and Hunt (2009) surveyed approximately 20 deals and found that 10% of deals prohibit modifications

³³ Amendments to cure or correct ambiguities and conflicts are allowed without shareholder consent, and some PSAs (32%) allow more general amendments without consent if they don't adversely impact certificateholders.

and another 40% of deals require ratings agency approval if more than 5% of a loan pool is changed.

1.5.3 PSA Term Regressions

To assess how modification restrictions affect servicer behavior, I link PSAs to individual loans in Core Logic panel data.³⁴ For comparability to my earlier analysis, I limit the dataset to jumbo loans and impose the restrictions described in Section 3.³⁵ As described in Table 1.12, the linked dataset includes 85,000 loans with an aggregate origination value of \$60B. The loans are similar to the jumbo loans analyzed in Section 4 but are slightly larger (\$708K on average compared to \$691K) and have slightly higher FICOs (742 compared to 733) and lower LTVs (0.71 compared to 0.73). The linked sample also defaults less than the earlier sample (1% became seriously days delinquent within 1 year and 21% became seriously days delinquent within five years compared to 6% and 36%). These differences likely stem from the linked sample being entirely from prime MBS whereas my earlier sample included all jumbo mortgages with FICOs above 620. My analysis focuses on 18,000 loans that became seriously delinquent between 2007 and 2011. Foreclosure initiation (51.7% within six months), foreclosure completion (6.7% within six months) and modification (6.3% within six months) rates are similar to the previous full jumbo sample. Foreclosure and modification are defined and identified as before with one significant difference. I cannot identify term extensions in the Core Logic data. Thus, term modifications are missing from the PSA-linked data.

Having linked PSAs to individual delinquencies, I regress foreclosure and modification probability on indicators for PSA terms. Specifically, I regress foreclosure initiation, foreclosure completion, and modification within six months of first serious delinquency on

³⁴Core Logic mortgage data is similar to the LPS data used for my previous analysis but is limited to privately securitized mortgages. Unlike LPS, Core Logic contains identifiers for servicers, originators, and deals, which allows me to link loans to PSAs.

³⁵The only changes are that I no longer require loans to enter the dataset within four months of origination and I do not require loans to be originated in 2007. Survivor bias is not an issue in the Core Logic data because all loans enter the dataset when a deal closes.

Table 1.12: PSA-Linked Loan Sample

Data comes from Core Logic loan data linked to my sample of PSAs from prime non-agency MBS deals closed between January and August of 2007. The sample consists of jumbo (over \$417K) first-lien conventional loans that have origination FICO scores between 620 and 850, have origination loan-to-value ratios of less than 1.5, have terms of 15, 20, or 30 years, and are located in U.S. MSAs outside of Alaska and Hawaii. The delinquent loan sample includes loans that became seriously (60+ days) delinquent between 2007 and 2011. Delinquency is 60+ day delinquency. Foreclosure initiation is the referral of a mortgage to an attorney to initiate foreclosure proceedings. Foreclosure completion is identified by post-sale foreclosure or REO status. Modifications are identified based on observed changes to loan terms.

	All Loans	Delinquent Loans
Number	85,036	18,049
Size (mean)	\$707,542	\$671,927
FICO (mean)	742	722
LTV (mean)	0.71	0.75
Ownership		
Private Security	100%	100%
Delinquency		
Within 1 year	1.1%	
Within 5 years	20.9%	
Foreclosure Initiation		
Within 6 months		51.7%
Within 1 year		60.6%
Foreclosure Completion		
Within 6 months		6.7%
Within 1 year		20.6%
Modification		
Within 6 months		6.3%
<i>interest decrease</i>		5.4%
<i>term extension</i>		
<i>principal decrease</i>		0.0%
<i>principal increase</i>		2.5%
Within 1 year		13.3%

indicators for prohibitions of (1) permanent principal and interest reductions and (2) term extensions beyond the term of the MBS certificates or other mortgages. As discussed earlier, these terms vary across PSAs. To the extent that they bind, we should expect them to reduce modifications and potentially increase foreclosures. The regressions are OLS and include the same control variables as previous regressions plus servicer fixed effects. The servicer fixed effects are important because PSA terms vary across servicers and previous studies (e.g., Agarwal, et al. (2011) and Agarwal, et al. (2012a)) have demonstrated that servicers employ different modification and foreclosure practices. One caveat is that within-servicer term

Table 1.13: PSA Term Regressions

The dependent variables are indicators for foreclosure initiation, foreclosure completion, and modification within six months of first serious (60+ days) delinquency. All regressions are OLS. The reported independent variables are indicators for the presence of servicing contract terms. All observable loan characteristics shown in Table 3 are included as unreported controls. The regressions also control for MSA, origination month, delinquency month, and servicer fixed effects. The regressions analyze sample jumbo loans that became seriously (60+ days) delinquent between 2007 and 2011. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) OLS	(2) OLS	(3) OLS
	Foreclose Start	Foreclose	Modify
Mean	0.517	0.067	0.063
Permanent Principal and Interest Reductions Prohibited	0.137*** (0.025)	0.075*** (0.013)	0.001 (0.011)
Term Extensions Limited	0.110*** (0.028)	0.039*** (0.013)	-0.020* (0.010)
Loan Characteristic Controls	Yes	Yes	Yes
Servicer FE	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes
Origination Month FE	Yes	Yes	Yes
MSA FE	Yes	Yes	Yes
Observations	18,049	18,049	18,049
Adjusted R-Squared	0.138	0.049	0.034

variation is limited to two servicers. Servicer A has prohibitions of permanent principal and interest reductions in the seven deals it sponsors but not in the three deals it services for other sponsors. Servicer B has prohibitions on term extensions in the four deals it sponsors but not in the three deals it services for other sponsors.

Table 1.13 reports the results. Prohibitions on permanent principal and interest reductions are associated with increased foreclosure (13.7 ppt for foreclosure initiation and 7.5 ppt for foreclosure completion) and no change in modification. Prohibitions on term extensions are associated with increased foreclosure (11.0 ppt for foreclosure initiation and 3.9 ppt for foreclosure completion) and slightly decreased modification (-2.0 ppt, significant at the 10% level). Because I am unable to identify modifications that solely extend mortgage terms, this likely underestimates the full impact of term extension prohibitions on modifications.

These results are directionally what we should expect. Modification restrictions decrease modifications and increase foreclosures. However the magnitudes, particularly for modification, are too small to explain the overall bias of securitized loans toward foreclosure and away from modification. For example, the -2.0 ppt modification bias applied to the approximately 14% of securitized loans with this term only explains -0.3 ppt of the -3.6 ppt baseline modification bias for securitized loans. Similarly, the foreclosure coefficient estimates, combined with the incidence of these terms explain 56% of the foreclosure start bias and 46% of the foreclosure completion bias.

1.6 Conclusion

This paper's contribution is threefold. First, I propose a novel instrument for jumbo securitization and provide the first well-identified assessment of securitization's impact on foreclosure and modification rates. Private securitization increases foreclosure probability (by 8.0 ppt for foreclosure initiation and 4.7 ppt for foreclosure completion) and decreases modification probability (by 3.6 ppt). Second, I estimate the effect of securitization on foreclosure and modification over time, including periods before and after government intervention. Securitization increased foreclosure probability and decreased modification probability throughout 2007 to 2011, even after implementation of the Home Affordable Modification Program (HAMP) in 2009. Third, I identify the mechanisms through which securitization effects foreclosure and modification, highlighting that incentive differences are more important than contractual prohibitions and that the foreclosure bias is more than just a spillover from modification frictions.

The bias of securitized loans towards foreclosure and away from modification helps to explain why foreclosure is so prevalent. Securitization increases the incidence of foreclosure completion within three years by 31%. Extrapolated to all privately securitized mortgages, this adds up to over 500,000 of the 4.4 million foreclosures experienced since the start of the financial crisis. Securitization does not explain all foreclosures, but many foreclosures would have been prevented if mortgages had been held directly on bank balance sheets

instead of being securitized.

The differential treatment of securitized and portfolio loans serves as an example of how ownership structure can affect how assets are managed. Despite contracts designed to protect MBS investors from differential servicing treatment, securitized loans were systematically foreclosed more and modified less. This is an important factor in the debate about the welfare implications of securitized lending both in the mortgage market and elsewhere. Previously, most assessments of mortgage securitization have focused on origination, comparing the benefit of increased funding availability with the cost of lower-quality underwriting. Sub-optimal servicing is another channel through which securitization can be harmful and should be considered for both regulatory reforms and improvements to private contracts.

Finally, a word about welfare. In a first-best world where all loans are optimally managed, a loan's ownership status should not affect foreclosure and modification decisions. Thus, my results reject the hypothesis that mortgage servicing is efficient. However, this does not mean that eliminating securitization (or correcting its biases) would make servicing perfectly efficient. Portfolio lending is also subject to principal-agent problems, and externalities (particularly for foreclosure) could drive a wedge between private and social welfare. Properly interpreted, my results show the effect of adding a layer of principal-agent conflict through securitization and highlight a mechanism that has increased foreclosure rates. This understanding is critical for achieving the policy goal of reducing foreclosures, but it does not pin down what the policy goal should be. The private and social costs and benefits of foreclosure and modification remain important topics for future research to address the broader welfare question.

Chapter 2

Disagreement and Liquidity

2.1 Introduction

Extensive trading of equities and other informationally sensitive securities is a puzzle. Standard asset pricing models have no role for trading, and models that consider trading typically predict that asymmetric information decreases trading and destroys liquidity, defined as the ability to trade an asset without significantly changing its price. Given the large potential for asymmetric information in stocks, corporate bonds, and stock options, it is counterintuitive that these securities are heavily traded in liquid markets. Holmstrom (2008) highlights this puzzle by comparing money (liquidity) markets to stock markets: "Markets for liquidity are very different than stock markets. In the stock market, uncertainty and adverse selection fears are present all the time, but this does not prevent the markets from functioning.... Differences in beliefs often alleviate adverse selection. Stock markets thrive on differences in beliefs. Markets for liquidity are killed by them."

Since Akerlof (1970), economists have recognized that asymmetric information has the potential to destroy trade. To overcome asymmetric information, at least some trade must be motivated by something other than rationally processed information, otherwise liquidity will dry up, markets will freeze, and the no-trade prediction of Milgrom and Stokey (1982) will prevail. Starting with the noisy rational expectations models of Grossman and Stiglitz

(1980), Hellwig (1980), and Diamond and Verrecchia (1981) and including virtually all research on liquidity and market microstructure (most notably Kyle, 1985), this extra trading has been modeled as exogenous noise.

Traditional asymmetric information models make two basic predictions: (1) Significant noise trading is necessary to generate trading and liquidity; and (2) asymmetric information decreases trading and liquidity. Hong and Stein (2007) address the first prediction, noting that trading volume in traditional models is approximately pinned down by noise (non-informational) trading volume. For example, in Kyle's (1985) model exogenous noise trading represents half of total order flow variance. In my moderate variance calibration of Diamond and Verrecchia's (1981) model, liquidity trading is 95% of total trading volume. The New York Stock Exchange has daily volumes in excess of \$30B. Liquidity trading of that magnitude seems implausible. One way out of this problem is to interpret noise trading more generally and claim that the vast majority of trading is uninformed noise from irrational traders. While theoretically possible, this is not particularly satisfying. If most trading is exogenously assumed, we aren't really left with a model of trading. Moreover, traditional models assume that noise trading is not just exogenous but also orthogonal to information. This is a critical assumption, and it is likely invalid if noise trading is driven by disagreement among market participants. For example, if disagreement comes from overconfidence in private information, the same trade is at once informative and noise, making noise trading perfectly correlated with information.

Prediction (2) presents even more fundamental problems. In contrast to traditional intuition, my empirical work shows that asymmetric information actually increases trading. I study asymmetric information, turnover, and liquidity of stocks, corporate bonds, and stock options.¹ My analysis establishes three stylized facts: (1) Trade and liquidity are positively correlated; (2) asymmetric information increases trade and decreases liquidity;

¹I proxy for asymmetric information with analyst earnings forecast dispersion and also study periods around earnings announcements, which likely have elevated asymmetric information. For illiquidity, I use several measures of bid-ask spreads as well as Amihud's (2002) $illiq = \frac{|Return|}{\$Volume}$ measure.

and (3) high past returns increase trade and liquidity.² Fact (1) supports the notion that trade and liquidity reinforce one another. Fact (2) contradicts the prediction of traditional models that asymmetric information destroys trading. Fact (3) shows that traditional models leave out something related to past returns.

To resolve the failures of traditional models, I propose that trading is primarily driven by disagreement. I.e., people trade because they have different beliefs about an asset's value. Counterparties essentially make zero-sum bets about asset values, and they do so fully aware that other parties disagree with them. Disagreement trading has become an increasingly popular explanation of trading volumes (Hong and Stein, 2007, summarize this view), but there is little existing research on the relationship between disagreement and liquidity and virtually none on how disagreement changes asymmetric information's impact on trading and liquidity.

In my model of disagreement trading, belief differences stem from overconfident interpretation of private information. The overconfidence bias creates trade and liquidity even when prices fully reveal the beliefs of other agents. Moreover, because disagreement stems from private signals, trading and liquidity can increase with asymmetric information. Formally, I model disagreement trading among *ex ante* homogenous agents who simultaneously serve as informed traders, noise traders, and market makers. Agents are risk averse, receive endowments of a risky asset, observe private signals about the asset's value, and trade the asset with one another in an anonymous public market in which market price is visible to all agents. Agents are fully rational except for an overconfidence bias, which causes them to overestimate the precision of their own signals. I consider two versions of the model, a baseline model in which asset endowments are constant and a general model in which asset endowments are stochastic. The baseline model is an adaptation of Grossman

²In equity markets, these facts have been partially shown or hinted at before. In particular, Sadka and Scherbina (2007) show that analyst forecast dispersion (one proxy for asymmetric information) decreases liquidity; Frazzini and Lamont (2007) show that turnover is elevated around earnings announcements (another proxy for asymmetric information); and Statman, Thorley, and Vorkink (2006) show that trading increases following high returns. I extend these findings to corporate bonds and stock options and show for the first time that analyst dispersion increases trading, earnings announcements decrease liquidity, and past returns increase liquidity.

(1976) with overconfidence. The general model is an adaptation of Diamond and Verrecchia (1981) with overconfidence.

The baseline model describes an environment in which trading is entirely driven by disagreement. Because supply is certain and there is no non-informational motive for trade, prices fully reveal aggregate information (as in Grossman, 1976). Nonetheless, overconfidence induces agents to disagree and trade, thereby generating liquidity (in contrast to Grossman, 1976). The model's main predictions are: (1) Overconfidence increases trading and liquidity; (2) Private information increases trading and liquidity; and (3) Public uncertainty decreases liquidity without affecting trading volume.

The prediction that private information increases trade and liquidity conflicts with traditional intuition. To understand this contrast, I consider a general model that adds non-informational liquidity trading, modeled through stochastic endowments, to the baseline model. When some trading is uninformed, increasing private information can destroy liquidity by increasing the share of informed trade relative to uninformed trade. Private information increases a trade's price impact by increasing the probability that the trade is informed. In the baseline model, all trade is informed so this channel is inoperative. More generally, the probability that a trade is informed is insensitive to the level of private information whenever uninformed trade is very large or very small relative to informed trade. In these settings, traditional intuition fails, and private information increases liquidity as in the baseline model.

My model explains trade and liquidity in the face of asymmetric information and conforms to the stylized facts described above. It also generates the additional testable prediction that stocks with the highest turnover response to asymmetric information should have the smallest illiquidity response to asymmetric information.³ I test this prediction and

³Asymmetric information consists of both private information and public uncertainty. In the baseline model private information increases trading, whereas public uncertainty has no impact on it. Thus, asymmetric information changes with a larger trading impact are more likely to be driven by changes to private information. Private information enhances liquidity, whereas public uncertainty reduces it. Thus, asymmetric information should have the least negative impact on liquidity (and may even enhance it) when it has the most impact on trading.

find that it is true in the data.

In the next section, I review related literature. Section 3 presents empirical analysis supporting the stylized facts introduced above. Section 4 introduces, solves, and derives comparative statics for the baseline model. Section 5 presents the general model, including comparative statics and numerical examples of how overconfidence and asymmetric information affect trading and liquidity. Derivations and proofs for the general model are in an appendix. Section 6 discusses and tests the model's empirical predictions. Section 7 concludes.

2.2 Literature Review

2.2.1 Disagreement

Disagreement models posit that a combination of private information (or private interpretation of public information) and behavioral biases causes otherwise rational investors to disagree about asset values. Disagreement models are motivated by two failings of standard asset pricing models with homogenous beliefs. First, standard models (at least in their simplest forms) are at odds with well-established asset pricing anomalies like momentum (Jegadeesh and Titman, 1993), post-earnings drift (Bernard and Thomas, 1989), and long-term return reversion (Fama and French, 1992; Lakonishok, Shleifer, and Vishny, 1994). Second, standard models have no role for trading and thus cannot explain the high turnover observed in many financial markets. Disagreement is an intuitively appealing rationale for trade and, depending on what drives the disagreement, also has the potential to explain pricing anomalies.

Hong and Stein (2007) provide a nice summary and taxonomy of disagreement models. The first ingredient for these models is some manner of private information. One possibility is that private information comes from gradual information flow as in the gradual dissemination of information to newswatchers over time in Hong and Stein (1999). Another possibility is that investors have limited attention and thus process only a subset of available

information, possibly for entirely rational reasons related to the cost of attention (e.g., Peng and Xiong, 2006). A final possibility is that investors see the same information but interpret it differently, possibly due to heterogeneous priors (e.g., Harris and Raviv, 1993; Kandel and Pearson, 1995). Regardless of its source, the end result is equivalent to investors having access private information.

The second ingredient for disagreement models is a behavioral bias in information processing. Private information alone does not generate disagreement in standard models. Instead, market prices aggregate and fully reveal information (Grossman, 1976), which causes investors to agree about asset values and eliminates motives for trade (Milgrom and Stokey, 1982). Introducing random asset supply or exogenous liquidity trading (e.g., Hellwig, 1980; Grossman and Stiglitz, 1980; Diamond and Verrecchia, 1981; Kyle, 1985) mitigates information revelation and creates some disagreement, but trading is still largely pinned down by assumptions about exogenous trading. For example, in Kyle's (1985) model exogenous noise trading represents half of total order flow variance. In my moderate variance calibration of Diamond and Verrecchia's (1981) model liquidity trading is 95% of total trading volume. To yield more significant disagreement trading, investors must value their own information more highly than information extracted from market prices. Overconfidence is a convenient modeling device for achieving this result and is supported by substantial psychological evidence (see Odean, 1998; Daniel, Hirshleifer, and Subrahmanyam, 1998; and DeBondt and Thaler, 1995, for good discussions of overconfidence). Overconfidence can be modeled in different ways The typical approach is to assume that investors overestimate the precision of their own signals relative to the signals of other investors.

Dynamic models of overconfidence posit that investors learn to be overconfident based on past experience. In particular, investors are subject to a self-attribution bias that causes them to overestimate how much their own skill was responsible for past successes. As a result, overconfidence is highest following positive returns. Daniel, Hirshleifer, and Subrahmanyam (1998) and Gervais and Odean (2001) model this phenomenon. Because investors hold the market in aggregate, self-attribution bias predicts that overconfidence

should be high following high market returns. Stock-level overconfidence should be high following high individual stock returns because owners of the stock just experienced high returns. Statman, Thorley, and Vorkink (2006) show that turnover is higher than normal following high market returns and high individual stock returns, consistent with high returns increasing overconfidence, which in turn increases trading intensity.

Casual intuition suggests that disagreement trading should enhance liquidity. However, liquidity has not been a major focus of the disagreement literature and is not explicitly discussed in most disagreement papers. Exceptions include Odean (1998), Kyle, Obizhaeva, and Wang (2013), and Baker and Stein (2004). Odean (1998) adds overconfidence to the Kyle (1985) model of liquidity. When the informed insider receives a noisy signal and overestimates the precision of that signal, the insider's overconfidence increases liquidity. Specifically, the market maker's price function becomes less sensitive to order flow as the insider becomes more overconfident. Though they don't explicitly focus on liquidity, the duopoly model of Kyle and Wang (1997) produces a similar result with two overconfident insiders. Kyle, Obizhaeva, and Wang (2013) show that overconfidence mitigates price impact and generates disagreement trading.⁴ Baker and Stein (2004) also model overconfidence as increasing liquidity. However, this relationship is an ad hoc assumption based on the logic that the same behavioral biases that cause investors to overestimate the precision of their own signals will also cause them to underestimate the informational content of market prices. None of these papers address how overconfident disagreement changes the impact of asymmetric information on trading and liquidity.

⁴Kyle, Obizhaeva, and Wang's (2013) model is the closest to my own. The main main difference between their single period model and my baseline model is that investors in the Kyle, Obizhaeva, and Wang model have market power whereas all agents in my model are price takers. Despite the modeling similarities, Kyle, Obizhaeva, and Wang address different questions than I do. Their focus is on how market power and overconfidence combine to give large investors an incentive to smooth trading whereas I analyze how overconfident disagreement changes the impact of asymmetric information on trading and liquidity.

2.2.2 Liquidity

The market microstructure literature aims to understand what causes illiquidity in financial markets. The backdrop is that in Walrasian equilibrium beliefs are independent from prices and market prices perfectly reflect the demands of all agents. In real financial markets investors learn from market prices, and prices can deviate from fundamental values creating costs to trading. Trading costs (illiquidity) come from two main sources. First, not all agents are active in markets at the same time. Thus, transactions must be facilitated by market makers. These market makers must cover whatever costs they incur by being constantly active in financial markets, and they must be compensated for the risk they take by holding long or short positions in an asset while searching for a counterparty. Market makers might also extract profits from strategic behavior. The second source of illiquidity is asymmetric information. Uninformed buyers may worry that they are being exploited by better-informed counterparties and thereby demand lower prices. Biais, Glosten, and Spatt (2005) survey the microstructure literature. Vayanos and Wang (2009) propose a unified model encompassing multiple sources of illiquidity.

My focus is on asymmetric information illiquidity because asymmetric information is intimately tied to disagreement. Other sources of illiquidity may also be important, but they are likely to be largely orthogonal to changes in disagreement. The classic models of asymmetric information liquidity are Kyle (1985) and Glosten and Milgrom (1985). In both models, market makers see order flow and are unsure whether the order flow comes from an informed insider or an uninformed liquidity trader. Market makers rationally infer some probability that order flow reflects information and adjust prices accordingly. Kyle (1985) describes this process in terms of the impact of order flow on price. Glosten and Milgrom (1985) highlight that asymmetric information naturally leads to bid-ask spreads. More recent microstructure research extends these frameworks to consider strategic behavior by market makers and market design issues. The microstructure liquidity literature generally does not model overconfidence. Odean (1998) and Kyle, Obizhaeva, and Wang (2013), discussed above, are notable exceptions.

The microstructure literature typically considers asymmetric information illiquidity in settings where market makers set prices and bid-ask spreads. However, market makers are not necessary for the concept of asymmetric information illiquidity. For example, one can think about illiquidity in the rational expectations framework of Grossman (1976). All agents receive private signals, observe market prices, and form trading demands. Grossman's conclusion is that prices fully reveal the average signal. As a result, there is no disagreement and no trading. In effect, markets are infinitely illiquid. Hellwig (1980); Diamond and Verrecchia (1981); and Grossman and Stiglitz (1980) introduce uncertain asset supply so that prices are no longer fully revealing. As a result, agents disagree about asset prices and trade with one another. Prices finitely react to order flow. None of these models explicitly considers liquidity, but asymmetric information illiquidity is just as present in them as in the market maker microstructure models.

2.3 Stylized Facts

I propose three stylized facts about stock, bond, and option markets:

1. Trade and liquidity are positively correlated;
2. Asymmetric information increases trade and decreases liquidity; and
3. High past returns increase trade and liquidity.

These facts are not entirely new, especially with respect to the stock market. For example, Sadka and Scherbina (2007) show that analyst forecast dispersion (one proxy for asymmetric information) decreases liquidity. Frazzini and Lamont (2007) show that turnover is elevated around earnings announcements (another proxy for asymmetric information). Statman, Thorley, and Vorkink (2006) show that trading increases following high returns. Hong and Stein (2007) also observe that returns and trading volume are correlated.

I extend these findings and show for the first time that analyst dispersion increases trading, earnings announcements decrease liquidity, and past returns increase liquidity. I

also show that the stylized facts are robust across stock, corporate bond, and option asset classes.

My sources for stock data are CRSP for return and volume data, Compustat for industry and earnings announcement data, I/B/E/S for analyst earnings forecast data, and TAQ for intraday trade and quote data. I limit my stock sample to New York Stock Exchange (NYSE) stocks with prices above \$5 at the end of the previous month. The sample starts in 1926, but most of my analysis is limited by analyst earnings forecast data, which starts in 1976, and bid-ask spread data, which starts in 1993 for my favored measure based on intraday TAQ data. I measure stock turnover as monthly volume divided by shares outstanding. My primary liquidity measure is the effective bid-ask spread (*ebidask*) of Chordia, Roll, and Subrahmanyam (2000), which I calculate at the transaction level as twice the difference between a trade's price and the midpoint of the prevailing quote before the trade. Because this measure is only available starting in 1993, I also use Amihud's (2002) $illiq_{it} = \frac{|Return_{it}|}{\$Volume_{it}}$ measure for some analyses.

Bond data comes from TRACE, supplemented by Mergent FISD bond characteristics. The TRACE data starts in 2002. I limit my sample to investment grade U.S. corporate bonds and medium term notes without asset backing or security enhancement features that are at least one year old and have at least one year of maturity left. I also require that a bond be actively traded (defined as having at least two buy trades and two sell trades) on at least 15 days during the previous month. I consider only transactions between dealers and their customers. Turnover is the total par value of all trades in a bond scaled by the bond's outstanding par value. Effective bid-ask spread (*ebidask*) is the difference between the weighted average prices of a day's buy and sell trades.⁵

Option data comes from Ivy DB OptionMetrics, available starting in 1996. My analysis is at the stock (as opposed to option) level. I define turnover as total option dollar volume

⁵The TRACE data I use is the enhanced dataset available on WRDS, which identifies whether a trade is with a customer or another dealer and which side of the transaction the reporting dealer was on. The enhanced dataset also includes all volume data instead of truncating large trades. This data became available only recently and appears to be an enhancement over data used in previous studies.

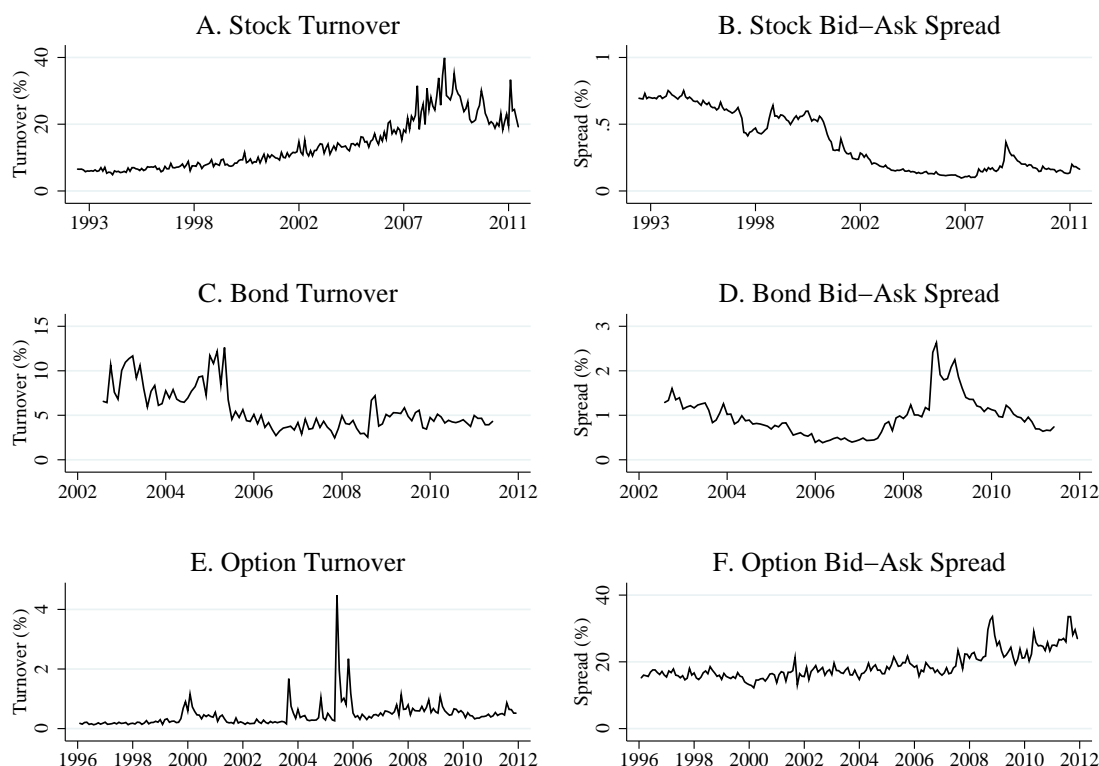


Figure 2.1: *Monthly Time Series*

Stock turnover is relative to stock market capitalization. Bond turnover is relative to outstanding bond value. Option turnover is option contract value relative to stock market capitalization. Bid-ask spreads are all proportional to the value of the security being traded. Stock and bond bid-ask spreads are intraday effective spreads. Option bid-ask spreads are end of day quoted spreads.

divided by stock market capitalization. Quoted end-of-day proportional bid-ask spreads are weighted by dollar volume when averaged to the stock level.

Figure 2.1 plots equally-weighted average monthly turnover and bid-ask spreads for stocks, bonds, and options. Stock turnover (panel A) averages 14% during the plotted 1993 to 2011 time period and reaches as high as 40% late in the sample. Stock effective bid-ask spreads (panel B) average 0.4% and decrease over the sample period. Corporate bonds also have significant trading activity and moderate bid-ask spreads. Bond turnover (panel C) is typically near the 5-10% range, and average bond effective bid-ask spreads (panel D) range from 0.5% to 2.5%. In contrast to stocks and bonds, dollar transaction volumes are relatively small for stock options. Average dollar option volume (panel E) is typically under

Table 2.1: Turnover Panel Regressions

Results are for stock- and bond-level regressions of log bid-ask spread measures on log turnover. Stock data is for NYSE stocks with lagged prices greater than \$5. Bond data is for actively traded U.S. corporate bonds without credit enhancements. Option data is for all traded stock options. Bid-ask spreads are proportional to security value. Stock and bond bid-ask spreads are intraday effective spreads. Option bid-ask spreads are end of day quoted spreads. Robust clustered (by firm) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	Stocks	Bonds	Options
	(1)	(2)	(3)
	Log Bid-Ask	Log Bid-Ask	Log Bid-Ask
Log Turnover	-0.134*** (0.006)	-0.090*** (0.011)	-0.174*** (0.004)
Stock/Bond FE	Yes	Yes	Yes
Year FE	Yes	Yes	Yes
Month FE	Yes	Yes	Yes
Date Range	1993-2011	2002-2011	1996-2011

1% of stock market capitalization. Average option bid-ask spreads hover around 20% of contract value. However, these figures are for option contract value as opposed to stock price exposure. In practice, options often deliver large stock price exposure with minimal up-front contract value.

2.3.1 Fact 1: Trade and Liquidity are Positively Correlated

Traditional reasoning predicts a strong positive relationship between trading and liquidity. The two quantities are mutually reinforcing. More noise trading improves liquidity, and enhanced liquidity attracts additional trading activity. Similar logic follows from my general disagreement model.

Positive correlation between trade and liquidity is clear in the stock, bond, and option data. As turnover increases, bid-ask spreads tend to decrease. Table 2.1 reports results for panel regressions of log bid-ask spreads on log turnover. The regressions include stock, bond, and time fixed effects. Because turnover and bid-ask spreads are both expressed as logs, the results can be interpreted as elasticities. The elasticity of stock bid-ask spreads with respect to turnover is -13%. The equivalent coefficients for bonds and options are -9%

and -17%, respectively. All three estimates are highly significant.

2.3.2 Fact 2: Asymmetric Information Increases Trade and Decreases Liquidity

While trading and liquidity are positively correlated, they do not always move in the same direction. In particular, asymmetric information tends to increase trading while reducing liquidity.

I identify changes in asymmetric information in two ways. First, periods around earnings announcements are likely to have elevated asymmetric information. Prior to announcements, private information can be in the form of leaks and insider trading. After announcements, investors process different pieces of information at different paces using different models, keeping private information high until the announcement is fully digested and reflected in prices. Public uncertainty is also high around earnings announcements because asset values are highly sensitive to the announcements. Second, I follow Sadka and Scherbina (2007) and use dispersion of analyst forecasts as a proxy for asymmetric information. Analyst dispersion may represent or cause public uncertainty. Dispersion could also stem from more private information. My specific measure of dispersion is the standard deviation across analysts of current year earnings forecasts scaled by the mean forecast. Firms are included if they are covered by at least two analysts, have a non-zero mean earnings forecast, and have a December fiscal year end. The December fiscal year requirement ensures that all stocks have the same amount of time remaining in the current fiscal year.

For my earnings announcement analysis, I scale turnover and bid-ask spreads by average values over the three calendar months prior to an earnings announcement and analyze scaled turnover and bid-ask spreads over a 21-day trading window around earnings announcements. Figure 2.2 plots equally weighted average scaled turnover and bid-ask spreads in event time around earnings announcements. Day 0 is the announcement day or first trading day after the announcement. Other days represent trading days relative to the announcement. 95% confidence intervals are plotted in dashed lines.

Panels A and B plot stock data. Consistent with Frazzini and Lamont (2007), turnover

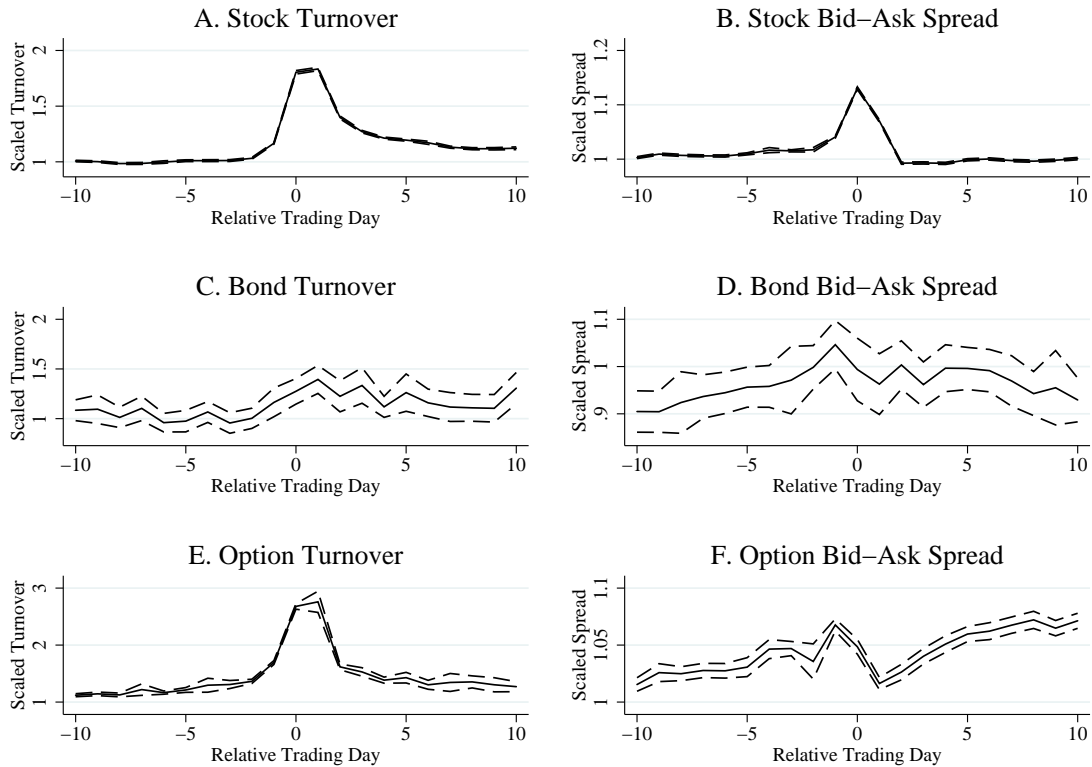


Figure 2.2: *Turnover and Liquidity Around Earnings Announcements*

Turnover and bid-ask spreads are scaled by average daily values over the three calendar months before the earnings announcement. Solid lines are equally weighted averages. Dashed lines are 95% confidence intervals. Day 0 is the day of the earnings announcement.

starts to increase the day before an announcement, spikes to 80% above normal levels on the announcement day, stays at that level for another day, and then decays. I extend the analysis of Frazzini and Lamont by also studying bid-ask spreads, which widen around earnings announcements. Bid-ask spreads peak at 13% above normal levels on the day of the announcement, and are also elevated the day before and after the announcement.

Though not always as pronounced, turnover and bid-ask spreads also tend to increase around earnings announcements for bonds and options. Panel C shows that bond turnover peaks at 40% above normal levels the day after an earnings announcement. Bond bid-ask spreads (panel D) are slightly elevated around earnings announcements, particularly the day before an announcement. Option volumes (panel E) surge to over 250% normal levels

Table 2.2: Analyst Dispersion Panel Regressions

Results are for stock- and bond-level regressions of log turnover and log bid-ask spread measures on lagged (by one month) log dispersion of analyst earnings forecasts. Data is limited to NYSE stocks with lagged prices greater than \$5, at least 2 analyst forecasts, and fiscal years that end in December. Bid-ask spreads are proportional to security value. Stock and bond bid-ask spreads are intraday effective spreads. Option bid-ask spreads are end of day quoted spreads. Robust clustered (by firm) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	Stocks		Bonds		Options	
	(1)	(2)	(3)	(4)	(5)	(6)
	Log Turnover	Log Bid-Ask	Log Turnover	Log Bid-Ask	Log Turnover	Log Bid-Ask
Lagged Log Analyst Dispersion	0.019*** (0.004)	0.109*** (0.004)	0.077*** (0.027)	0.079*** (0.020)	0.145*** (0.014)	0.036*** (0.005)
Stock/Bond FE	Yes	Yes	Yes	Yes	Yes	Yes
Year FE	Yes	Yes	Yes	Yes	Yes	Yes
Month FE	Yes	Yes	Yes	Yes	Yes	Yes
Date Range	1976-2011	1993-2011	2002-2011	2002-2011	1996-2011	1996-2011

around earnings announcements, and option bid-ask spreads (panel F) widen to 6% above normal levels, with a peak the day before the earnings announcement.

Analyst earnings forecast dispersion is a second proxy for asymmetric information. Sadka and Scherbina (2007) show that in sorts on analyst dispersion, high dispersion stocks tend to be less liquid. I employ panel regressions to control for firm and time fixed effects and add a test of the effect of analyst dispersion on trading volumes. I also extend the analysis to bonds and options. Table 2.2 presents my results. The analyzed variables are logs so coefficients can be interpreted as elasticities. For stocks, the turnover coefficient on lagged analyst dispersion (column 1) is 1.9% and the bid-ask spread coefficient on lagged analyst dispersion (column 2) is 10.9%. Bonds and options respond similarly to analyst dispersion. For bonds, the turnover coefficient (column 3) is 7.7%, and the bid-ask spread coefficient (column 4) is 7.9%. For options, the turnover coefficient (column 5) is 14.5%, and the bid-ask spread coefficient (column 6) is 3.6%. All coefficients are highly significant.

2.3.3 Fact 3: High Past Returns Increase Trade and Liquidity

Statman, Thorley, and Vorkink (2006) use a market VAR and individual stock-level VARs to show that market turnover increases following high market returns and individual stock turnover increases following both high market returns and high individual stock returns. I add illiquidity to Statman, Thorley, and Vorkink's market VAR methodology and apply it to stocks, bonds, and options. The market VAR model is:

$$Y_t = \alpha + \sum_{k=1}^2 A_k Y_{t-k} + e_t \quad (2.1)$$

where Y_t is a 3×1 vector of detrended log turnover, detrended log illiquidity, and excess market returns.⁶ Using two lags is optimal according to the Bayesian information criteria. In all cases, the market return variable is excess stock market returns. Thus, I am assessing the impact of stock market returns on future trading and liquidity in stocks, bonds, and options. For my baseline stock analysis, I use Amihud's *illiq* instead of bid-ask spread because it is available for the full sample instead of just after 1993. For bonds and options I use the same bid-ask spread measures as before.

Figure 2.3 plots impulse response functions for stock, bond, and option market VARs. The plots show how one standard deviation unexpected stock market return shocks affect future realizations of turnover and illiquidity measures.⁷ Consistent with Statman, Thorley, and Vorkink (2006), panel A shows that stock turnover responds positively to market returns. A one standard deviation return shock increases turnover in the next month by about 5%. Turnover increases slightly in the following month and then decays toward normal levels. Panel B shows that positive market returns also enhance liquidity. A one standard deviation return shock decreases *illiq* by 8% in the next month. Positive stock return shocks also

⁶Turnover and illiquidity measures are detrended using a Hodrick and Prescott (1997) filter. Following Statman, Thorley, and Vorkink (2006) and common practice, I use a penalty value of 14,400 for the filter. Also following Statman, Thorley, and Vorkink (2006), I employ a 2-sided filter. The 2-sided filter, which makes use of future data, would be problematic if I was using it for forecasting purposes, but I am not. To verify that my results are unaffected by the use of future data, I replicated my market VAR with a 1-sided HP filter proposed by Stock and Watson (1999). Results (which are untabulated but are available on request) were unchanged.

⁷Other impulse-response combinations are omitted for brevity.

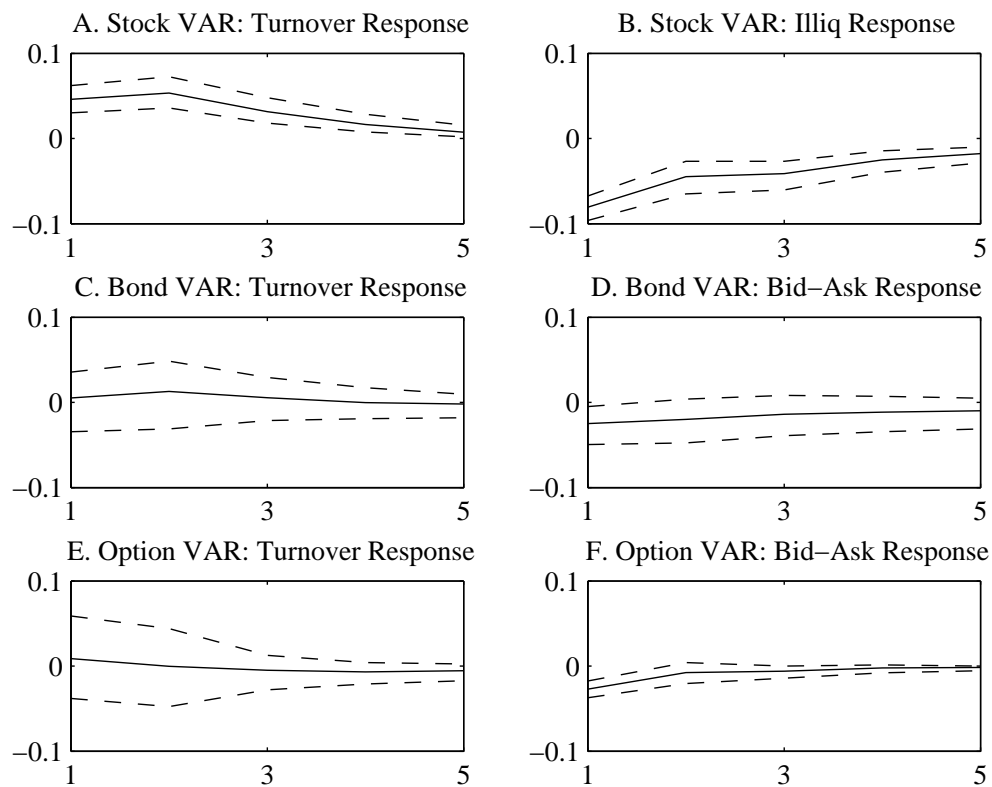


Figure 2.3: Market VAR Responses to Market Return Impulse

Each VAR includes detrended log market turnover ($turn$), CRSP value-weighted market returns in excess of the risk free rate ($rmrf$), and a detrended log measure of market illiquidity ($illiq$ for the stock VAR in the first row, effective bid-ask spread for the bond VAR in the second row, and quoted bid-ask spread for the option VAR in the third row). The solid lines are responses to one standard deviation shocks to $rmrf$ after the number of lags indicated on the horizontal axis. The dashed lines are 95% confidence intervals.

decrease bond and option bid-ask spreads (panels D and F). Bond and option volumes (panels C and E) do not significantly respond to past stock returns. The online appendix reports coefficients for the stock VAR.

In addition to being impacted by market returns, individual stock turnover and liquidity respond positively to past stock and industry level returns. Using separately estimated stock-level VARs, Statman, Thorley, and Vorkink (2006) show that stock turnover is positively influenced by both past market returns and past individual stock returns. I employ a different econometric strategy and estimate a single panel VAR that includes stock-level turnover, illiquidity, and returns as well as industry returns. The panel VAR specification allows me to employ stock and time fixed effects, eliminating the need for detrending the data. Specifically, I estimate:

$$Y_{i,t} = \alpha_t + f_i + \sum_{k=1}^2 A_k Y_{i,t-k} + e_t \quad (2.2)$$

where $Y_{i,t}$ is a 4×1 vector of log stock turnover, log stock *illiq*, stock returns, and industry returns for stock i in month t . α_t and f_i are 4×1 vectors of time and stock fixed effects for each variable. I employ two lags for consistency with the market model. The time fixed effects control for the effect of market returns as well as any other market-level time variation. Prior to estimation, I eliminate the time fixed affects by time de-meaning all variables. The panel fixed effects are a little trickier because stock demeaned lag variables are not orthogonal to the regression residual. Similarly, directly estimating stock fixed effects would produce biased and non-consistent estimates for all coefficients. Following Holtz-Eakin, Newey, and Rosen (1988), I take the first differences of all variables, resulting in:

$$Y_{i,t} - Y_{i,t-1} = (\alpha_t - \alpha_{t-1}) + \sum_{k=1}^2 A_k (Y_{i,t-k} - Y_{i,t-1-k}) + e_t \quad (2.3)$$

which can be estimated using using $Y_{i,t-2}$ and $Y_{i,t-3}$ as instruments. I include all observations with at least three lagged observations. When there are breaks in the data. I treat observations before and after the break as if they were separate stocks. The only remaining complication is estimating standard errors. The lagged variables directly control for auto-

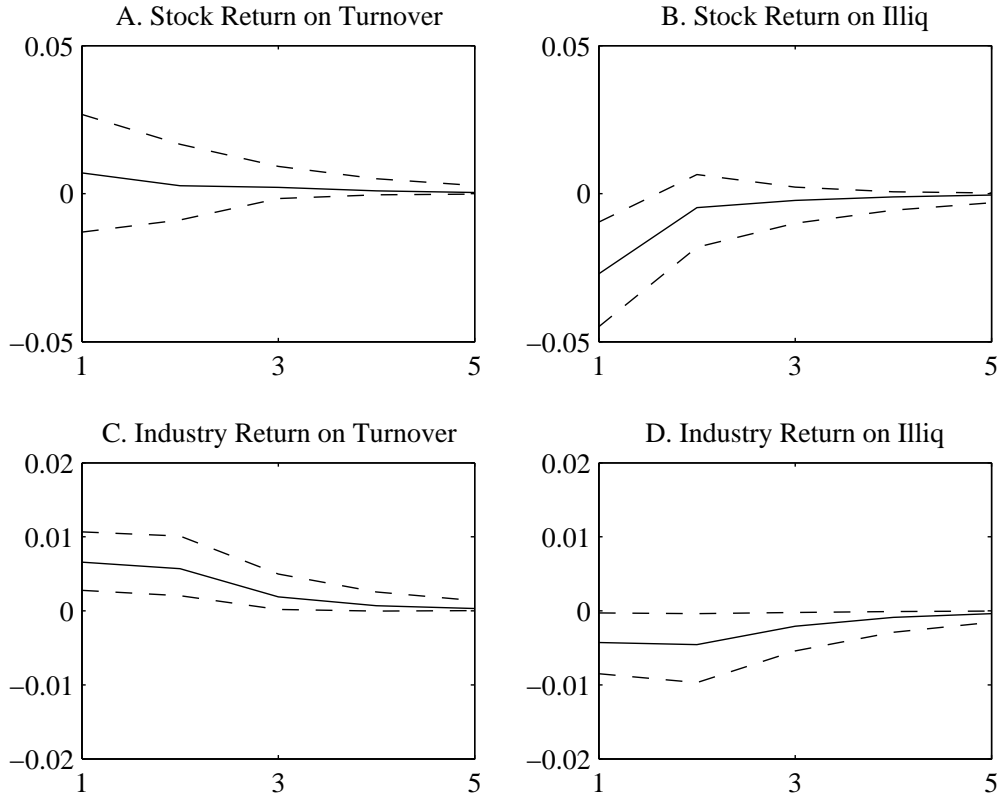


Figure 2.4: *Stock Panel VAR Impulse Response Functions*

The panel VAR includes stock log turnover, stock log *illiq* (an illiquidity measure), stock returns, industry returns, and stock and time fixed effects. The first variable in each panel title is the impulse variable. The second variable is the response variable. The solid lines are responses to one standard deviation shocks to the impulse variables after the number of lags indicated on the horizontal axis. The dashed lines are 95% confidence intervals. For brevity only the most relevant impulse response functions are shown.

correlation in the data, but there is likely cross-sectional correlation within time periods. To account for this I employ bootstrapped standard errors with a bootstrap that randomly samples (with replacement) time periods. When a time period is drawn, all observations in that time period are included. This preserves the data's cross-sectional correlation structure.

Figure 2.4 plots the most relevant impulse response functions of the panel VAR. As before, the impulse shocks are all one standard deviation. In panel A, turnover is unaffected by individual stock returns. In the other three panels, past returns forecast increased turnover and decreased illiquidity. A one standard deviation shock to an individual stock's return forecasts a future decline in *illiq* of 2.7% (panel B). A one standard deviation shock

to an industry's return forecasts a 0.7% increase in turnover (panel C) and a 0.4% decrease in *illiq* (panel D). Coefficient estimates are reported in the online appendix.

2.3.4 Past Returns and Overconfidence

My preferred interpretation of the past returns evidence is that high past returns increase overconfidence, which in turn increases trading and liquidity. The connection between past returns and overconfidence is based on the learning models of Daniel, Hirshleifer, and Subrahmanyam (1998) and Gervais and Odean (2001). Self attribution bias causes investors to be particularly overconfident following high returns. Because investors hold the market on average, aggregate overconfidence should track market returns. Similarly, individual stock returns could affect stock-level overconfidence. To the extent that investors specialize in certain industries or have industry-specific confidence levels, past industry returns could also affect stock-level overconfidence.

To test the overconfidence interpretation, I analyze investor-level returns and trading activity. Self-attribution bias predicts that an investor's overconfidence will increase following positive returns to his own portfolio. I test this hypothesis using account-level trading records from a discount brokerage firm (this is the Barber and Odean, 2000, data). Specifically, I look at how trading intensity responds to market returns, individual stock returns, and an investor's own portfolio returns. Using six months of trailing trade data, I estimate an investor's portfolio to be the net positions his trade's over that period would result in. I set all short positions to zero because shorting is uncommon for retail investors. The outcome variable of interest is whether buying intensity, measured as the total dollar value of all buy trades increases between month t and month $t+2$. The returns considered are excess returns over the risk free rate in the interim month.

Table 2.3 reports the results. Column (1) regresses increases in overall buying intensity at the investor-month level on market and portfolio returns. Unconditionally, buying intensity increases 15% of the time. 1% shocks to portfolio and market returns increase this probability by 27 and 23 basis points, respectively. Column (2) regresses increases in stock specific

Table 2.3: *Impact of Returns on Buying Intensity*

Dependent variables are indicators for an investor increasing his dollar buying activity over a two-month period. A value of 1 indicates that the dollar sum of all an investor's buy trades in month $t+2$ is greater than the dollar sum of all his buy trades in month t . Column (1) analyzes total buys at the investor-month level. Column (2) analyzes stock-specific buys at the investor-month-stock level. To be included, the investor must have at least two buy trades in month t (overall for column (1) and of the specific stock for column (2)). The explanatory variables represent excess returns over the risk free rate in the interim month ($t+1$). The portfolio return is the return to a portfolio consisting of the investor's cumulative net trades over the six months leading up to month t . Implied short positions are set to zero. Standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance. The analyzed data is discount brokerage trades in 100,000 accounts between 1991 and 1996

	(1) Overall Buy Increase	(2) Stock-Specific Buy Increase
Portfolio Return	0.268*** (0.009)	0.065*** (0.009)
Market Return	0.231*** (0.033)	0.069** (0.032)
Stock Return		0.046*** (0.007)
Constant	0.151*** (0.001)	0.039*** (0.001)
Date Range	1991-1996	1991-1996

buying intensity at the investor-month-stock level on market, portfolio, and individual stock returns. Individual stock buying intensity increases 4% of the time, and 1% shocks to all three return variables increase this probability by 5 to 7 basis points. All coefficient estimates are statistically significant. The results are consistent with past returns increasing investor confidence, causing investors to trade more aggressively.

2.4 Baseline Model

2.4.1 Setup

I consider a model in which agents have fixed endowments of a risky asset and receive private signals about the asset's value. The agents trade the asset in a public market in which all agents see the market-clearing price. Informed by their private signals and the observed market price, agents form beliefs about the asset's payoff and decide how much of it to buy or sell. The only departure from full rationality is that agents are overconfident about the precision of their own signals. All agents are identical other than their realizations of the private signal. Thus, the same agents simultaneously act as informed traders, behavioral traders, and market makers. The model is a variant of Grossman's (1976) rational expectations model in which the one significant change is that agents are overconfident about the precision of their signals. As in Grossman's model, the lack of supply variance or any other noise results in prices that are fully revealing. Nonetheless, overconfidence induces disagreement and trade.

In the next section, I introduce stochastic endowments. This adds liquidity trading to the model and makes prices only partially revealing. The baseline model described here is a limiting case of the more general model. I develop the baseline model separately both for expositional simplicity and because the baseline model corresponds to a setting in which trade is entirely generated by informed disagreement. Since my goal is to understand how liquidity interacts with disagreement trading, this is a natural place to start.

2.4.2 Assumptions

There are two assets, a risk-free asset in elastic supply that yields 1 unit of consumption and a risky asset in fixed supply that yields θ units of consumption and has a price of P (determined in equilibrium), where the risk-free asset is the numeraire. All agents share a common prior that θ is normally distributed with a mean of μ and precision of τ_p (i.e., $\theta \sim \mathcal{N}(\mu, \frac{1}{\tau_p})$). In addition to the common prior, there are private signals with precision τ_s about the asset's value. The signals are $y_m = \theta + \varepsilon_m$, where $\varepsilon_m \stackrel{iid}{\sim} \mathcal{N}(0, \frac{1}{\tau_s})$. τ_p and τ_s are both positive and finite. μ is finite, and it is most natural to think of it as positive.

The economy has N agents divided into M equal groups, each of size $\frac{N}{M}$. Agent i in group $m(i)$ sees signal $y_{m(i)}$. All agents have a known and certain endowment of $\frac{\mu_X}{N}$ units of the risky asset. Thus, each group has an aggregate endowment of $\frac{\mu_X}{M}$ and total asset supply is μ_X .⁸ M is greater than one and finite. More than one group is required to create disagreement and trade. A finite number of groups is required to prevent θ from being perfectly revealed by the aggregate of the signals. I consider the limiting case in which $N \rightarrow \infty$ to ensure that individual agents have negligible impact on the price of the risky asset.⁹ This limiting case is equivalent to a continuum of agents divided into M groups of equal mass.

All agents have constant absolute risk aversion preferences and risk tolerance of $\frac{\eta}{N}$ (i.e., $U_i(c_i) = -\exp\left\{-\frac{N}{\eta}c_i\right\}$). Thus, aggregate risk tolerance is η . Agents are overconfident about the precision of their own signals. They believe ε_m are independent and $\varepsilon_m \sim_i \mathcal{N}(0, \frac{1}{\psi_{i,m}\tau_s})$, where $\psi_{i,m} = \psi$ if agent i is a member of group m and $\psi_{i,m} = 1$ otherwise. Unless otherwise noted, I assume ψ is greater than one and finite (i.e., agents are finitely overconfident). Agents know all model parameters including the overconfidence of other

⁸The μ_X notation is a little unnatural here, but it allows for directly comparable notation in the general model where total asset supply will be normally distributed with mean μ_X and variance V .

⁹This is in contrast to the traditional market microstructure literature (e.g., Kyle, 1985), which models insiders as risk-neutral monopolists. Risk aversion and monopolistic behavior both have the effect of limiting asset demands. Incorporating both would unnecessarily complicate the model. Adding market power (as in Kyle, Obizhaeva, and Wang (2013)) increases the amount of overconfidence necessary to induce investors to trade, decreases trading volumes, and increases liquidity but does not alter the three propositions derived from the baseline model.

agents. Agents observe price but do not observe the signals of other agents.

2.4.3 Equilibrium

I consider an equilibrium in which the asset's price is a linear function of the average private signal. I.e., I assume:

$$P = \alpha + \beta \bar{y} \quad (2.4)$$

where \bar{y} is the average of the M private signals.

Because price is a 1:1 function of the average private signal, all agents effectively see the average signal, from which they can extract the average signal of agents in groups other than their own, $\bar{y}_{-m(i)}$. Specifically, $\bar{y}_{-m(i)} = \frac{M}{\beta(M-1)} (P - \alpha) - \frac{1}{M-1} y_{m(i)}$. Using Bayesian updating, agent i 's posterior beliefs as a function of $y_{m(i)}$ and P are:

$$E_i[\theta | y_{m(i)}, P] = \frac{\tau_p \mu + (\psi - 1) \tau_s y_{m(i)} + \frac{M \tau_s}{\beta} (P - \alpha)}{\tau_p + (M + \psi - 1) \tau_s} \quad (2.5a)$$

$$Var_i[\theta | y_{m(i)}, P] = (\tau_p + (M + \psi - 1) \tau_s)^{-1} \quad (2.5b)$$

Given his CARA utility, agent i 's asset demand is:

$$\begin{aligned} D_i &= \frac{E_i[\theta | y_{m(i)}, P] - P}{\frac{N}{\eta} Var_i[\theta | y_{m(i)}, P]} \\ &= \frac{\eta}{N} \left(\tau_p \mu - \frac{M \tau_s}{\beta} \alpha + (\psi - 1) \tau_s y_{m(i)} - \left(\tau_p + \left(M + \psi - 1 - \frac{M}{\beta} \right) \tau_s \right) P \right) \end{aligned} \quad (2.6)$$

The market clearing price must solve $\mu_X = \sum_i D_i$, which results in a price that is a linear function of \bar{y} . Equating its coefficients with the coefficients of (2.4) yields:

$$P = \frac{\tau_p \mu + (M + \psi - 1) \tau_s \bar{y}}{\tau_p + (M + \psi - 1) \tau_s} - \frac{\mu_X}{\eta (\tau_p + (M + \psi - 1) \tau_s)} \quad (2.7)$$

This result should not be surprising. $\frac{\tau_p \mu + (M + \psi - 1) \tau_s \bar{y}}{\tau_p + (M + \psi - 1) \tau_s}$ is the average posterior expectation of the agents and $\frac{\mu_X}{\eta (\tau_p + (M + \psi - 1) \tau_s)}$ is the risk premium required to hold asset supply μ_X with posterior variance $(\tau_p + (M + \psi - 1) \tau_s)^{-1}$ and aggregate risk tolerance η . Compared to the price that would prevail without overconfidence ($\psi = 1$), equation (2.7) shows that overconfidence biases price toward the private signals and decreases the required risk

premium. For ψ that is small relative to M , both of these effects are modest.

2.4.4 Trading and Liquidity

Each agent's directed trading volume is his net asset demand, $D_i - \frac{\mu_X}{N}$. Aggregate trading is $Vol = \frac{1}{2} \sum_m |Trade_m|$, where $Trade_m$ is the net asset demand of group m :

$$\begin{aligned} Trade_m &= \sum_{i:m(i)=m} \left[D_i - \frac{\mu_X}{N} \right] \\ &= \frac{\eta}{M} (\psi - 1) \tau_s (y_m - \bar{y}) \end{aligned} \quad (2.8)$$

$|Trade_m|$ is a folded mean-zero random variable so its expectation is $E |Trade_m| = \sqrt{\frac{2Var(Trade_m)}{\pi}}$.

Expected aggregate trading is:

$$\begin{aligned} E [Vol] &= \frac{1}{2} \sum_m E |Trade_m| \\ &= \frac{\eta (\psi - 1)}{2} \sqrt{\frac{2 (1 - \frac{1}{M}) \tau_s}{\pi}} \end{aligned} \quad (2.9)$$

From equation (2.9) it is clear that trading increases with ψ and τ_s and is unaffected by τ_p .

In this model there is no liquidity trading, but the concept of liquidity is still operative. Analogous to Kyle's (1985) lambda, I define illiquidity as the price impact of trade resulting from an exogenous shock. Intuitively, I am interested in how price would respond to an exogenous buy or sell trade. However, there is no exogenous trading in this model (nor is there in the real world). Rather, trade is an endogenous response to underlying shocks received by agents. Illiquidity is the ratio of a shock's price impact to its impact on the shocked agents' trades (i.e., their net asset demand). Because agents only interact through their trades, this ratio exactly represents the trades' price impact. A shock affects an entire group of agents so the relevant net asset demand is the group's, $Trade_m$.¹⁰ Formally, illiquidity is:

¹⁰In the baseline model, the only shock is to a group's signal so this is the shock I use to define illiquidity. More generally, one could also consider the impact of group endowment shocks or even shocks to individual agents. In all cases the resulting illiquidity is the same because in an anonymous market any trade must have the same price impact regardless of its source.

$$\lambda \equiv \frac{\frac{dP}{dy_m}}{\frac{dTrade_m}{dy_m}} \quad (2.10)$$

Taking derivatives of $Trade_m$ (eq. 2.8) and P (eq. 2.7) with respect to y_m yields:

$$\begin{aligned} \lambda &= \frac{M(M+\psi-1)}{\eta(M-1)(\psi-1)(\tau_p + (M+\psi-1)\tau_s)} \\ &= \left\{ \frac{M}{(M-1)\eta(\tau_p + (M+\psi-1)\tau_s)} \right\} \\ &\quad + \left\{ \left[\frac{\tau_s}{\tau_p + (M+\psi-1)\tau_s} \right] \left[\frac{\eta}{M} \left(\psi - \frac{(M+\psi-1)}{M} \right) \tau_s \right]^{-1} \right\} \\ &= \{S\} + \{B\} \end{aligned} \quad (2.11)$$

Equation (2.11) shows that a buy trade affects price in two ways. First, it decreases the net asset supply that must be held by the non-shocked agents. The supply effect (S) is the decline in the risk premium required by the non-shocked agents.¹¹ Second, the trade increases non-shocked agents' posterior expectations. B captures this belief channel. The trade's impact on posterior expectations is the informational value of a y_m shock, $\left[\frac{\tau_s}{\tau_p + (M+\psi-1)\tau_s} \right]$, divided by how aggressively the shocked agents trade on the shock, $\left[\frac{\eta}{M} \left(\psi - \frac{(M+\psi-1)}{M} \right) \tau_s \right]$.¹²

Note that trading aggression is proportional to private signal precision and private signal value is the ratio of private signal precision to total precision. As a result, illiquidity depends only on aggregate information $(\tau_p + (M+\psi-1)\tau_s)$, not its component parts. Public and private information both enhance liquidity. By contrast, overconfidence more than proportionally increases trading aggression without having much impact on signal value or aggregate information. Thus, overconfidence enhances liquidity, primarily through the belief channel.

The above equations and discussion support three propositions about how overconfidence and asymmetric information affect trading and liquidity.

¹¹The non-shocked agents have posterior variance $(\tau_p + (M+\psi-1)\tau_s)^{-1}$ and risk tolerance $\frac{(M-1)\eta}{M}$, resulting in a risk premium (price reduction) of $Supply * \frac{M}{(M-1)\eta(\tau_p + (M+\psi-1)\tau_s)}$.

¹²Taking the derivative of equation (2.8) with respect to y_m establishes that $\frac{dTrade_m}{dy_m} = \frac{\eta}{M} \left(\psi - \frac{(M+\psi-1)}{M} \right) \tau_s$.

Proposition 1. *As overconfidence increases (ψ increases), trading and liquidity both increase.*

Proposition 2. *As private information becomes more precise (τ_s increases), trading and liquidity both increase.*

Proposition 3. *As public uncertainty increases (τ_p decreases), trading is unaffected and liquidity decreases.*

Of the three propositions, proposition 2 is probably most surprising because it directly contradicts the traditional intuition that private information destroys liquidity and causes markets to break down. The general model develops this contrast in more detail and shows that private information enhances liquidity whenever the mix of informed and uninformed trade is insensitive to increases in private information. This is clearly the case in the baseline model because it only includes informed trade.

Propositions 2 and 3 concern different aspects of asymmetric information. Asymmetric information can be high because private signals are precise or because there is little public information. In either case, private information is more valuable and beliefs rely more heavily on private signals. In combination, propositions 2 and 3 imply that asymmetric information (weakly) increases trading and has an ambiguous impact on liquidity.

2.5 General Model

2.5.1 Setup and Assumptions

The general model is identical to the baseline model except that endowments are uncertain and unknown to agents in other groups. Specifically, agent i in group m (i) is endowed with $\frac{M}{N}x_{m(i)}$ units of the risky asset, where $x_m \stackrel{iid}{\sim} \mathcal{N}\left(\frac{\mu_X}{M}, \frac{V}{M}\right)$ is the total endowment of group m . The resulting total asset supply is $X = \sum_m x_m \sim \mathcal{N}(\mu_X, V)$. Agents not in group m know the distribution of x_m , but do not observe x_m .

The model is a variant of Diamond and Verrecchia's (1981) noisy rational expectations model in which the one significant change is that agents are overconfident about the

precision of their signals. The main distinguishing characteristic of Diamond and Verrecchia (1981) compared to other noisy rational expectations models (e.g., Hellwig, 1980) is that Diamond and Verrecchia consider endowment shocks to modeled agents whereas Hellwig and others consider direct, unobserved shocks to aggregate asset supply. The Diamond and Verrecchia approach is more natural because it makes liquidity trading an endogenous response to underlying endowment shocks instead of modeling liquidity trades as direct exogenous shocks to external asset supply. Diamond and Verrecchia's approach is also analytically convenient because it yields closed form solutions.

Results from the model are presented and discussed below. Derivations are in the appendix.

2.5.2 Equilibrium

I assume that price is a linear function of the average private signal and aggregate asset supply:

$$P = \alpha + \beta \bar{y} - \gamma (X - \mu_X) \quad (2.12)$$

Given the price function described by equation (2.12), agent i extracts a noisy signal ($A_{m(i)}$) for the average private signal of other groups ($\bar{y}_{-m(i)}$) from observing price, $y_{m(i)}$, and $x_{m(i)}$:

$$\begin{aligned} A_{m(i)} &= \frac{M}{\beta(M-1)} (P - \alpha) - \frac{1}{M-1} y_{m(i)} + \frac{\gamma M}{\beta(M-1)} \left(x_{m(i)} - \frac{\mu_X}{M} \right) \\ &= \bar{y}_{-m(i)} - \frac{\gamma M}{\beta} \left(\bar{x}_{-m(i)} - \frac{\mu_X}{M} \right) \end{aligned} \quad (2.13)$$

Note that $A_{m(i)}$ is independent of $y_{m(i)}$ and $x_{m(i)}$ and $A_{m(i)} \sim_i \mathcal{N} \left(\theta, \frac{1}{\tau_A} \right)$, where τ_A is the precision agent i attributes to $A_{m(i)}$:

$$\tau_A = \left(\frac{1}{(M-1) \tau_s} + \left(\frac{\gamma}{\beta} \right)^2 \frac{M}{M-1} V \right)^{-1} \quad (2.14)$$

Agent i forms posterior beliefs about the asset's payoff (θ) using Bayesian updating with signals $y_{m(i)}$ and $A_{m(i)}$. All agents use their posterior beliefs to determine their asset demands. Setting total asset demand equal to total asset supply results in a market-clearing

price that is a linear function of the average private signal and aggregate asset supply just as I assumed in equation (2.12). The resulting fixed point problem has the unique solution:

$$\alpha = \frac{(\eta^2 \psi^2 \tau_p \tau_s + MV \tau_p) \mu - \left(\eta \psi^2 \tau_s + \frac{MV}{\eta} \right) \mu_X}{\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV} \quad (2.15a)$$

$$\beta = \frac{\psi \tau_s (\eta^2 \psi (M + \psi - 1) \tau_s + MV)}{\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV} \quad (2.15b)$$

$$\gamma = \frac{\eta^2 \psi (M + \psi - 1) \tau_s + MV}{\eta (\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV)} \quad (2.15c)$$

For many applications, the ratio of γ to β is an important quantity. I define this ratio as:

$$\Gamma \equiv \frac{\gamma}{\beta} = \frac{1}{\eta \psi \tau_s} \quad (2.16)$$

To see that the baseline model is a limiting case of the general model, note that as $V \rightarrow 0$, $X \xrightarrow{p} \mu_X$ and $P \xrightarrow{p} \frac{\tau_p \mu + (M + \psi - 1) \tau_s \bar{y}}{\tau_p + (M + \psi - 1) \tau_s} = \frac{\mu_X}{\eta (\tau_p + (M + \psi - 1) \tau_s)}$, the baseline model price.

2.5.3 Price Informativeness

In the baseline model, price fully revealed all relevant information about the asset's value. When endowments are stochastic, this is no longer the case. How much less informative is price?

One measure of price informativeness, used by Diamond and Verrecchia (1981), is the posterior precision an agent achieves relative to what his posterior precision would be if he observed all signals. Under full information, each agent has a posterior precision of $\tau_p + (M + \psi - 1) \tau_s$.¹³ This is the same posterior precision achieved in the baseline model. In the general model each agent knows the public prior and observes $y_{m(i)}$ and $A_{m(i)}$, resulting in posterior precision:

$$\tau_p + \psi \tau_s + \tau_A = \tau_p + \psi \tau_s + \left(\frac{1}{(M - 1) \tau_s} + \Gamma^2 \frac{M}{M - 1} V \right)^{-1} \quad (2.17)$$

More recently, Bai, Philippon, and Savov (2012) propose measuring price informativeness

¹³The public prior has precision τ_p ; an agent's own signal has subjective precision $\psi \tau_s$; and the $M - 1$ signals of agents in other groups each have precision τ_s . Because the signals and prior are all independent, their precisions are additive.

from the econometrician's point of view. Specifically, they measure price informativeness as the R^2 of a regression of price on future asset value. In the general model, $P = \alpha + \beta \bar{y} - \gamma (X - \mu_X)$ has a variance of $\beta^2 \left(\frac{1}{\tau_p} + \frac{1}{M\tau_s} \right) + \gamma^2 V$; asset value (θ) has a variance of $\frac{1}{\tau_p}$; and the covariance of price with asset value is $\frac{\beta}{\tau_p}$, resulting in:

$$R^2 = \frac{\tau_p^{-1}}{\tau_p^{-1} + (M\tau_s)^{-1} + \Gamma^2 V} \quad (2.18)$$

By contrast, if agents saw all private signals (as they effectively do in the baseline model), the R^2 of this regression would be $\frac{\tau_p^{-1}}{\tau_p^{-1} + (M\tau_s)^{-1}}$.

Under both measures of price informativeness, deviations from baseline full revelation price informativeness are a function of $\Gamma^2 V = \frac{V}{\eta^2 \psi^2 \tau_s^2}$. As noise (V) increases, price informativeness decreases. As risk tolerance (η), overconfidence (ψ), and private information (τ_s) grow, prices become more informative. Roughly speaking, price informativeness is determined by the relative levels of informed and liquidity trading. Liquidity trading is increasing in V . Informed trading is increasing in η , ψ , and τ_s .

2.5.4 Trading

As in the baseline model, group m 's directed trading volume is its net asset demand. The difference is that group m 's trading now depends on two random shocks instead of just one. Specifically, $Trade_m = \left\{ \frac{\eta}{M} (\psi \tau_s - \frac{\tau_A}{M-1}) (y_m - \bar{y}) \right\} - \left\{ \left(1 - \frac{\eta \gamma \tau_A}{(M-1)\beta} \right) (x_m - \bar{x}) \right\}$, where the $(y_m - \bar{y})$ term represents informed trading and the $(x_m - \bar{x})$ term represents liquidity trading. Informed trading is greater than in the baseline model.¹⁴ Agents now have two motives for informed trade. First, overconfidence ($\psi > 1$) causes them to overweight their own signals as in the baseline model. Second, price no longer fully reveals the average signal, giving agents another reason to trade on their own signal. Liquidity trading is less than the endowment shocks themselves because endowment shocks are partially offset by demand changes. Agents realize that endowment shocks affect price and take this into

¹⁴To see that informed trade is greater than in the baseline model, note that $\tau_A < (M-1)\tau_s$. Thus, $\frac{\eta}{M} (\psi \tau_s - \frac{\tau_A}{M-1}) < \frac{\eta}{M} (\psi - 1) \tau_s$, the trading coefficient on $(y_m - \bar{y})$ in the baseline model.

account when determining their asset demands.¹⁵ As a result, liquidity, asset riskiness, and risk tolerance all influence liquidity trading.

Expected trading volume increases in the variance of group m 's trading:¹⁶

$$\begin{aligned}
Var[Trade_m] &= \{Var[Informed_Trade_m]\} + \{Var[Liquidity_Trade_m]\} \\
&= \left\{ \frac{\eta^2 (M-1) \psi^2 \tau_s (\eta^2 (\psi-1) \psi \tau_s + MV)^2}{M^3 (\eta^2 \psi^2 \tau_s + MV)^2} \right\} \\
&\quad + \left\{ \frac{(M-1) (\eta^2 (\psi-1) \psi \tau_s + MV)^2 V}{M^2 (\eta^2 \psi^2 \tau_s + MV)^2} \right\} \\
&= \frac{(M-1) (\eta^2 (\psi-1) \psi \tau_s + MV)^2}{M^3 (\eta^2 \psi^2 \tau_s + MV)} \tag{2.19}
\end{aligned}$$

From equation (2.19), it is clear that public uncertainty (τ_p^{-1}) has no impact on trading volume, just as in the baseline model. Taking derivatives with respect to ψ , one can also see that overconfidence increases overall and informed trading (again consistent with the baseline model). Overconfidence can initially decrease liquidity trading if V is large, but as ψ increases it eventually decreases liquidity trading as well.¹⁷ These effects are small. In practice, overconfidence has very little impact on liquidity trading.

The relationship between private information (τ_s) and trade is more complicated. Liquidity trading always decreases with τ_s . When overconfidence is high ($\psi > \frac{9}{8}$ for informed trade and $\psi > 2$ for overall trade), informed and overall trading increase monotonically with τ_s . When overconfidence is moderate ($1 < \psi < \frac{9}{8}$ for informed trade and $1 < \psi < 2$ for overall trade), informed and overall trading increase with τ_s if τ_s is large relative to V .¹⁸ Without overconfidence, all types of trading decrease with τ_s . Essentially, private

¹⁵ Agents are atomistic and do not have any price impact by themselves (thus no monopoly pricing motive is present), but endowment shocks are shared by a positive mass of agents. The group's endowment shock drives a wedge between price and group's posterior value, which agents in the group exploit by changing asset demand in the opposite direction of the endowment shock.

¹⁶ Specifically, expected volume is $E[Vol] = \frac{1}{2} \sum_m E|Trade_m|$ and $E|Trade_m| = \sqrt{\frac{2Var(Trade_m)}{\pi}}$ just as in the baseline model.

¹⁷ Specifically, $\frac{dVar[Liquidity_Trade_m]}{d\psi} < 0$ if $1 < \psi < \frac{1}{\eta} \sqrt{\frac{MV}{\tau_s}}$ and is positive for larger ψ .

¹⁸ Assuming $\psi > 1$, $\frac{dVar[Informed_Trade_m]}{d\tau_s} < 0$ iff $\psi < \frac{9}{8}$ and $\tau_s < \frac{MV(3-2\psi-\sqrt{9-8\psi})}{2\eta^2\psi^2(\psi-1)}$ and $\frac{dVar[Trade_m]}{d\tau_s} < 0$ iff

information always induces trade when there is high overconfidence. Under moderate overconfidence, private information decreases trade in liquidity trading (high V) environments but increases trade in disagreement trading (low V) environments. The Akerlof (1970) logic that private information destroys trade applies when agents are fully rational and in liquidity trading environments when agents are only moderately overconfident. When trade primarily stems from overconfident disagreement, the opposite effect prevails, and private information increases trade.

2.5.5 Liquidity

I employ the same definition and measure of liquidity that I introduced in the baseline model. Illiquidity is the price impact of a trade resulting from an exogenous shock, formally measured as:

$$\lambda \equiv \frac{\frac{dP}{dy_m}}{\frac{dTrade_m}{dy_m}}$$

I could just as easily define λ using endowment (x_m) shocks instead of information (y_m) shocks. The resulting λ is the same. In either case, the shocked agents interact with the rest of the market only through their trading demand. Thus, a given shock to trading must have the same price impact regardless of what motivated the trade. This can be verified algebraically by taking derivatives with respect to x_m instead of y_m . Even more generally, I could consider shocks to individual agents or exogenous trades external to the model. Regardless, price will always have the same response to a unit trade shock.

Taking derivatives of price and net asset demand with respect to underlying shocks

$$\psi < 2 \text{ and } \tau_s < \frac{(2-\psi)MV}{\eta^2\psi^2(\psi-1)}.$$

yields:

$$\begin{aligned}
\lambda &= \left\{ \frac{M}{(M-1)\eta(\tau_p + \psi\tau_s + \tau_A)} \right\} \\
&\quad + \left\{ \frac{\eta^2\psi^2\tau_s}{\eta^2\psi^2\tau_s + MV} \right\} \left\{ \frac{\tau_s}{\tau_p + \psi\tau_s + \tau_A} \right\} \left\{ \frac{\eta}{M} \left(\psi\tau_s - \frac{\beta}{M}(\tau_p + \psi\tau_s + \tau_A) \right) \right\}^{-1} \\
&= \{S\} + \{B1\} \{B2\} \{B3\}^{-1} \tag{2.20}
\end{aligned}$$

Equation (2.20) expresses lambda as the sum of a supply channel and a belief channel. The belief channel is further decomposed into the probability that a trade is informed (B1) times the impact a known shock to y_m would have on the posteriors of other agents (B2) divided by how aggressively shocked agents trade on y_m shocks (B3). S , $B2$, and $B3$ were present in the baseline model. As before, S and $\frac{B2}{B3}$ tend to decrease as total information ($\tau_p + \psi\tau_s + \tau_A$) increases regardless of whether the information is public or private. S and $\frac{B2}{B3}$ also decrease with overconfidence.

$B1$ is new and deserves special consideration. First note that $B1 = \frac{\eta^2\psi^2\tau_s}{\eta^2\psi^2\tau_s + MV}$ is the probability that a trade is informed. Specifically, $B1$ is the ratio of informed trading variance to total trading variance (see equation (2.19) to verify this). $B1$ is increasing in ψ and τ_s and represents the channel through which they can destroy liquidity. Private information and overconfidence increase informed trading as a share of overall trading. When V is close to $\frac{\eta^2\psi^2\tau_s}{M}$, this ratio is highly sensitive to ψ and τ_s . By contrast, for very small or large V , $B1$ is close to 1 or 0 and fairly stable. The traditional logic that private information destroys liquidity applies only when increases in private information have a large impact on the ratio of informed to total trade. In particular, the traditional logic does not apply to disagreement trading environments because in those environments trade is primarily informed regardless of the exact level of private information. Similarly, overconfidence and private information enhance liquidity in extreme liquidity trading environments. The appendix formally considers derivatives of λ with respect to ψ , τ_s , and τ_p and derives parameter regions in which the derivatives are positive and negative. The appendix also shows that private information can enhance liquidity even without overconfidence. The

basic result hinges on how much trading is informed, not on the presence of overconfidence.

2.5.6 Numerical Examples

To better understand how overconfidence and asymmetric information affect trading and liquidity, it is useful to consider numerical examples. I use the following baseline parameter values:

$$\mu = 1$$

$$\mu_X = 1$$

$$M = 10$$

$$\tau_p = 100$$

$$\tau_s = 10$$

$$\psi = 2$$

$$\eta = 0.1$$

$$V \in \{0.0000001, 0.1, 10\}$$

μ and μ_X are normalized to one. I consider 10 groups of agents. Prior precision of 100 yields a public prior standard deviation of 10%. Private precision of 10 makes the private signals in aggregate as valuable as the public prior. Overconfidence of 2 means that agents attribute twice as much value to their own signals as they do to the signals of agents in other groups. Aggregate risk tolerance of 0.1 produces a risk premium of 10% under public information without supply shocks.

I start by considering a low variance environment ($V = 0.0000001$), which roughly corresponds to the baseline constant endowment model. At baseline values, expected turnover is 12% and $\lambda = 58\%$ (meaning an exogenous trade of 1% of aggregate asset supply would change the asset's price by 58 basis points). The first row of Figure 2.5 plots these quantities as functions of overconfidence, varying ψ from 1 to 10 while holding all other parameters at baseline values. Panel A shows that trading is approximately zero when $\psi = 1$ and trading increases close to proportionally with ψ . When $\psi = 2$, expected turnover is 12%. When $\psi = 10$, expected turnover is 108%. The solid line in Panel B plots λ as

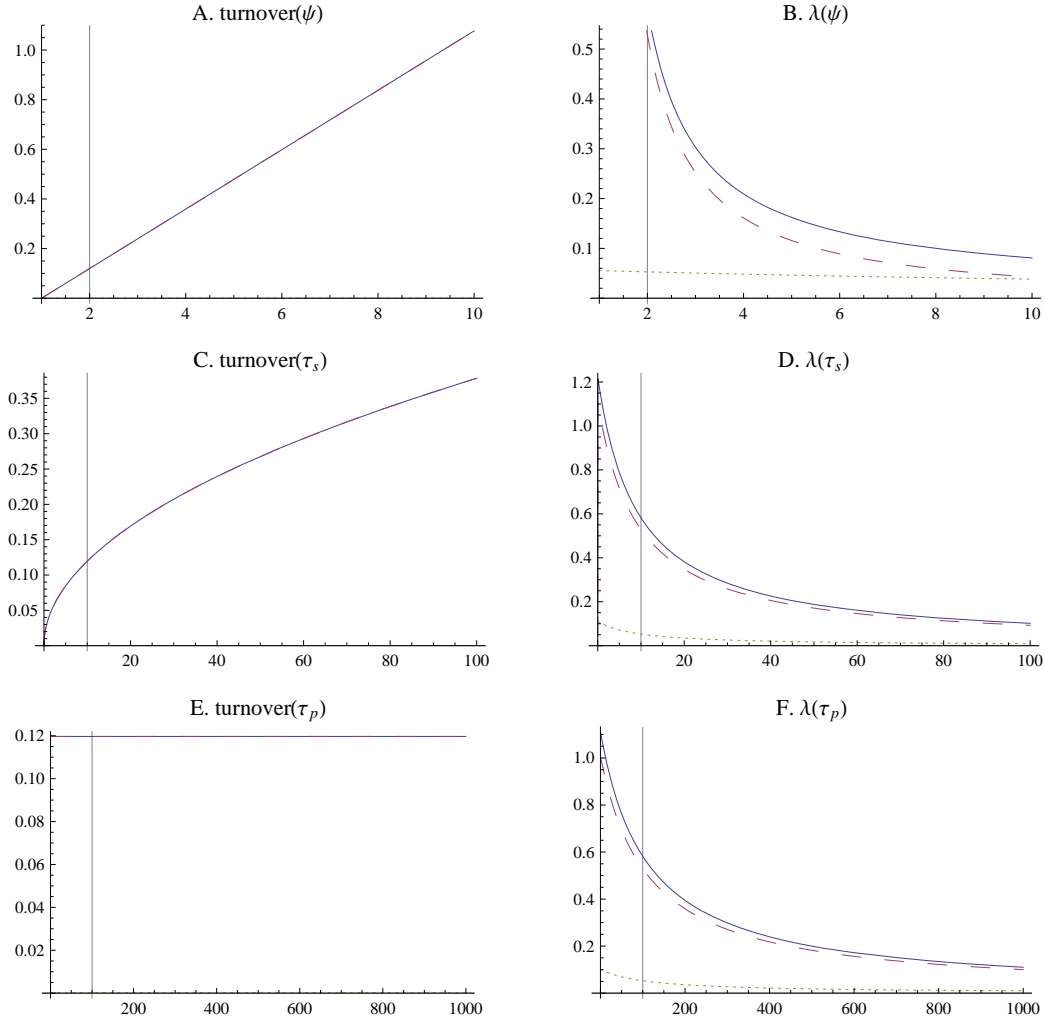


Figure 2.5: *Trading and Illiquidity under Low Variance*

Expected turnover and illiquidity (λ) are calculated using values indicated on the horizontal axis for the parameter in parentheses and low variance baseline values ($\mu = 1$, $\mu_x = 1$, $M = 10$, $\tau_p = 100$, $\tau_s = 10$, $\psi = 2$, $\eta = 0.1$, $V = 0.0000001$) for all other parameters. Vertical lines represent the baseline. Expected total turnover is a solid line; expected informed turnover is a dashed line; and expected liquidity turnover is a dotted line. Overall illiquidity is a solid line; the illiquidity belief channel is a dashed line; and the illiquidity supply channel is a dotted line.

a function of ψ . As predicted by the baseline model, the market is highly illiquid when $\psi = 1$ (approaching infinity as $V \rightarrow 0$) and becomes more liquid as ψ increases. When $\psi = 2$, $\lambda = 58\%$. When $\psi = 10$, $\lambda = 8\%$. Beyond $\psi = 10$, λ continues to decrease with ψ , approaching 0 as $\psi \rightarrow \infty$. The dotted and dashed lines in panel B decompose λ into its supply and belief channels. The belief channel (dashed line) is the dominant source of illiquidity. The second row of Figure 2.5 repeats the same exercise, varying private signal precision from 0 to 100. As private signals become more precise, trading increases (panel C) and illiquidity decreases (panel D). The final row of Figure 2.5 considers public prior precision. As predicted, turnover is unaffected and illiquidity decrease as τ_p increases.

Figure 2.6 plots expected turnover and illiquidity as functions of overconfidence, private information precision, and public prior precision in a moderate supply variance environment. Baseline parameter values are the same as before except that endowment variance is now 0.1, which corresponds to an aggregate asset supply standard deviation of 0.32, compared to its mean of 1. These examples capture a market in which trading comes from both informational and liquidity motives. Panels A, C, and E plot expected total turnover (solid line), expected informed turnover (dashed line), and expected liquidity turnover (dotted line). Informed turnover is the turnover that would prevail if agents differed only in their information shocks (i.e., if $x_m = \bar{x} \forall m$). Analogously, liquidity turnover is the turnover that would prevail if agents differed only in their supply shocks. Note that total turnover is less than the sum of informed and liquidity turnover because these two types of trade partially offset one another.

The $\psi = 1$ starting point of panel A plots turnover in the absence of overconfidence, which recreates the Diamond and Verrecchia (1981) model. As alluded to earlier in the paper, liquidity turnover represents 95% of total turnover. As overconfidence (panel A) and private information precision (panel C) increase, informed turnover increases, driving up total turnover. By contrast, private information decreases liquidity turnover as τ_s increases. Liquidity turnover is fairly insensitive to overconfidence. At first it slightly decreases with ψ , then it slightly increases with ψ . Both forms of turnover are unaffected by public prior

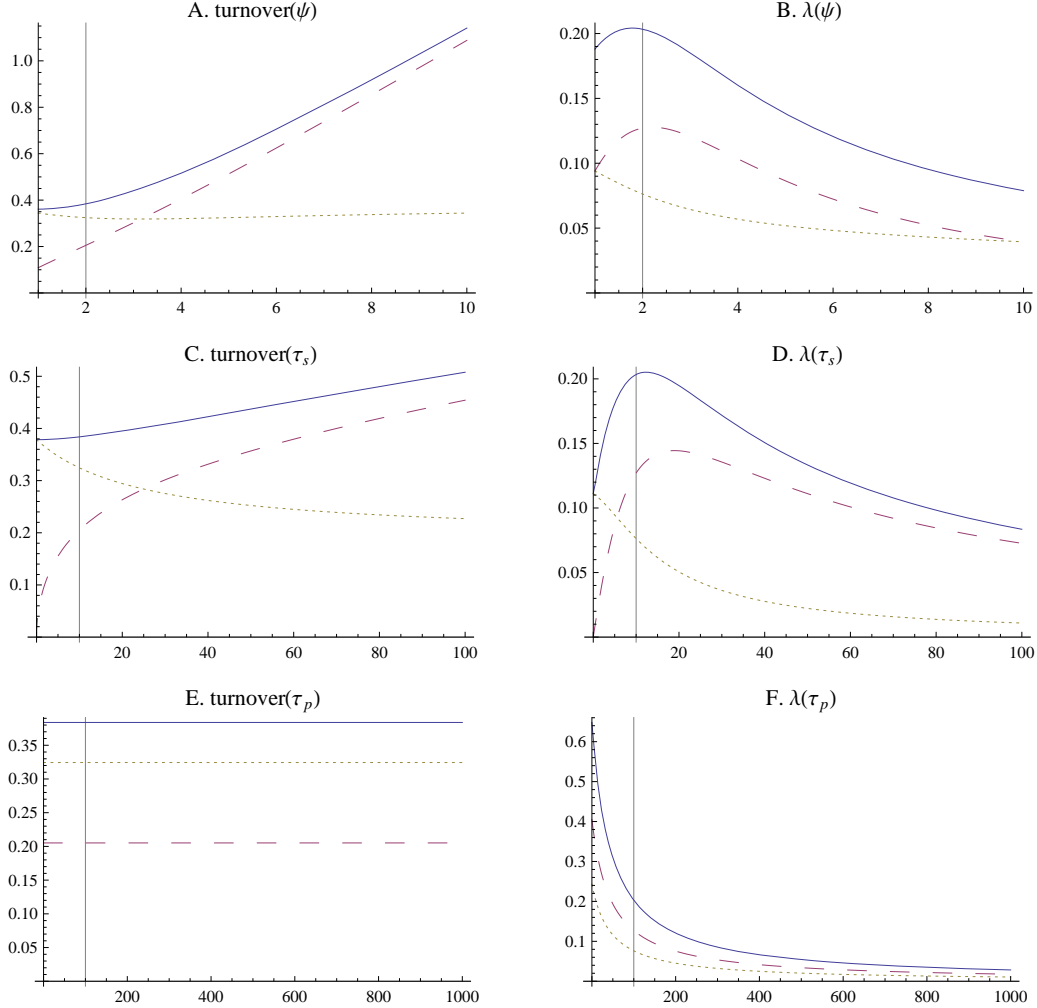


Figure 2.6: Trading and Illiquidity under Moderate Variance

Expected turnover and illiquidity (λ) are calculated using values indicated on the horizontal axis for the parameter in parentheses and moderate variance baseline values ($\mu = 1$, $\mu_x = 1$, $M = 10$, $\tau_p = 100$, $\tau_s = 10$, $\psi = 2$, $\eta = 0.1$, $V = 0.1$) for all other parameters. Vertical lines represent the baseline. Expected total turnover is a solid line; expected informed turnover is a dashed line; and expected liquidity turnover is a dotted line. Overall illiquidity is a solid line; the illiquidity belief channel is a dashed line; and the illiquidity supply channel is a dotted line.

precision.

As expected, liquidity trading enhances liquidity. The baseline λ decreases from 58% to 20% when V increases from 0.0000001 to 0.1. The reduction in λ is entirely driven by the belief channel. Belief and supply illiquidity now have similar magnitudes. Most interestingly, liquidity trading changes the relationships between ψ , τ_s , and illiquidity. Illiquidity is now a hump-shaped function of ψ (panel B) and τ_s (panel D). Overconfidence and private information precision initially decrease liquidity before eventually enhancing it. Panels A and C show why. Initial increases in ψ and τ_s dramatically increase the ratio of informed trading to total trading, which increases the probability that any given trade is informed. At higher levels of ψ and τ_s this ratio and probability are fairly stable.

Figure 2.7 replicates the moderate variance example under a no-overconfidence ($\psi = 1$) baseline. Panel A shows that without overconfidence private information decreases turnover. This is an illustration of the general result derived above. Overconfidence is a necessary ingredient for private information to increase trading. Nonetheless, panel B shows that private information enhances liquidity for τ_s above 32. Overconfidence amplifies this liquidity enhancement but is not necessary for the basic result.

Figure 2.8 plots expected turnover and illiquidity in a high supply variance ($V = 10$) environment in which trading is primarily liquidity-driven. In this environment, liquidity is enhanced (the baseline λ is 9.4%, and this is almost entirely from the supply channel). λ decreases in ψ , τ_s , and τ_p (see panels B, D, and F) because only the supply channel is really in play. Panels A, C, and E show that expected total turnover is high (its baseline value is 378%) and insensitive to ψ , τ_s , and τ_p even though ψ and τ_s increase informed trading.

2.6 Model Assessment

Unlike traditional models, disagreement trading generates significant trading and liquidity in the baseline model even without exogenous noise. Moreover, disagreement trading is consistent with the stylized facts developed in Section 2.

First, high turnover is generally associated with high liquidity. This is easiest to see

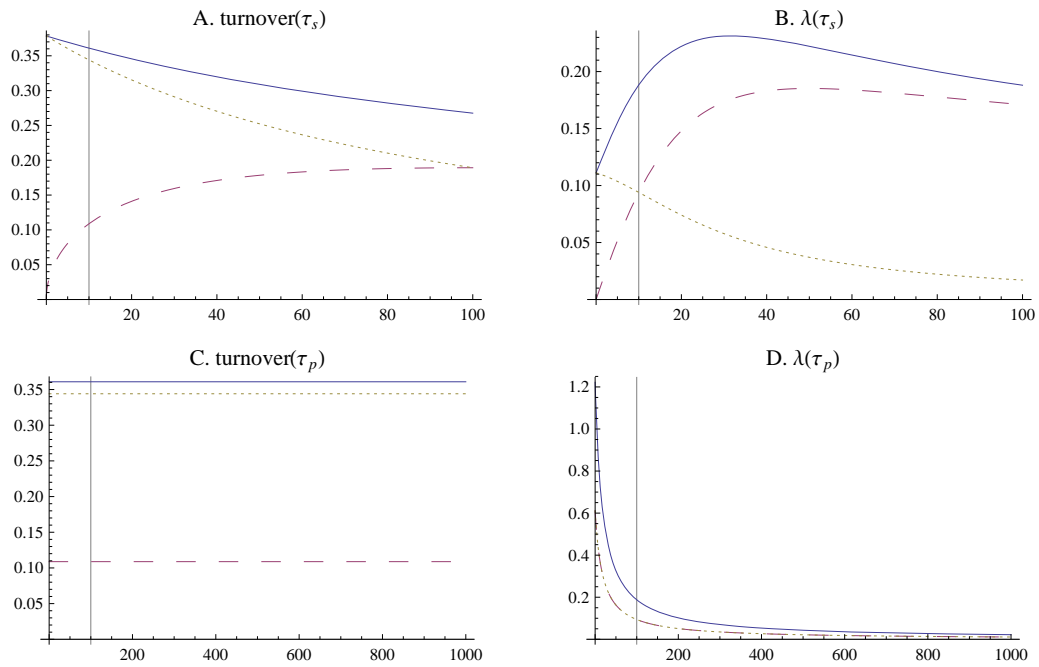


Figure 2.7: *Trading and Illiquidity without Overconfidence*

Expected turnover and illiquidity (λ) are calculated using values indicated on the horizontal axis for the parameter in parentheses and moderate variance baseline values without overconfidence ($\mu = 1$, $\mu_x = 1$, $M = 10$, $\tau_p = 100$, $\tau_s = 10$, $\psi = 1$, $\eta = 0.1$, $V = 0.1$) for all other parameters. Vertical lines represent the baseline. Expected total turnover is a solid line; expected informed turnover is a dashed line; and expected liquidity turnover is a dotted line. Overall illiquidity is a solid line; the illiquidity belief channel is a dashed line; and the illiquidity supply channel is a dotted line.

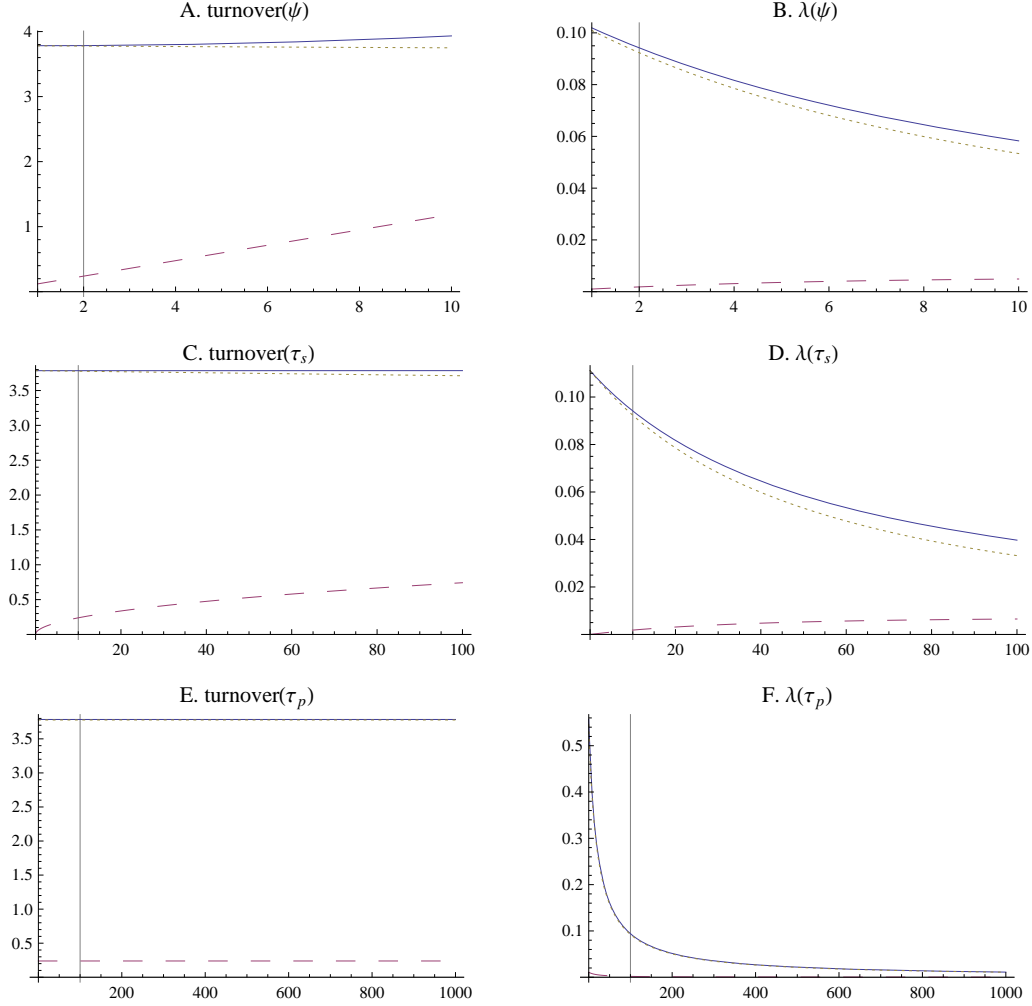


Figure 2.8: Trading and Illiquidity under High Variance

Expected turnover and illiquidity (λ) are calculated using values indicated on the horizontal axis for the parameter in parentheses and high variance baseline values ($\mu = 1$, $\mu_x = 1$, $M = 10$, $\tau_p = 100$, $\tau_s = 10$, $\psi = 2$, $\eta = 0.1$, $V = 10$) for all other parameters. Vertical lines represent the baseline. Expected total turnover is a solid line; expected informed turnover is a dashed line; and expected liquidity turnover is a dotted line. Overall illiquidity is a solid line; the illiquidity belief channel is a dashed line; and the illiquidity supply channel is a dotted line.

by comparing the low, medium, and high variance numerical examples. As liquidity trading increases across the scenarios, trading and liquidity both increase dramatically. Overconfidence also typically moves trading and liquidity in the same direction.

Second, the disagreement model is consistent with asymmetric information increasing trade while decreasing liquidity. Proposition (2) of the baseline model predicts that private information increases trade and liquidity. Proposition (3) predicts that public uncertainty decreases liquidity while having no impact on trading. Jointly, propositions (2) and (3) predict that asymmetric information (which consists of private information and public uncertainty) can only increase trading and has an ambiguous effect on liquidity. Unlike traditional models, these predictions are consistent with observed empirical evidence.

Third, overconfidence increases trade and liquidity. If overconfidence increases following high past returns, as self-attribution bias theory predicts, this delivers the prediction that turnover and liquidity will increase following high past returns.

In addition to conforming with the stylized facts, the model generates new predictions about how the impact of asymmetric information on trading and liquidity varies with the type of asymmetric information shock, the level of liquidity trading, and the existing level of private information. Testing these predications is challenging because they involve unobservable quantities, and I have not found a way to separately identify private information, public uncertainty, and liquidity trading. Fortunately, the model itself provides guidance for differentiating private information changes from public uncertainty changes. In the baseline model, private information increases trading, whereas public uncertainty has no impact on it. Thus, asymmetric information changes with a larger trading impact are more likely to be driven by changes in private information. The baseline model predicts that private information enhances liquidity whereas public uncertainty reduces it. Thus, we should expect asymmetric information to have the least negative impact on liquidity (and potentially even enhance it) when it has the most impact on trading.

I test this prediction in the data by sorting stocks based on their past turnover responses to asymmetric information changes. Specifically, I estimate stock-level rolling 5-year regressions

Table 2.4: *Analyst Dispersion Panel Regressions by Lagged Turnover Response*

Results are for stock-level regressions of log turnover and log illiquidity measures on lagged (by one month) log dispersion of analyst earnings forecasts. Medium and high turnover responsiveness indicator variables are based on turnover responsiveness to dispersion changes over the past five years relative to 30th and 70th percentile breakpoints. Data is limited to NYSE stocks with lagged prices greater than \$5, at least 2 analyst forecasts, and fiscal years that end in December. Robust clustered (by firm) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	(1) Log Turnover	(2) Log illiq	(3) Log bidask	(4) Log qbidask	(5) Log ebidask
Lagged Log Analyst Dispersion	-0.006 (0.006)	0.210*** (0.010)	0.100*** (0.005)	0.109*** (0.005)	0.111*** (0.005)
Lagged Log Dispersion * Medium Turn Response	0.024*** (0.006)	-0.002 (0.010)	-0.006 (0.005)	-0.006 (0.005)	-0.005 (0.005)
Lagged Log Dispersion * High Turn Response	0.058*** (0.007)	-0.041*** (0.013)	-0.007 (0.007)	-0.011* (0.006)	-0.008 (0.006)
Medium Turn Response	0.031 (0.021)	0.033 (0.036)	0.0002 (0.021)	0.009 (0.020)	0.013 (0.021)
High Turn Response	0.190*** (0.026)	-0.126*** (0.048)	0.023 (0.026)	0.007 (0.025)	0.021 (0.025)
Stock FE	Yes	Yes	Yes	Yes	Yes
Year FE	Yes	Yes	Yes	Yes	Yes
Month FE	Yes	Yes	Yes	Yes	Yes
Date Range	1981-2011	1981-2011	1993-2011	1993-2011	1993-2011

of turnover on lagged analyst forecast dispersion, controlling for aggregate dispersion. Stocks are annually sorted into low, medium, and high responsiveness groups based on 30th and 70th percentile breakpoints. I then replicate my analyst forecast dispersion panel regressions with interactions between analyst forecast dispersion and past turnover responsiveness groups.

Table 2.4 reports the results. Column (1) shows that turnover responsiveness to analyst forecast dispersion is persistent. Low past turnover responsiveness stocks have no turnover response to analyst forecast dispersion (the coefficient of log turnover on log lagged analyst dispersion is an insignificant -0.6% for the low responsiveness group). As past turnover responsiveness increases, this coefficient increases by 2.4 ppt for the medium responsiveness group and 5.8 ppt for the high responsiveness group. Both results are highly significant.

The model predicts that as turnover responsiveness increases, illiquidity responsiveness should decrease. This is what I find in the data. Column (2) presents results for *illiq*. High turnover response stocks have a highly significant 4.2 ppt lower illiquidity response to analyst dispersion compared to low turnover response stocks. Medium turnover response stocks have about the same dispersion coefficient as low turnover response stocks. Column (3) to (5) present results for different bid-ask spread measures. The pattern is the same. As turnover responsiveness increases, bid-ask responsiveness decreases. In part due to the shorter sample, most of the bid-ask spread results are not significant. The exception is quoted intraday bid-ask spreads (column 4) for high response stocks, which have a significant (at the 10% level) 1.1 ppt lower dispersion coefficient compared to low response shocks.

2.7 Conclusion

Liquidity plays an increasingly important role in asset pricing and macro finance. Yet, we lack a clear understanding of some of the most basic drivers of liquidity in informationally sensitive markets. Existing models and intuition suggest that asymmetric information destroys trading and liquidity. Though less well understood, overconfidence is generally associated with enhanced liquidity. The theory and empirics supporting these contentions are not satisfying. In particular, existing models rely heavily on exogenous noise trading, usually ignore overconfidence, and are unable to explain the empirical reality of large stock, corporate bond, and option trading volumes that are positively correlated with asymmetric information.

The disagreement literature posits that overconfidence-driven disagreement provides a rationale for trade that does not require exogenous noise traders or uncertain asset supply. I show that overconfidence is also sufficient for generating and thinking about liquidity. In my baseline model, agents differentially weight their own signals even though prices perfectly reveal the average signal. This causes them to disagree about the asset's value and trade. The market is liquid even without liquidity trading. All of this is within an intentionally

simple market setup. All agents are homogenous until receiving signals. No outside parties are needed for noise trading or market making. The same agents simultaneously serve as informed traders, noise traders, and market makers.

The baseline model rationalizes heavy trading and liquidity despite asymmetric information with no exogenous liquidity trading. The model also produces three predictions: (1) as overconfidence increases (ψ increases), trading and liquidity both increase; (2) as private information becomes more precise (τ_s increases), trading and liquidity both increase; and (3) as public uncertainty increases (τ_p decreases) trading is unaffected and liquidity decreases. Consistent with stylized facts about stocks, corporate bonds, and stock options, these predictions jointly imply that asymmetric information increases trading and to the extent that past returns increase overconfidence they also increase trading and enhance liquidity. The predictions also imply that asymmetric information shocks with the largest trading impact should have the smallest (and potentially even negative) illiquidity impact. I test this prediction in the data and find that it is true.

The baseline model's predictions are at odds with some of the recent literature on financial crises. Kacperczyk and Schnabl (2010) and Gorton and Metrick (2011) document the collapse of trade in asset backed commercial paper and repurchase agreements during the 2007-2009 financial crisis. Both of these markets previously facilitated liquidity trading in instruments that were perceived to be safe and information-insensitive. The authors reasonably argue that the market collapses were at least in part driven by increases in asymmetric information. Dang, Gorton, and Holmstrom (2009) propose a model of liquidity in which debt contracts optimally facilitate trade in part by minimizing asymmetric information. Consistent with traditional intuition, if the debt contracts become informationally sensitive trade and liquidity dry up. This narrative of the financial crisis contradicts my baseline model and is also difficult to reconcile with the liquid trade observed in equity markets despite significant asymmetric information. My general model provides a way to bridge this gap. In the face of moderate liquidity trading, adding private information to a market at first destroys liquidity by increasing the likelihood any given trade is informed.

Once most trades are already informed, further increases in private information enhance liquidity.

One aspect of disagreement trading I don't address is welfare. Overconfidence-driven disagreement clearly has some negative implications. Unequal risk sharing causes optimistic agents to hold higher variance portfolios than they would without overconfidence, which diminishes welfare under the criterion of Brunnermeier, Simsek, and Xiong (2012). On the other hand, overconfidence facilitates liquidity, which is likely beneficial. Overconfidence also makes prices more informative by causing agents to trade on their information more aggressively.¹⁹ Additional work connecting the microfoundations of liquidity and trading to their welfare implications is necessary to fully understand these trade-offs.

¹⁹Though not in my model, overconfidence likely also incentivizes gathering more information. Rubinstein (2001) makes this point and argues that irrational investors may enhance market rationality by increasing price informativeness.

Chapter 3

Is Real Interest Rate Risk Priced?

Theory and Empirical Evidence

Authored with Alexander Chernyakov

3.1 Introduction

Are expected returns related to covariance with shocks to the real riskfree interest rate? Put differently, is the real riskfree rate a priced state variable? Since Fama (1970), financial economists have understood that state variables can be priced if they are correlated with changes to (1) investor preferences or (2) the consumption-investment opportunity set.¹ Because the riskfree rate is an equilibrium outcome that is sensitive to preferences and consumption-investment opportunities, it is a prime candidate to be a priced state variable.

Previous research primarily focuses on shocks to consumption-investment opportunities. For example, Merton's (1973) Intertemporal Capital Asset Pricing Model (ICAPM) considers changing investment opportunities while holding preferences constant. Campbell (1993) follows the same approach to derive ICAPM pricing as a function of changes to expected returns. More recently, Bansal and Yaron (2004) initiated a literature on long-run consump-

¹Fama (1970) considered consumption and investment opportunities separately. In practice, these two opportunity sets are typically collapsed by considering a single homogenous consumption good.

tion growth shocks in which expectations about future consumption growth are priced. In these frameworks, positive interest rate shocks are generally good news, which makes long-duration assets valuable hedges, reducing their risk premia.

In contrast, Albuquerque, Eichenbaum, and Rebelo (2012, hereafter AER) consider preference shocks to investor patience. In their framework, positive interest rate shocks stem from impatience and are generally bad news, making long-duration assets more risky and increasing their risk premia.

We propose a model with both consumption-investment and preference shocks. Expected consumption growth and time preferences both impact interest rates, and covariance with these shocks is priced relative to the Capital Asset Pricing Model (CAPM) and the Consumption CAPM (CCAPM). However, the two types of interest rate risk carry different prices. Relative to both the CAPM and CCAPM, the price of interest rate risk associated with time preference shocks differs from the price of consumption growth interest rate risk by a factor of $\frac{-1}{\psi-1}$, where ψ is elasticity of intertemporal substitution. For $\psi > 1$, this means the two different interest rate risk premia have opposite signs. It also implies that time preference risk premia are very large when ψ is close to 1. We interpret this as evidence that calibrations with ψ close to 1 and far from the inverse of relative risk aversion represent implausible preferences.

Empirically, we estimate real interest rate shocks based on a vector autoregression (VAR) model of nominal interest rates, CPI inflation rates, and other state variables. When sorted based on interest rate exposure, stocks with high exposure have slightly lower expected returns, both on an absolute basis and relative to CAPM and Fama and French (1993) three factor model predictions. This evidence is consistent with risk premia required for time preference shocks and at odds with risk premia demanded for consumption-investment shocks. That said, the effects are modest, and the return differences are not statistically significant.

Moreover, the overall stock market appears to have very little exposure to interest rate risk. The market's interest rate news beta is an insignificant 0.11, which would carry a risk

premium of -8 bps based on our cross-sectional pricing results. This evidence contradicts the conclusion of AER that interest rate risk (valuation risk) explains the equity premium puzzle. The main difference between our empirical work and theirs is that we estimate covariance between excess returns and real interest rate shocks, whereas AER omit this moment from their GMM analysis. AER's baseline estimates imply that excess equity returns have a correlation of approximately -0.92 with interest rate shocks. We estimate this correlation as 0.05 in the data.

3.2 Theory

We consider a model with shocks to consumption growth and time preferences. Thus, the model violates both of Fama's (1970) assumption. Interest rate shocks are priced relative to the CAPM and the CCAPM. The model essentially nests the long-run risk consumption growth shocks of Bansal and Yaron (2004) with the valuation shocks of AER. The main result is that consumption growth interest rate risk has a different price than time preference interest rate risk, and the two risk premia have opposite signs when elasticity of intertemporal substitution is greater than one.

Our main results are presented and discussed below. Detailed derivations are in the appendix.

3.2.1 Setup and General Pricing Equations

Following AER, we consider a representative agent with recursive utility function:

$$U_t = \max_{C_t} \left[\lambda_t C_t^{1-1/\psi} + \delta (U_{t+1}^*)^{1-1/\psi} \right]^{1/(1-1/\psi)} \quad (3.1)$$

where C_t is consumption at time t , δ is a positive scalar capturing time discounting, ψ is elasticity of intertemporal substitution, and $U_{t+1}^* = \left\{ E_t \left[U_{t+1}^{1-\gamma} \right] \right\}^{1/(1-\gamma)}$ is the certainty equivalent of future utility with relative risk aversion of γ . The function is defined for $\psi \neq 1$ and $\gamma \neq 1$. This utility function represents standard Epstein-Zin preferences of Epstein and Zin (1991) and Weil (1989) except that time preferences are allowed to vary over time

instead of being constant. Time preferences are affected by $\frac{\lambda_{t+1}}{\lambda_t}$, which is known at time t . Using standard techniques for working with Epstein-Zin preferences, AER show that equation (3.1) implies a log stochastic discount factor of:

$$m_{t+1} = \theta \log \left(\delta \frac{\lambda_{t+1}}{\lambda_t} \right) - \frac{\theta}{\psi} \Delta c_{t+1} + (\theta - 1) r_{w,t+1} \quad (3.2)$$

where

$$\theta = \frac{1 - \gamma}{1 - 1/\psi} \quad (3.3)$$

Lower case letters signify logs. Δc_{t+1} is log consumption growth from period t to period $t + 1$. $r_{w,t+1}$ is the log return on the overall wealth portfolio. This stochastic discount factor is standard for Epstein-Zin preferences except that time discounting (δ) is augmented by $\frac{\lambda_{t+1}}{\lambda_t}$.

We assume that innovations to consumption and expected future consumption are jointly lognormal and homoskedastic. Similarly, innovations to time preferences and expected time preferences are jointly lognormal and homoskedastic. Formally,

$$E_t [c_{t+a}] = E_{t-1} [c_{t+a}] + \varepsilon_{a,t}^c \quad (3.4)$$

$$E_t [\lambda_{t+1+b}] = E_{t-1} [\lambda_{t+1+b}] + \varepsilon_{b,t}^\lambda \quad (3.5)$$

with $\left[\left\{ \varepsilon_{a,t}^c \right\}_{a>0}, \left\{ \varepsilon_{b,t}^\lambda \right\}_{b>0} \right]$ distributed jointly normally with constant variance (i.e., $cov_t \left(\varepsilon_{a,t}^c, \varepsilon_{b,t+1}^\lambda \right) = V$ for all t).² This implies that excess returns on the wealth portfolio are lognormal and homoskedastic. For simplicity, we assume that all other excess returns are lognormal as well. Lognormality and homoskedasticity simplify the model and ensure that risk premia are constant over time, focusing attention on interest rate shocks. AER specify a more restrictive stochastic process for λ_{t+1} and assume that expected consumption growth is constant over time. Similarly, Bansal and Yaron (2004) specify a more restrictive consumption growth process in their fluctuating growth rates model.³

²Note that λ_{t+1} is known one period in advance so time t shocks to λ expectations start with λ_{t+1} .

³Bansal and Yaron (2004) also consider changes to the volatility of consumption growth. We omit these shocks because they complicate the model without having a first order effect on the riskfree rate, which is our

The stochastic discount factor of equation (3.2) can be used to price all assets. In particular, it implies a riskfree rate of:

$$r_{f,t+1} = -\log \left(\delta \frac{\lambda_{t+1}}{\lambda_t} \right) + \frac{1}{\psi} E_t [\Delta c_{t+1}] - \frac{1-\theta}{2} \sigma_w^2 - \frac{\theta}{2\psi^2} \sigma_c^2 \quad (3.6)$$

and risk premia of:

$$E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2} \sigma_i^2 = \frac{\theta}{\psi} \sigma_{ic} + (1-\theta) \sigma_{iw} \quad (3.7)$$

σ_w^2 is the variance of excess returns to the wealth portfolio. $\sigma_c^2 = \text{var}_t \left(\varepsilon_{0,t+1}^c \right)$ is consumption variance relative to expectations last period. σ_{ic} is covariance of asset i 's return with current consumption shocks. σ_{iw} is covariance of asset i 's return with wealth portfolio returns. $\frac{1}{2} \sigma_i^2$ is a Jensen's inequality correction for expected log returns using variance of asset i 's return. From equations (3.6) and (3.7), it is clear that the real riskfree interest rate changes over time in response to time preferences ($\frac{\lambda_{t+1}}{\lambda_t}$) and expected consumption growth ($E_t [\Delta c_{t+1}]$) and that risk premia are constant over time.

3.2.2 Substituting out Consumption (The ICAPM)

Following Campbell (1993), we log-linearize the representative agent's budget constraint ($W_{t+1} = R_{w,t+1} (W_t - C_t)$) to yield:

$$r_{w,t+1} - E_t [r_{w,t+1}] = (E_{t+1} - E_t) \sum_{j=0}^{\infty} \rho^j \Delta c_{t+1+j} - (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{w,t+1+j} \quad (3.8)$$

where ρ is a log-linearization constant.⁴ Because risk premia are constant over time, $\text{News}_{h,t+1} = (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{w,t+1+j}$ depends solely on changes to expected interest rates, which change over time in response to time preferences and expected consumption growth as described by equation (3.6).⁵ We use the budget constraint (equation 3.8) and the riskfree

focus.

⁴Specifically, $\rho = 1 - \exp(\overline{c-w})$ where $\overline{c-w}$ is the average log consumption-wealth ratio. We use a monthly coefficient value of $\rho = 0.996$ in our analysis.

⁵The h subscript follows the notation of Campbell (1993) to indicate hedging of future interest rates.

rate decomposition (equation 3.6) to substitute out current consumption covariance from the risk premia in equation (3.7).

These substitutions yield the following ICAPM:

$$E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2}\sigma_i^2 = \gamma\sigma_{iw} + (\gamma - 1)\sigma_{ih(c)} - \frac{\gamma - 1}{\psi - 1}\sigma_{ih(\lambda)} \quad (3.9)$$

Risk premia are determined by covariance with the market and covariance with state variables related to future interest rates. $\sigma_{ih(c)}$ is covariance with consumption growth shocks to future interest rates. $\sigma_{ih(\lambda)}$ is covariance with time preference shocks to future interest rates. Together, they add up to covariance with overall interest rate news. I.e.,

$$\begin{aligned} \sigma_{ih} &\equiv cov_t \left(r_{i,t+1}, (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{f,t+1+j} \right) \\ &= \sigma_{ih(c)} + \sigma_{ih(\lambda)} \end{aligned} \quad (3.10)$$

The risk prices in equation (3.9) are revealing. Market return risk (σ_{iw}) is priced by relative risk aversion (γ) as in other ICAPM models. Also consistent with other ICAPM models, state variable covariance ($\sigma_{ih(c)}$ and $\sigma_{ih(\lambda)}$) is priced only if $\gamma \neq 1$. Yet, the two components of interest rate risk have different prices. Whereas $\sigma_{ih(c)}$ is priced by $\gamma - 1$, $\sigma_{ih(\lambda)}$ is priced by $-\frac{\gamma-1}{\psi-1}$. When $\psi > 1$, the prices have opposite signs, and if ψ is close to 1, time-preference risk is amplified relative to consumption growth risk. The key distinction between equation (3.9) and previous ICAPM models like Campbell (1993) is that we consider shocks to both consumption growth and time preferences. Because Campbell assumes constant preferences, he omits $\sigma_{ih(\lambda)}$ and treats σ_{ih} as equivalent to $\sigma_{ih(c)}$.

3.2.3 Substituting out Wealth Returns (The Generalized CCAPM)

The budget constraint (equation 3.8) can also be used to substitute out covariance with wealth portfolio returns to express risk premia in terms of a generalized CCAPM along the

lines of Bansal and Yaron's (2004) long run risk model. The resulting pricing equation is:

$$E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2}\sigma_i^2 = \gamma\sigma_{ic} + (\gamma\psi - 1)\sigma_{ih(c)} - \frac{\gamma\psi - 1}{\psi - 1}\sigma_{ih(\lambda)} \quad (3.11)$$

Consumption risk (σ_{ic}) is priced by relative risk aversion (γ) as in the standard CCAPM. Consistent with Bansal and Yaron (2004), interest rate risk is only priced if $\gamma \neq 1/\psi$.⁶ I.e., interest rate risk is priced under general Epstein-Zin preferences, but not under power utility. As in our ICAPM, the most striking thing about equation (3.11) is that the two types of interest rate risk are priced differently. Once again, time preference interest rate risk differs from consumption growth interest rate risk by a factor of $\frac{-1}{\psi-1}$.

Our ICAPM (equation 3.9) and generalized CCAPM (equation 3.11) are at odds with traditional reasoning about interest rate risk. If one considers only consumption growth shocks, positive interest rate shocks are good news for investors under typical parameter assumptions ($\gamma > 1$ for the ICAPM and $\gamma > 1/\psi$ for the CCAPM). Thus, assets that positively covary with interest rate shocks are risky and require extra risk premia relative to CAPM and CCAPM pricing. Campbell and Viceira (2003, Chapter 3) use this logic to argue that long term bonds are valuable hedges against interest rate decreases. If $\psi > 1$ and $\frac{1}{\psi-1}\sigma_{ih(\lambda)}$ dominates $\sigma_{ih(c)}$, the logic actually goes the opposite way. Investors want to hedge against interest rate *increases*, making long term assets (including bonds) risky investments.

3.2.4 Disciplining Parameter Values

The case of elasticity of intertemporal substitution close to one deserves special attention.⁷ In both the ICAPM (equation 3.9) and generalized CCAPM (equation 3.11), the price of time preference risk ($\sigma_{ih(\lambda)}$) is scaled by a factor of $\frac{-1}{1-\psi}$. When ψ is close to 1, these risk prices can have arbitrarily large magnitudes. Are infinite (or even very large) premia for time preference risk plausible? We believe they are not, and we interpret this as evidence

⁶Bansal and Yaron (2004) express their version of equation (3.11) in terms of future consumption growth. This is just a different way of describing the same relationship.

⁷Because Epstein-Zin preferences in equation (3.1) are not defined for $\psi = 1$ or $\gamma = 1$, we do not consider the case where ψ exactly equals 1.

that ψ must be close to $1/\gamma$ or far from 1.

Before assessing the plausibility of high time preference risk premia, it is important to understand why the premia are high when ψ is close to 1. Under Epstein-Zin preferences, current utility flows are roughly $\lambda_t C_t^{1-1/\psi}$. When ψ is close to 1, these flows are much more sensitive to λ_t than C_t . Yet, the riskfree rate (equation 3.6) is equally sensitive to consumption growth and time preference changes when ψ is near 1. Thus, the hedging premium for time preference risk blows up relative to the hedging premium for consumption growth.

Another way to see this is to change notation to consider time preference shocks in the same units as consumption. Specifically, consider augmented consumption, defined as:

$$\tilde{C}_t \equiv \lambda_t^* C_t \quad (3.12)$$

where

$$\lambda_t^* \equiv \lambda_t^{1/(1-1/\psi)} \quad (3.13)$$

With this notation change, equation (3.1) is transformed into standard Epstein-Zin preferences with respect to augmented consumption. All of Campbell's (1993) and Bansal and Yaron's (2004) results hold with respect to augmented consumption and returns measured in units of augmented consumption. In particular, the augmented riskfree rate is:

$$\tilde{r}_{f,t+1} = -\log(\delta) + \frac{1}{\psi} E_t [\Delta \tilde{c}_{t+1}] - \frac{1-\theta}{2} \sigma_w^2 - \frac{\theta}{2\psi^2} \sigma_c^2 \quad (3.14)$$

and the risk premium for any asset is given by

$$E_t [\tilde{r}_{i,t+1}] - \tilde{r}_{f,t+1} + \frac{1}{2} \sigma_i^2 = \gamma \sigma_{iw} + (\gamma - 1) \sigma_{ih(\tilde{c})} \quad (3.15)$$

where tildas represent augmented consumption and returns. Using the identities $\tilde{r}_{i,t+1} = r_{i,t+1} + \frac{1}{1-1/\psi} \log\left(\frac{\lambda_{t+1}}{\lambda_t}\right)$ and $\Delta \tilde{c}_{t+1} = \Delta c_{t+1} + \frac{1}{1-1/\psi} \log\left(\frac{\lambda_{t+1}}{\lambda_t}\right)$, equations (3.14) and (3.15) are equivalent to equations (3.6) and (3.9). The time preference risk premia in equations (3.9) and (3.11) blow up as ψ gets close to 1 because time preferences (λ_t) have an outsized impact on augmented consumption through $\lambda_t^* = \lambda_t^{1/(1-1/\psi)}$.

If one accepts that time preference risk premia cannot be infinite, equations (3.9) and

(3.11) rule ψ that are too close to 1. To generate better intuition for how close ψ can be to 1, we propose a thought experiment with simple consumption and time preference processes. Specifically, consider a three period economy with constant perishable consumption endowments of $C_0 = C_1 = C_2 = C$ in each period. Time preferences are known in advance for periods 0 and 1. For simplicity we assume $\lambda_0 = \lambda_1 = 1$ and we also assume $\delta = 1$. The only uncertainty in the economy is period 2 time preferences, which are revealed at time 1. λ_2 takes on two possible values, λ_H or λ_L with probabilities π_H and π_L , respectively. We want to know how the representative agent values wealth in state L relative to state H .

In the appendix, we derive Arrow-Debreu state prices for the two states and find that their ratio is:

$$\frac{P_L}{P_H} = \frac{\pi_L}{\pi_H} \left(\frac{1 + \lambda_L}{1 + \lambda_H} \right)^{-\frac{\gamma-1/\psi}{1-1/\psi}} \quad (3.16)$$

Note that these are prices at time 0 for state-contingent payoffs at time 1. Under power utility with $\gamma = 1/\psi$, the price ratio is simply the probability ratio. This is exactly what we should expect. With power utility, marginal utility of wealth is pinned down by consumption and current time preferences, which is constant across states. By contrast, state prices are highly sensitive to future time preferences when $1/\psi$ differs from γ and is close to 1. We do not have great intuition for whether $-\frac{\gamma-1/\psi}{1-1/\psi}$ should be positive or negative, but we believe its magnitude should be small.

To be more concrete, assume $\pi_L = \pi_H = 0.5$, $\lambda_H = 1$, and $\lambda_L = 0.9$. Table 3.1 presents the equation (3.16) state price ratio for these parameters at various values of γ and ψ . Parameterizations with $\gamma > 1$ are in Panel A. Parameterizations with $\gamma < 1$ are in Panel B. The upward sloping diagonals of 1's in both panels represent power utility with $\gamma = 1/\psi$.

What are reasonable values for $\frac{P_L}{P_H}$? The thought experiment is what you would pay for an extra dollar in a state in which time preferences will soon fall versus an extra dollar in a state in which time preferences will remain constant, keeping in mind that current and future consumption are the same in both states. As a starting point, we propose that it is difficult to rationalize state price ratios larger in magnitude than the ratio of the time preference shock itself. In Table 3.1, ratios between 0.95 and 1.05 are in bold italics, and

Table 3.1: State Price Ratios

This table displays state price ratios from equation (16) at different values of relative risk aversion (RRA) and elasticity of intertemporal substitution (EIS).

A. RRA > 1									
EIS	Relative Risk Aversion								
	1.01	1.10	1.25	1.5	2	3	5	10	25
0.04	1.05	1.05	1.05	1.05	1.05	1.05	1.04	1.03	1.00
0.10	1.05	1.05	1.05	1.05	1.05	1.04	1.03	1.00	0.92
0.20	1.05	1.05	1.05	1.05	1.04	1.03	1.00	0.94	0.77
0.33	1.05	1.05	1.05	1.04	1.03	1.00	0.95	0.84	0.57
0.50	1.05	1.05	1.04	1.03	1.00	0.95	0.86	0.66	0.31
0.67	1.05	1.04	1.03	1.00	0.95	0.86	0.70	0.42	0.09
0.80	1.05	1.03	1.00	0.95	0.86	0.70	0.46	0.17	<.01
0.91	1.05	1.00	0.93	0.81	0.63	0.38	0.14	0.01	<.01
0.99	1.00	0.63	0.29	0.08	<.01	<.01	<.01	<.01	<.01
1.01	1.11	1.77	3.84	14.04	>100	>100	>100	>100	>100
1.10	1.06	1.11	1.21	1.40	1.85	3.25	10.06	>100	>100
1.25	1.06	1.08	1.12	1.20	1.36	1.76	2.94	10.59	>100
1.5	1.05	1.07	1.09	1.14	1.23	1.43	1.95	4.20	42.28
2	1.05	1.06	1.08	1.11	1.17	1.29	1.59	2.65	12.35
3	1.05	1.06	1.07	1.09	1.14	1.23	1.43	2.10	6.67
5	1.05	1.06	1.07	1.09	1.12	1.20	1.36	1.87	4.90
10	1.05	1.06	1.07	1.08	1.11	1.18	1.32	1.76	4.13
25	1.05	1.06	1.07	1.08	1.11	1.17	1.30	1.70	3.79

B. RRA < 1									
EIS	Relative Risk Aversion								
	0.04	0.10	0.20	0.33	0.50	0.67	0.80	0.91	0.99
0.04	1.05	1.05	1.05	1.05	1.05	1.05	1.05	1.05	1.05
0.10	1.06	1.06	1.06	1.06	1.06	1.05	1.05	1.05	1.05
0.20	1.07	1.06	1.06	1.06	1.06	1.06	1.06	1.05	1.05
0.33	1.08	1.08	1.07	1.07	1.07	1.06	1.06	1.06	1.05
0.50	1.11	1.10	1.10	1.09	1.08	1.07	1.06	1.06	1.05
0.67	1.16	1.15	1.14	1.13	1.11	1.09	1.07	1.06	1.05
0.80	1.28	1.27	1.24	1.21	1.17	1.13	1.10	1.07	1.05
0.91	1.72	1.67	1.59	1.48	1.36	1.25	1.17	1.10	1.06
0.99	>100	>100	63.74	32.16	13.68	5.82	2.94	1.68	1.11
1.01	<.01	<.01	0.02	0.03	0.08	0.19	0.37	0.66	1.00
1.10	0.61	0.63	0.67	0.72	0.79	0.87	0.94	1.00	1.05
1.25	0.82	0.84	0.86	0.89	0.93	0.97	1.00	1.03	1.05
1.5	0.91	0.92	0.93	0.95	0.97	1.00	1.02	1.04	1.05
2	0.95	0.96	0.97	0.98	1.00	1.02	1.03	1.04	1.05
3	0.98	0.98	0.99	1.00	1.01	1.03	1.04	1.05	1.05
5	0.99	0.99	1.00	1.01	1.02	1.03	1.04	1.05	1.05
10	1.00	1.00	1.01	1.01	1.02	1.03	1.04	1.05	1.05
25	1.00	1.00	1.01	1.02	1.02	1.03	1.04	1.05	1.05

ratios between 0.9 and 1.1 are highlighted in italics.⁸ As expected, ratios in these ranges require $1/\psi$ to be close to γ or far from 1. For example, if γ is 5, ψ must be less than 0.44. With lower relative risk aversion, ψ can be closer to one without posing a problem.

Researchers frequently calibrate models with parameters that imply implausible state price ratios. For example, Bansal and Yaron (2004) calibrate their model with relative risk aversion of $\gamma = 7.5$ and $\gamma = 10$ and elasticity of intertemporal substitution of $\psi = 1.5$. These parameter assumptions imply a state price ratios of 2.9 (for $\gamma = 7.5$) and 4.2 (for $\gamma = 10$). By comparison, AER's benchmark calibration of $\gamma = 1.0684$ and $\psi = 1.0275$ implies a somewhat high but much more plausible price ratio of 1.2.

Importantly, our claim is not just that ψ cannot be close to 1 and far from $1/\gamma$ in a model with time preference shocks. Rather, it is that ψ cannot be close to 1 and far from $1/\gamma$ in *any* model. Calibrations of ψ and γ need to reflect actual preferences,⁹ and one aspect of those preferences is how agents value covariance with (real or hypothetical) time preference shocks. Our argument is similar in spirit to Epstein, Farhi, and Strzalecki's (2013) claim that ψ significantly greater than $1/\gamma$ (e.g., as calibrated by Bansal and Yaron, 2004) implies agents are willing to pay an implausibly large premium in order to resolve risk earlier.

3.3 Empirical Analysis

Our empirical focus is not to test the model discussed in the previous section but rather to directly address the question of whether real interest rate risk is priced. This question is actually a bit at odds with the model in that it implies a single type of interest rate risk whereas the model shows that there are two different interest rate factors with different risk prices. Ideally, we would like to separately measure consumption growth and time

⁸The broader range requires that $\frac{P_L \pi_H}{P_H \pi_L}$ falls between $\left(\frac{\lambda_L}{\lambda_H}\right)$ and $\left(\frac{\lambda_L}{\lambda_H}\right)^{-1}$. The narrower range requires that $\frac{P_L \pi_H}{P_H \pi_L}$ falls between $\left(\frac{1+\lambda_L}{1+\lambda_H}\right)$ and $\left(\frac{1+\lambda_L}{1+\lambda_H}\right)^{-1}$, which is equivalent to the condition that $|\gamma - 1/\psi| \leq |1 - 1/\psi|$.

⁹If one relaxes the requirement that calibrations represent reasonable preferences, the equity premium puzzle is easy to solve. Simply assume that relative risk aversion is extremely high. The whole point of the equity premium puzzle is that conventional models cannot explain the equity premium without implausible risk aversion. Introducing implausible Epstein-Zin preferences is not a solution to this problem.

preference interest rate risk. Given the unobservability of time preferences and the imprecise and low-frequency nature of consumption data, measuring aggregate interest rate risk is probably the best we can do. Moreover, aggregate interest rate risk is of direct interest because interest rates are highly visible and economically important. Even though we don't directly test it, the model does inform how we think about and measure interest rate risk. Perhaps most significantly, the model predicts that investors care about shocks to both current and expected future riskfree interest rates. Thus, instead of considering just $cov_t(r_{i,t+1}, r_{f,t+2} - E_t[r_{f,t+2}])$, we focus on $\sigma_{ih} \equiv cov_t(r_{i,t+1}, (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{w,t+1+j})$.

Our empirical work faces two primary challenges. First, our focus is on real interest rates. This is the riskfree rate in our model, and it is the relevant quantity for actual economic decisions. Unfortunately, real interest rates are not directly observed. We overcome this problem by modeling expected Consumer Price Index (CPI) inflation and estimating monthly real interest rates as the difference between nominal 1-month Treasury bill interest rates and expected inflation over the next month. For our baseline estimates, we focus on the 1983 to 2012 time period because monetary policy has been more consistent and inflation has been less volatile during the Greenspan and Bernanke Federal Reserve chairmanships than in previous periods.

Our second empirical challenge is that interest rate risk involves shocks to expectations. Thus, we need to estimate interest rate expectations. We do this with a vector autoregression (VAR) of interest rates, inflation, and other state variables. From the VAR, we extract an estimate for the time series of $(E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{f,t+1+j}$ innovations, which we in turn use to estimate σ_{ih} for various assets.

3.3.1 Vector Autoregression

Our VAR model is:

$$Y_t = AY_{t-1} + \omega_t \quad (3.17)$$

Y_t is a $k \times 1$ vector with the nominal 1-month treasury bill log yield and seasonally adjusted log CPI inflation over the past month as its first two elements. The remaining elements of Y_t

are state variables useful for forecasting these two variables. The assumption that the VAR model has only one lag is not restrictive because lagged variables can be included in Y_t . We demean Y_t before estimating the VAR to avoid the need for a constant in equation (3.17).

We define vector ei to be the i th column of a $k \times k$ identity matrix. Using this notation we can extract expectations and shocks to current and future expectations from Y_t , A , and ω_t . Our interest is in the real riskfree interest rate, which we estimate as the nominal 1-month treasury bill yield less expected inflation:

$$\widehat{r_{f,t+1}} = (e1' - e2'A) Y_t \quad (3.18)$$

Similarly, expected future riskfree rates are:

$$E_t [\widehat{r_{f,t+j}}] = (e1' - e2'A) A^{j-1} Y_t \quad (3.19)$$

Shocks to current and expected riskfree rates are:

$$(E_{t+1} - E_t) \widehat{r_{f,t+1+j}} = (e1' - e2'A) A^{j-1} \omega_{t+1} \quad (3.20)$$

Most importantly, total interest rate news is:

$$\begin{aligned} News_{h,t+1} &= (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \widehat{r_{f,t+1+j}} \\ &= (e1' - e2'A) \sum_{j=1}^{\infty} \rho^j A^{j-1} \omega_{t+1} \\ &= (e1' - e2'A) \rho (I - \rho A)^{-1} \omega_{t+1} \end{aligned} \quad (3.21)$$

where I is the identity matrix.

All that remains is to choose state variables for Y_t and estimate equation (3.17). Following Campbell (1996), we include the relative treasury bill rate, defined as the difference between the current one-month treasury bill yield and the average one-month treasury bill yield over the previous 12 months. Similarly, we include the relative monthly CPI inflation rate, defined the same way. Next, we include the yield spread between 10-year treasury bonds and 3-month treasury bonds because the slope of the yield curve is known to predict

interest rate changes. Finally, we include the CRSP value-weighted market return and the log dividend-price ratio (defined as dividends over the past year divided by current price), which is known to predict market returns. These variables are useful to the extent that equity returns are related to expected future interest rates. We considered including additional lags of these variables by re-estimating equation (3.17) with multiple lags of Y_t . The Bayesian Information Criteria is insensitive to adding lags so we do not include lagged variables in Y_t .

Table 3.2 shows coefficient estimates and standard errors for the elements of A related to predicting nominal interest rates and inflation. Columns (1) and (2) report results for the 1983 to 2012 time period, which is our primary focus. Nominal interest rate shocks are highly persistent with lag coefficient of 0.96. Inflation shocks are much less persistent and only have a lag coefficient of 0.07. Inflation is increasing in lagged nominal yields. The VAR explains 95% of the variation in nominal yields over time. Inflation changes are less predictable with an R-squared of 0.24.

Because our main interest is in the riskfree rate, we plot $\widehat{r_{f,t+1}}$ in Figure 3.1. Along with

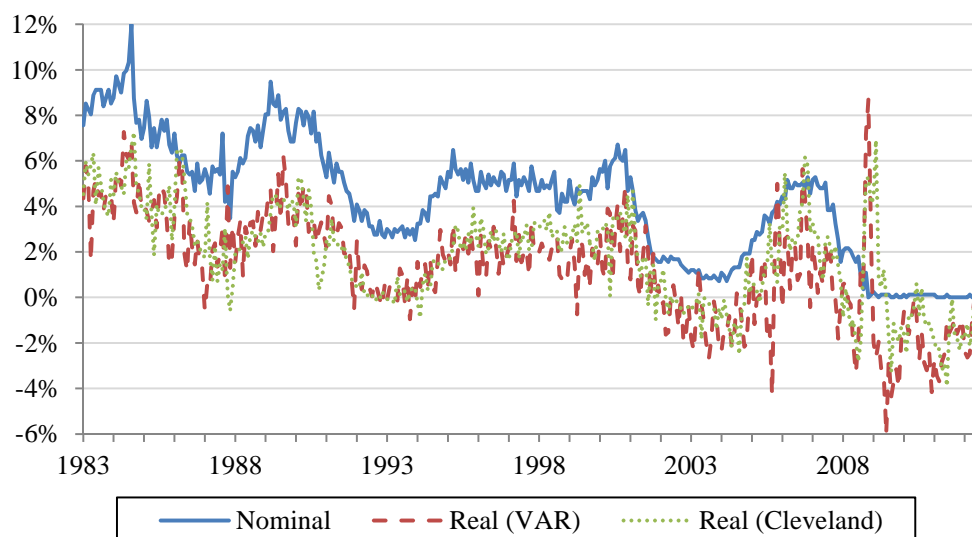


Figure 3.1: *Riskfree Rate, 1983-2012*

The nominal riskfree rate is the yield on a one-month nominal treasury bill. The real risk free rate is estimated using our VAR analysis. We also report the real riskfree rate estimated by the Federal Reserve Bank of Cleveland.

Table 3.2: VAR Results

y1 is the nominal log yield on a one-month treasury bill. Inflation is one-month log inflation. Relative y1 and relative inflation are the difference between current yields and inflation and average values over the past twelve months. y120 - y3 is the yield spread between 10-year and 3-month treasury bonds. rmrf is the excess return of the CRSP value weighted market return over the risk free rate. d - p is the log dividend-price ratio, calculated for the CRSP value-weighted market index using current prices and average dividends over the past twelve months. Results are for a 1-lag VAR of demeaned y1, inflation, relative y1, relative inflation, rmrf, and d-p. Coefficients for dependent variables y1 and inflation are reported. The other dependent variables are omitted for brevity. Bootstrapped standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

	1983-2012		1927-2012	
	(1) y1	(2) inflation	(3) y1	(4) inflation
Lagged Variables				
y1	0.9639*** (0.0202)	0.1939* (0.1003)	0.9741*** (0.0116)	0.0631 (0.0773)
inflation	0.0314 (0.0297)	0.0737 (0.1734)	0.0102* (0.0062)	0.7762*** (0.0709)
relative y1	-0.0976** (0.0457)	0.1295 (0.1585)	-0.1752*** (0.0407)	0.5909*** (0.1599)
relative inflation	-0.0136 (0.0281)	0.3268* (0.1767)	-0.003 (0.0056)	-0.4554*** (0.0837)
y120 - y3	-0.0032 (0.0036)	-0.002 (0.0155)	-0.0062** (0.0024)	0.0014 (0.0122)
rmrf	0.0013* (0.0007)	0.0083* (0.0042)	0.0008** (0.0004)	0.0061* (0.0034)
d - p	0.0001 (0.0001)	0.0002 (0.0005)	0.0000 (0.0000)	-0.0002 (0.0003)
R-Squared	0.95	0.24	0.95	0.32

our estimated real riskfree rate, we also plot the nominal one-month treasury bill yield and the Federal Reserve Bank of Cleveland's real riskfree rate estimate.¹⁰ As we would expect in a stable inflation environment, real interest rates generally follow the same pattern as nominal interest rates. Nonetheless, inflation expectations do change over time, particularly over the past few years. Our real riskfree rate estimate closely tracks the Federal Reserve Bank of Cleveland's estimate, which increases our confidence in our methodology.

As a robustness check, we also estimate real riskfree rates and real riskfree rate news over a longer time period, starting in 1927. Our methodology for the longer time period is the same as before except that we use the unadjusted CPI because the seasonally adjusted CPI is only available starting in 1947. Columns (3) and (4) of Table 3.2 report the VAR results. In the extended time sample, inflation shocks are more persistent (inflation's lagged coefficient is 0.78, compared to 0.07 before). The results are otherwise similar to the original VAR. Figure 3.2 plots nominal and estimated real interest rates from 1927 to 2012. Expected inflation varies more in the extended sample than it does after 1983. Thus, the real and

¹⁰The Federal Reserve Bank of Cleveland's real riskfree rate estimates are described by Haubrich, Pennacchi, and Ritchken (2008, 2011).

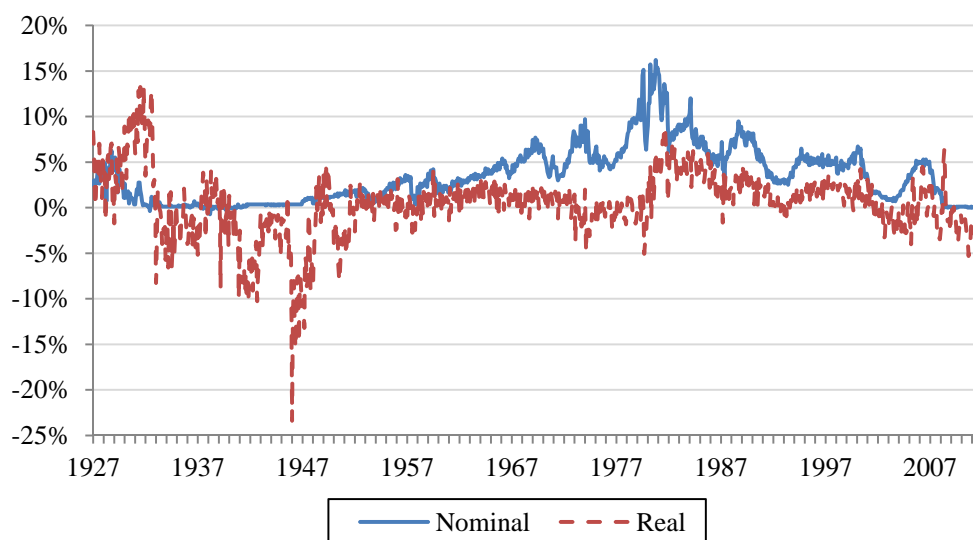


Figure 3.2: *Riskfree Rate, 1927-2012*

The nominal riskfree rate is the yield on a one-month nominal treasury bill. The real risk free rate is estimated using our VAR analysis.

nominal interest rates do not track each other as closely. Expected inflation is particularly high in the 1930's, 1940's, and 1970's, and deflation caused real interest rates to exceed nominal interest rates in the 1920's.

3.3.2 Cross-Sectional Equity Pricing

If real interest rate risk is priced and stocks vary in their exposure to real interest rate risk, real interest rate risk should be priced in the cross section of stock returns. This is not the first paper to connect time series interest rate changes with cross-sectional stock returns. For example, Fama and French (1993) find comovement between excess stock returns and excess returns on long term bonds but conclude that bond factors have little impact on cross sectional stock prices. Petkova (2006) finds that innovations to term spreads and one month nominal interest rates are correlated with and partially explain size and value returns. Kojen, Lustig, and Van Nieuwerburgh (2012) find that high returns to value stocks relative to growth stocks are explained by covariance with shocks to nominal bond risk premia whereas returns to treasury bond portfolios of different maturities are largely explained by differential exposure to the level of interest rates. Our empirical analysis differs from previous studies because we focus specifically on stock exposure to real interest rate innovations. Moreover, we sort stocks based on this exposure instead of focusing on established size and value returns.

To test whether interest rate risk is priced we sort stocks into portfolios according to covariance with interest rate news ($News_{h,t+1}$). Specifically, we estimate $\sigma_{ih} = cov_t(r_{i,t+1}, News_{h,t+1})$ on a rolling basis for all NYSE, AMEX, and NASDAQ common stocks using returns and VAR $News_h$ estimates over the past three years, with the requirement that included stocks must have at least two years of historical data. Value-weighted decile portfolios are formed monthly by sorting stocks according to those estimates.

Table 3.3 reports market capitalization, average excess returns, and $\beta_{ih} = \frac{\sigma_{ih}}{\sigma_h^2}$ estimates for each portfolio. The table also reports pricing errors (alphas) relative to the CAPM and Fama and French (1993) three factor model and factor loadings (betas) for the three factor

Table 3.3: Real Riskfree Rate News Covariance Deciles

Value-weighted decile portfolios are formed at the end of each month by sorting stocks based on covariance with riskfree rate news over the past three years. The table reports betas with respect to riskfree rate news, average size, and average excess returns for each portfolio. The table also reports results for time series regressions of excess returns on excess market returns (the CAPM regression) and excess market returns, the Fama-French size factor (smb), and the Fama-French value factor (hml) (the 3 Factor regression). Standard errors for the 10-1 portfolio difference are reported in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance. The sample is NYSE, AMEX, and NASDAQ common stocks.

A. 1985-2012

Decile	Rf News	Market Cap (\$B)	Excess Return	CAPM Alpha	3 Factor Alpha	Factor Loadings (Betas)		
	Beta					rmrf	smb	hml
1	-0.17	0.72	0.63%	-0.19%	-0.16%	1.27	0.61	-0.06
2	0.07	1.36	0.94%	0.24%	0.30%	1.10	0.22	-0.15
3	-0.04	1.94	0.87%	0.25%	0.23%	1.04	0.07	0.04
4	0.13	2.42	0.65%	0.06%	0.03%	1.00	-0.04	0.09
5	0.00	2.74	0.51%	-0.03%	-0.05%	0.94	-0.10	0.03
6	0.02	2.76	0.48%	-0.06%	-0.08%	0.93	-0.14	0.05
7	0.03	2.58	0.54%	-0.02%	-0.04%	0.97	-0.11	0.03
8	0.15	2.21	0.68%	0.06%	0.08%	1.04	-0.13	-0.07
9	0.14	1.69	0.61%	-0.06%	-0.04%	1.10	0.01	-0.06
10	0.41	0.85	0.21%	-0.62%	-0.44%	1.21	0.55	-0.47
10-1	0.58** (0.23)	0.13** (0.06)	-0.42% (0.33%)	-0.42% (0.34%)	-0.27% (0.34%)	-0.06 (0.08)	-0.07 (0.11)	-0.41*** (0.12)

B. 1929-2012

Decile	Rf News	Market Cap (\$B)	Excess Return	CAPM Alpha	3 Factor Alpha	Factor Loadings (Betas)		
	Beta					rmrf	smb	hml
1	-0.01	0.17	0.66%	-0.05%	-0.12%	1.15	0.52	-0.03
2	0.00	0.48	0.66%	0.04%	0.03%	1.04	0.20	-0.06
3	0.03	0.69	0.70%	0.13%	0.12%	0.99	0.08	-0.01
4	0.06	0.86	0.71%	0.15%	0.15%	0.96	0.02	0.00
5	0.01	0.98	0.60%	0.04%	0.02%	0.97	-0.03	0.06
6	0.03	1.05	0.56%	-0.01%	-0.03%	0.98	-0.03	0.09
7	0.06	1.08	0.58%	-0.01%	-0.02%	1.03	-0.08	0.08
8	0.06	1.05	0.56%	-0.07%	-0.10%	1.08	0.00	0.11
9	0.10	0.83	0.61%	-0.07%	-0.12%	1.15	0.04	0.17
10	0.11	0.38	0.58%	-0.18%	-0.27%	1.23	0.50	0.03
10-1	0.13 (0.09)	0.21*** (0.02)	-0.09% (0.18%)	-0.13% (0.18%)	-0.14% (0.18%)	0.07** (0.03)	-0.02 (0.06)	0.05 (0.05)

model. Panel A reports results for our baseline 1985-2012 time period.¹¹ Riskfree rate news betas increase across the portfolios, and decile 10's news beta is a significant 0.58 higher than decile 1's news beta. Monthly excess returns are 42 bps lower in the 10th decile than in the 1st decile, but this return difference is not statistically significant, and there is no clear pattern to excess returns across the decile portfolios other than a drop in returns in decile 10. CAPM and 3 Factor alphas follow the same basic pattern. Factor loadings are also similar across the portfolios. The one exception is that decile 10 has a large negative loading on the value factor (*hml*). The bottom line is that there is no evidence that interest rate risk is priced in the cross section of equities.

Results are similar in the extended 1929-2012 sample, reported in Panel B. Once again, average excess returns and alpha estimates decrease with interest rate news exposure, but the differences are not significant. The most striking difference between Panel A and Panel B is that β_{ih} differences across the portfolios are not significant in the extended sample. This suggests that stock-level interest rate risk was not stable over time early in the sample, undercutting our ability to form interest rate risk portfolios. This problem appears to be concentrated in the first few decades of the sample when inflation and interest rates were most volatile. In later analysis, we examine a 1952 to 2012 sample and find significant β_{ih} differences between the decile portfolios. As in the other samples, these β_{ih} differences are not accompanied by significant return differences.

3.3.3 Equity Premium

Because the market portfolio is a claim to future dividends, it may be exposed to interest rate risk. Thus, interest rate risk may affect expected equity returns and could explain part of the equity premium puzzle. The magnitude and direction of this effect depend on the market return's covariance with interest rate news and the price of interest rate risk.

AER make the extreme claim that interest rate risk explains virtually all of the equity

¹¹We form the portfolios based on at least two years of historical data, which causes the sample to start in 1985 instead of 1983.

premium. In their model, assets are priced based on covariance with consumption growth shocks and time preference shocks, which map directly into interest rate shocks. Consistent with previous studies, they estimate that equity returns are essentially uncorrelated with consumption growth. Thus, their explanation of the equity premium is almost entirely based on interest rate risk. Equities are risky because they have a long duration and are sensitive to persistent real interest rate shocks. Duration simultaneously explains the upward sloping yield curve and the equity premium. In the AER benchmark model, equity returns are highly sensitive to interest rate shocks, with a correlation of approximately -0.92. Moreover, their benchmark model implies that equity returns have an interest rate news beta of -1.¹²

Using our estimates of interest rate news, we can directly measure these two moments. Panel A of Table 3.4 shows results for the 1985 to 2012 time period. Excess market returns (*rmrf*) have a correlation of 0.05 and a beta of 0.11 with respect to interest rate news. These estimates are close to zero, suggesting that equity returns have little exposure to interest rate risk. According to the point estimate, the market return is positively correlated with interest rate shocks, consistent with long run consumption growth shocks and in contrast to AER's time preference shocks.

Table 3.4 also reports interest rate correlations and betas for the long-short decile 10 minus decile 1 interest rate risk portfolio and for 1 to 2 year and 5 to 10 year bonds.¹³ By construction, the long-short interest rate risk portfolio has a positive beta. The bond portfolios have negative exposures to interest rate news. However, these exposures are small. Interest rate betas are -0.04 for both portfolios, and the beta is only significantly different from zero for the short-term bonds.

The final rows of Table 3.4 report average excess returns and average excess returns divided by interest rate news beta. If interest rate news is the primary risk factor investors care about, this ratio (the implied price of beta) should be consistent across assets. The point

¹²The high negative correlation comes from AER's Table 3 estimate that interest rate shocks are relatively large and persistent while dividend variance is low. The beta of -1 is implied by AER's benchmark assumption that real dividend growth is independent of real interest rates.

¹³Bond return data is from CRSP.

Table 3.4: Equity Market and Bond Real Interest Rate Risk

rmrf is the excess return on the CRSP value weighted market portfolio. Decile 10-1 is returns to long-short portfolio representing the difference between the 10th and first riskfree rate news covariance portfolios, described in Table 2. 1-2 and 5-10 year bonds represent excess returns to treasury bonds of those durations, as calculated by CRSP. Correlations and betas with respect to riskfree rate news and average returns are reported for each return series. The price of beta is defined as average returns divided by beta. Standard errors are reported in parentheses. Standard errors for the price of beta are calculated using the delta method. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

<i>A. 1985-2012</i>				
	rmrf	Decile 10-1	1-2 Year Bonds	5-10 Year Bonds
Rf News Correlation	0.04 (0.05)	0.14** (0.05)	-0.14*** (0.05)	-0.03 (0.05)
Rf News Beta	0.11 (0.17)	0.58** (0.23)	-0.04*** (0.02)	-0.04 (0.06)
Average Excess Returns	0.60%** (0.25%)	-0.42% (0.33%)	0.12%*** (0.02%)	0.34%*** (0.09%)
Price of Beta	5.35% (10.57%)	-0.72%** (0.30%)	-3.14%*** (0.64%)	-9.70% (13.81%)
<i>B. 1952-2012</i>				
	rmrf	Decile 10-1	1-2 Year Bonds	5-10 Year Bonds
Rf News Correlation	0.05 (0.04)	0.12*** (0.04)	-0.40*** (0.03)	-0.12*** (0.04)
Rf News Beta	0.10 (0.08)	0.30*** (0.09)	-0.12*** (0.01)	-0.10*** (0.03)
Average Excess Returns	0.55%*** (0.16%)	-0.16% (0.19%)	0.09%*** (0.02%)	0.16%*** (0.06%)
Price of Beta	5.43% (5.91%)	-0.54% (0.46%)	-0.72%*** (-0.12%)	-1.57%*** (-0.13%)

estimates clearly differ. In particular, the bond returns and cross-sectional interest rate risk portfolio imply a negative price of interest rate risk whereas market returns imply a positive price. Unfortunately, betas and average returns are measured too imprecisely to definitively rule out consistent interest rate risk pricing across the assets.

Panel B of Table 3.4 reports the same statistics for a longer sample period, starting in 1952 when CRSP bond return data starts. The basic results are all the same.

Our findings suggest that interest rate risk is unlikely to explain the equity premium. Certainly, there is no evidence in favor of the hypothesis that equities face significant interest rate risk. How can this be reconciled with AER's empirical findings? The main difference between our analysis and AER's is that AER do not estimate real interest rate innovations. Their GMM includes the unconditional correlation between equity returns and the real risk free rate at an annual frequency but omits the more important correlation of interest rate *news* with *excess* equity returns. Our analysis estimates this moment and finds that it is essentially zero.

3.4 Conclusion

Is real interest rate risk priced? Theoretically, it could be priced in either direction. Empirically, there is little evidence that real interest rate risk is priced at all.

Our interest rate risk model has two theoretical implications. First, it matters where interest rate shocks comes from. Interest rate increases stemming from news about future consumption growth are generally good news to investors whereas interest rate increases stemming from time preference shocks are generally bad news. Thus, long-run consumption risk logic implies that long-duration assets are relatively safe whereas time preference risk logic implies that long-duration assets are relatively risky. A more general lesson is the importance of thinking in general equilibrium terms. Because interest rates are endogenous, interest rate risk is not a meaningful concept without specifying what is driving interest rate shocks.

The second theoretical implication of our model is that Epstein-Zin preferences with

ψ close to 1 and significantly different from $1/\gamma$ imply implausible aversion to future time preference shocks. If we take Epstein-Zin utility seriously as a description of actual preferences, this undermines many popular calibrations, such as those proposed by Bansal and Yaron (2004).

Empirically, stocks sorted on interest rate risk have only small, statistically insignificant return differences. Moreover, the market return and treasury bond returns have low covariance with interest rate news. Thus, interest rate risk is unlikely to explain much of equity or bond return premia even if it is priced to some extent in the cross section. Overall, our results suggest that interest rate risk is not a major concern to investors.

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Appendix A

Appendix to Chapter 1

A.1 Modification Algorithm

The LPS dataset lacks an explicit modification flag but contains enough detailed panel information to identify changes to loan terms over time. My loan modification algorithm differs in a few details but is essentially the same as the algorithm employed by Adelino, Gerardi, and Willen (2011b). The purpose of the algorithm is to identify changes to loan terms that are consistent with modification and do not have other likely explanations. Some changes are enough to identify a modification on their own. For example, absent errors in the data, an interest rate change to a fixed rate loan must stem from modification. Other changes require confirmatory evidence. For example, a principal reduction could be from a modification or from a prepayment. The size of the reduction, changes in monthly payments, and other simultaneous modifications all inform whether the reduction stems from a modification. In all cases, the loans in question are seriously delinquent at the time of the potential modification, adding to the likelihood that the algorithm is identifying true modifications. The algorithm separately identifies four types of modifications: interest rate reductions, term extensions, principal decreases, and principal increases. These modifications are not mutually exclusive and often take place simultaneously. I consider a loan to be modified if the algorithm flags it with any of the four modification types.

A.1.1 Interest Rate Reductions

Interest rate reductions are easiest to identify in fixed-rate loans and adjustable-rate loans that are still in their introductory fixed-rate period. For these loans, I define an interest rate reduction as a change that reduces a loan's interest rate to at least 0.5 ppt below the previous month's rate and the loan's origination interest rate.

For adjustable-rate mortgages, I first compute a fully indexed interest rate for each loan in each month using LPS data on the loan's reference index and spread combined with time-series data on the index rates. For example, a loan that references LIBOR and has a spread of 2 ppt would have a fully indexed rate of LIBOR + 2 ppt in any month. I abstract from details on exactly how frequently rates reset and consider any loan to be adjustable if it is past or within 2 months of the end of its introductory period. To be flagged as an interest rate reduction, a loan's interest rate must decrease to at least 0.5 ppt below the previous month's rate, the origination interest rate, and the fully indexed rate.

A.1.2 Term Extensions

To be flagged as a term extension, a loan's remaining term to maturity must increase by at least 20 months or rise above its initial term to maturity. The term change must also be contemporaneous with a monthly payment decrease, principal increase, or explicit loss mitigation flag in the data.

A.1.3 Principal Decreases

To be flagged as a principal decrease, the mortgage must have had outstanding principal of at least \$25K in the previous month, and the principal balance must have decreased by between 10% and 30% and be accompanied by a payment decrease or term extension. The 10-30% range is used to differentiate modifications from scheduled principal decreases and prepayments. Adelino, Gerardi, and Willen (2011b) experiment with the 30% cutoff and find that results are not sensitive to its exact value.

A.1.4 Principal Increases

To be flagged as a principal increase, principal must increase by at least 1% (0.5% for option ARM mortgages) and be accompanied by either a payment increase or a term length decrease.

A.2 Supplemental Figures and Tables

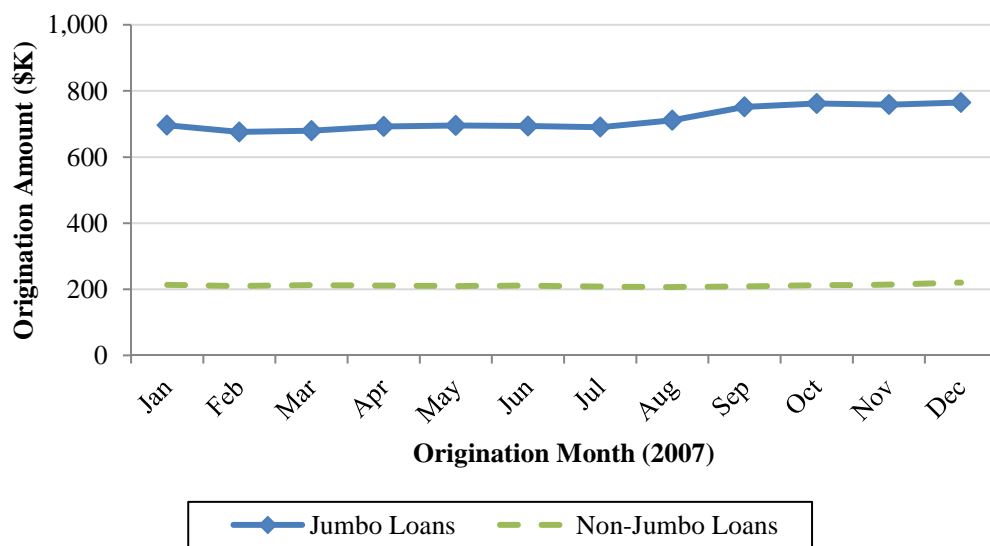


Figure A.1: *Origination Amount by Origination Month*
Mean loan origination amounts for sample jumbo and non-jumbo loans.

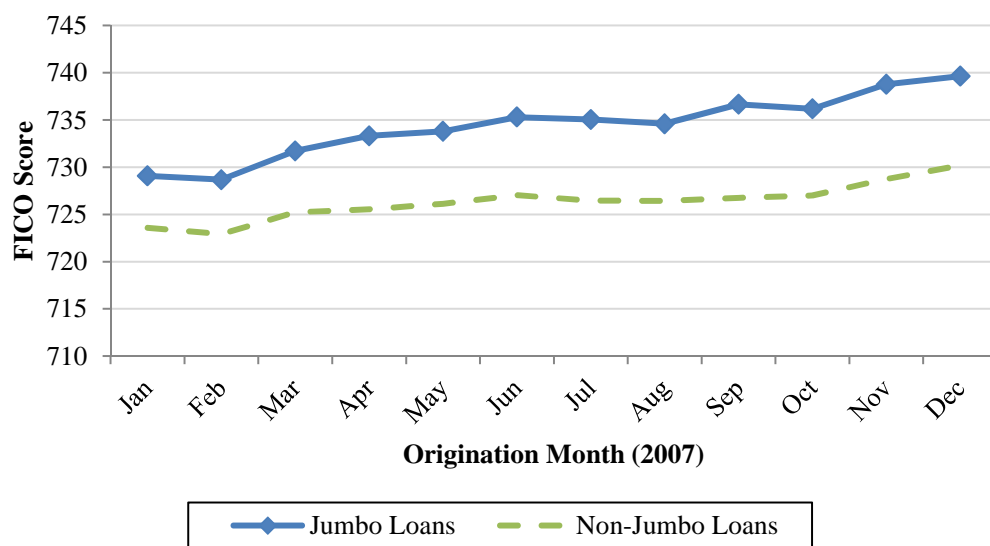


Figure A.2: *FICO Score by Origination Month*
Mean FICO scores for sample jumbo and non-jumbo loans.

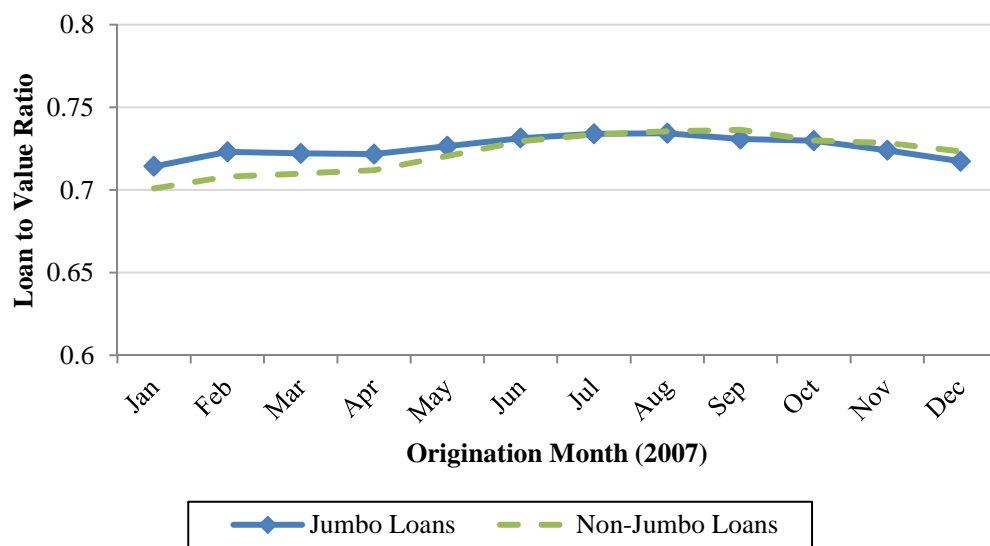


Figure A.3: *Loan to Value Ratio by Origination Month*
Mean loan to value ratios for sample jumbo and non-jumbo loans.

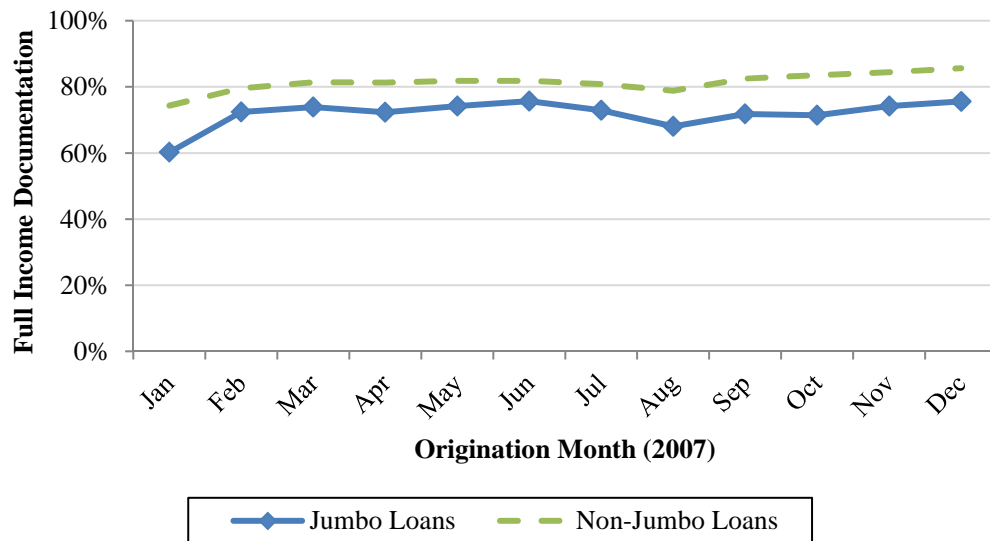


Figure A.4: Income Documentation by Origination Month
Percent of sample jumbo and non-jumbo loans with full income documentation.

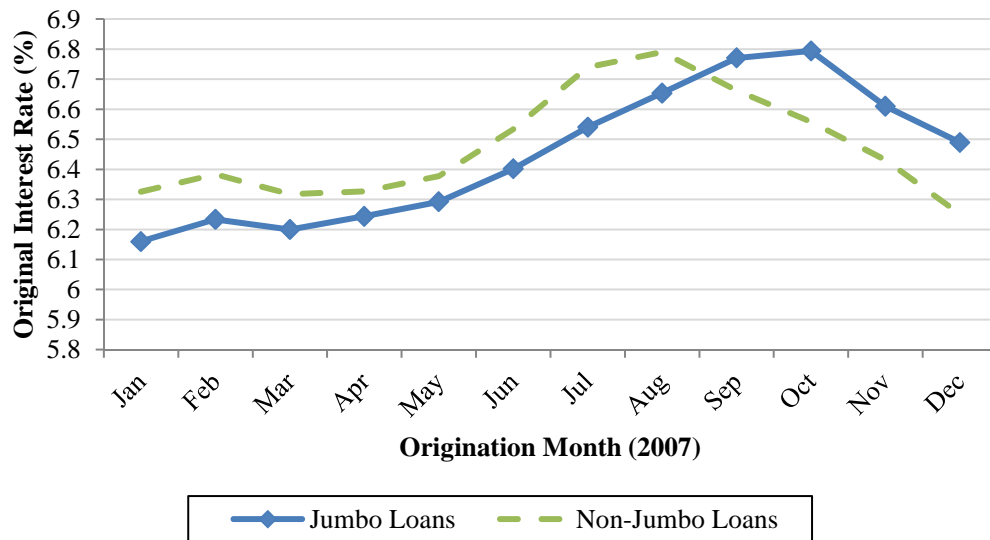


Figure A.5: Original Interest Rate by Origination Month
Mean original interest rates for sample jumbo and non-jumbo loans.

Table A.1: Additional Robustness Checks

Regressions are the same as Kruger's (2013) baseline IV regressions (Table 4, columns 2-4) except where noted. Columns 1-3 of Panel A drop loan characteristic controls. Columns 4-6 of Panel A add back loans transferred to non-LPS servicers, which were previously dropped from the sample. Panel B control for origination-month fixed effects using non-jumbo loans without controlling for the interaction between private securitization and non-jumbo status. R-squared statistics are calculated within MSAs. Clustered (by MSA) standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance.

<i>A. Regressions without loan characteristic controls (1-3) and with transferred loans (4-6)</i>						
	(1) IV	(2) IV	(3) IV	(4) IV	(5) IV	(6) IV
	Foreclose Start	Foreclose	Modify	Foreclose Start	Foreclose	Modify
Mean	0.695	0.135	0.052	0.695	0.135	0.052
Privately Securitized	0.055*** (0.016)	0.030** (0.012)	-0.039*** (0.010)	0.063*** (0.015)	0.051*** (0.012)	-0.032*** (0.009)
Loan Characteristics	No	No	No	Yes	Yes	Yes
Delinquency Month FE	Yes	Yes	Yes	Yes	Yes	Yes
Origination Month FE	No	No	No	No	No	No
MSA FE	Yes	Yes	Yes	Yes	Yes	Yes
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug	Jan-Aug
Include Non-Jumbo Loans	No	No	No	No	No	No
Observations	15,945	15,945	7,893	17,165	17,165	8,556
Adjusted R-Squared	0.036	0.011	-0.002	0.079	0.027	0.088
<i>B. Non-jumbo origination month control regressions without securitization*non-jumbo interaction</i>						
	(1) IV	(2) IV	(3) IV			
	Foreclose Start	Foreclose	Modify			
Mean	0.695	0.135	0.052			
Privately Securitized	0.172*** (0.031)	0.079*** (0.018)	-0.050** (0.022)			
Loan Characteristics	Yes	Yes	Yes			
Delinquency Month FE	Yes	Yes	Yes			
Origination Month FE	Yes	Yes	Yes			
MSA FE	Yes	Yes	Yes			
Origination Months	Jan-Aug	Jan-Aug	Jan-Aug			
Include Non-Jumbo Loans	Yes	Yes	Yes			
Observations	77,160	77,160	35,934			
Adjusted R-Squared	0.072	0.031	0.060			

Appendix B

Appendix to Chapter 2

B.1 General Model Derivations and Proofs

B.1.1 Solution

I assume that the price function is linear:

$$P = \alpha + \beta \bar{y} - \gamma (X - \mu_X) \quad (\text{B.1})$$

Claim 1. $\beta \neq 0$.

PROOF. Assume $\beta = 0$. Thus, price is uninformative about private signals, and all agents have posterior beliefs of $E_i[\theta|y_{m(i)}, x_{m(i)}, P] = \frac{\tau_p \mu + \psi \tau_s y_{m(i)}}{\tau_p + \psi \tau_s}$ and $\text{Var}_i[\theta|y_{m(i)}, x_{m(i)}, P] = (\tau_p + \psi \tau_s)^{-1}$, resulting in asset demand $D_i[y_{m(i)}, x_{m(i)}, P] = \frac{E_i[\theta|y_{m(i)}, x_{m(i)}, P] - P}{\frac{\gamma}{\eta} \text{Var}_i[\theta|y_{m(i)}, x_{m(i)}, P]} = \frac{\eta}{N} [\tau_p \mu + \psi \tau_s y_{m(i)} - (\tau_p + \psi \tau_s) P]$. Solving $\sum_i D_i = X$ for the market clearing price implies $P = \frac{\tau_p \mu + \psi \tau_s \bar{y} - \frac{X}{\eta}}{\tau_p + \psi \tau_s}$. Thus, $\beta = \frac{\psi \tau_s}{\tau_p + \psi \tau_s} \neq 0$, a contradiction. ■

Given the price function described by equation (B.1), agent i extracts a noisy signal for $\bar{y}_{-m(i)}$ from observing price, $y_{m(i)}$, and $x_{m(i)}$:

$$\begin{aligned} A_{m(i)} &= \frac{M}{\beta(M-1)} (P - \alpha) - \frac{1}{M-1} y_{m(i)} + \frac{\gamma M}{\beta(M-1)} \left(x_{m(i)} - \frac{\mu_X}{M} \right) \\ &= \bar{y}_{-m(i)} - \frac{\gamma M}{\beta} \left(\bar{x}_{-m(i)} - \frac{\mu_X}{M} \right) \end{aligned} \quad (\text{B.2})$$

Note that $A_{m(i)} \sim_i \mathcal{N}\left(\theta, \frac{1}{(M-1)\tau_s} + \left(\frac{\gamma}{\beta}\right)^2 \frac{M}{M-1} V\right)$ and $A_{m(i)}$ is independent of $y_{m(i)}$ and $x_{m(i)}$. Using Bayesian updating with signals $y_{m(i)}$ and $A_{m(i)}$ and substituting P , $y_{m(i)}$, $x_{m(i)}$ for $A_{m(i)}$ using (B.2), agent i 's posterior beliefs as a function of P , $y_{m(i)}$, $x_{m(i)}$ are:

$$E_i[\theta|y_{m(i)}, x_{m(i)}, P] = \frac{\left(\tau_p \mu - \frac{M\tau_A}{\beta(M-1)} \alpha + \left(\psi \tau_s - \frac{\tau_A}{M-1} \right) y_{m(i)} + \frac{\gamma M \tau_A}{\beta(M-1)} \left(x_{m(i)} - \frac{\mu_X}{M} \right) + \frac{M\tau_A}{\beta(M-1)} P \right)}{\tau_p + \psi \tau_s + \tau_A} \quad (\text{B.3a})$$

$$\text{Var}_i[\theta|y_{m(i)}, x_{m(i)}, P] = (\tau_p + \psi \tau_s + \tau_A)^{-1} \quad (\text{B.3b})$$

where $\tau_A = \left(\frac{1}{(M-1)\tau_s} + \left(\frac{\gamma}{\beta} \right)^2 \frac{M}{M-1} V \right)^{-1}$ is the precision agent i attributes to $A_{m(i)}$.

Agent i 's asset demand is:

$$\begin{aligned} D_i &= \frac{E_i[\theta|y_{m(i)}, x_{m(i)}, P] - P}{\frac{N}{\eta} \text{Var}_i[\theta|y_{m(i)}, x_{m(i)}, P]} \\ &= \frac{\eta}{N} \left(\tau_p \mu - \frac{M\tau_A}{\beta(M-1)} \alpha + \left(\psi \tau_s - \frac{\tau_A}{M-1} \right) y_{m(i)} + \frac{\gamma M \tau_A}{\beta(M-1)} \left(x_{m(i)} - \frac{\mu_X}{M} \right) - \left(\tau_p + \psi \tau_s + \left(1 - \frac{M}{\beta(M-1)} \right) \tau_A \right) P \right) \end{aligned} \quad (\text{B.4})$$

The market clearing price must solve $X = \sum_i D_i$. Thus,

$$P = \frac{\tau_p \mu - \frac{1}{\eta} \mu_X - \frac{M\tau_A}{\beta(M-1)} \alpha + \left(\psi \tau_s - \frac{\tau_A}{M-1} \right) \bar{y} - \left(\frac{1}{\eta} - \frac{\gamma \tau_A}{\beta(M-1)} \right) (X - \mu_X)}{\tau_p + \psi \tau_s + \left(1 - \frac{M}{\beta(M-1)} \right) \tau_A} \quad (\text{B.5})$$

Equations (B.1) and (B.5) yield the following system of equations:

$$\begin{bmatrix} \alpha \\ \beta \\ \gamma \end{bmatrix} \left(\tau_p + \psi \tau_s + \left(1 - \frac{M}{\beta(M-1)} \right) \tau_A \right) = \begin{bmatrix} \tau_p \mu - \frac{1}{\eta} \mu_X - \frac{M\tau_A}{\beta(M-1)} \alpha \\ \psi \tau_s - \frac{\tau_A}{M-1} \\ \frac{1}{\eta} - \frac{\gamma \tau_A}{\beta(M-1)} \end{bmatrix} \quad (\text{B.6})$$

Claim 2. The unique solution to equations (B.6) is:

$$\alpha = \frac{(\eta^2 \psi^2 \tau_p \tau_s + M V \tau_p) \mu - \left(\eta \psi^2 \tau_s + \frac{M V}{\eta} \right) \mu_X}{\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) M V} \quad (\text{B.7})$$

$$\beta = \frac{\psi \tau_s (\eta^2 \psi (M + \psi - 1) \tau_s + M V)}{\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) M V} \quad (\text{B.8})$$

$$\gamma = \frac{\eta^2 \psi (M + \psi - 1) \tau_s + M V}{\eta (\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) M V)} \quad (\text{B.9})$$

PROOF. Consider $\Gamma \equiv \frac{\gamma}{\beta}$. We already established that $\beta \neq 0$ so Γ is finite. Substituting Γ into (B.6) and dividing the γ equation by the β equation yields:

$$\begin{aligned}\Gamma &= \frac{\frac{1}{\eta} - \Gamma \frac{\tau_A}{M-1}}{\psi \tau_s - \frac{\tau_A}{M-1}} \\ &= \frac{1}{\eta \psi \tau_s}\end{aligned}\tag{B.10}$$

Plugging (B.10) into the β equation of (B.6) yields:

$$\beta = \frac{\psi \tau_s (\eta^2 \psi (M + \psi - 1) \tau_s + MV)}{\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV}\tag{B.11}$$

Plugging (B.10) and (B.11) into the γ equation of (B.6) yields:

$$\gamma = \frac{\eta^2 \psi (M + \psi - 1) \tau_s + MV}{\eta (\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV)}\tag{B.12}$$

Finally, plugging (B.10), (B.11), and (B.12) into the α equation of (B.6) yields:

$$\alpha = \frac{(\eta^2 \psi^2 \tau_p \tau_s + MV \tau_p) \mu - \left(\eta \psi^2 \tau_s + \frac{MV}{\eta} \right) \mu_X}{\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV}\tag{B.13}$$

■

B.1.2 Trading

Using equation (B.4),

$$\begin{aligned}\text{Trade}_m &\equiv \sum_{i:m(i)=m} \left[D_i - \frac{M}{N} x_m \right] \\ &= \left\{ \frac{\eta}{M} \left(\psi \tau_s - \frac{\tau_A}{M-1} \right) (y_m - \bar{y}) \right\} - \left\{ \left(1 - \frac{\eta \gamma \tau_A}{(M-1) \beta} \right) (x_m - \bar{x}) \right\}\end{aligned}\tag{B.14}$$

All other trading derivations are in the main text of the paper.

B.1.3 Liquidity

Recall that illiquidity is defined as:

$$\lambda \equiv \frac{\frac{dP}{dy_m}}{\frac{d\text{Trade}_m}{dy_m}}$$

Taking derivatives of P (eq. B.1) and $Trade_m$ (eq. B.14) with respect to y_m and plugging in γ from (B.9) and Γ from (B.10) yields:

$$\begin{aligned}
\lambda &= \frac{-\gamma}{\left(\frac{N}{M}\right) \left(\frac{\eta}{N}\right) \left(\frac{\gamma M \tau_A}{\beta(M-1)} + \gamma \left(\tau_p + \psi \tau_s + \left(1 - \frac{M}{\beta(M-1)}\right) \tau_A\right)\right) - 1} \\
&= \frac{M (\eta^2 \psi^2 \tau_s + MV) (\eta^2 \psi (M + \psi - 1) \tau_s + MV)}{\eta (M - 1) (\eta^2 (\psi^2 - \psi) \tau_s + MV) (\eta^2 \psi^2 \tau_s (\tau_p + (M + \psi - 1) \tau_s) + (\tau_p + \psi \tau_s) MV)} \\
&= \left\{ \frac{M}{(M - 1) \eta (\tau_p + \psi \tau_s + \tau_A)} \right\} \\
&\quad + \left\{ \frac{\eta^2 \psi^2 \tau_s}{\eta^2 \psi^2 \tau_s + MV} \right\} \left\{ \frac{\tau_s}{\tau_p + \psi \tau_s + \tau_A} \right\} \left\{ \frac{\eta}{M} \left(\psi \tau_s - \frac{\beta}{M} (\tau_p + \psi \tau_s + \tau_A) \right) \right\}^{-1} \\
&= \{S\} + \{B1\} \{B2\} \{B3\}^{-1} \tag{B.15}
\end{aligned}$$

Consistent with the baseline model, $\lim_{V \rightarrow 0} \frac{d\lambda}{d\psi} < 0$, $\lim_{V \rightarrow 0} \frac{d\lambda}{d\tau_s} < 0$, and $\lim_{V \rightarrow 0} \frac{d\lambda}{d\tau_p} < 0$. From (B.15) one can see that $\frac{d\lambda}{d\tau_p} < 0$ for all V . However, $\frac{d\lambda}{d\psi}$ and $\frac{d\lambda}{d\tau_s}$ are not always negative. Their signs are determined by complicated functions of the parameters. Considering limiting cases is instructive. We have already seen that $\frac{d\lambda}{d\psi}$ and $\frac{d\lambda}{d\tau_s}$ are negative in the limit as $V \rightarrow 0$. Both are also negative in the limit as $V \rightarrow \infty$. For interim values of V (i.e., positive, finite V), $\frac{d\lambda}{d\psi}$ and $\frac{d\lambda}{d\tau_s}$ can be positive or negative. Both follow a similar pattern. As $\psi \rightarrow 0$ or $\tau_s \rightarrow 0$, $\lambda \rightarrow \frac{M}{(M-1)\eta\tau_p}$, which is solely a supply impact – it includes no belief price response.^{1,2} $\frac{d\lambda}{d\psi}$ and $\frac{d\lambda}{d\tau_s}$ initially have the same sign as $\eta^2 \tau_p - V$ (i.e., $\text{sign} \left[\lim_{\psi \rightarrow 0} \frac{d\lambda}{d\psi} \right] = \text{sign} \left[\lim_{\tau_s \rightarrow 0} \frac{d\lambda}{d\tau_s} \right] = \text{sign} [\eta^2 \tau_p - V]$). As ψ and τ_s increase, they eventually decrease λ , driving it to approach zero as $\psi \rightarrow \infty$ or $\tau_s \rightarrow \infty$.

¹Though I restrict my attention to overconfidence ($\psi > 1$) in other parts of the paper, it is useful to generalize and consider underconfidence ($\psi < 1$) here to get a full picture of the relationship between λ and ψ .

²The total risk tolerance of agents not receiving the shock is $\frac{(M-1)\eta}{M}$ and their posterior variance is τ_p^{-1} .

B.1.4 Liquidity without Overconfidence

Private information precision can enhance liquidity even without overconfidence. When $\psi = 1$ (which reproduces the model of Diamond and Verrecchia (1981)), illiquidity is:

$$\lambda_{\psi=1} = \frac{M (\eta^2 \tau_s + MV) (\eta^2 \tau_s + V)}{\eta (M-1) (\eta^2 \tau_s (\tau_p + M \tau_s) + (\tau_p + \tau_s) MV) V} \quad (\text{B.16})$$

and its derivative with respect to private information precision is:

$$\frac{d\lambda}{d\tau_s}_{\psi=1} = \frac{M (\eta^6 \tau_p \tau_s^2 + \eta^4 \tau_s (2\tau_p - M \tau_s) MV + \eta^2 (\tau_p - 2\tau_s) M^2 V^2 - M^2 V^3)}{\eta (M-1) (\eta^2 \tau_s (\tau_p + M \tau_s) + (\tau_p + \tau_s) MV)^2 V} \quad (\text{B.17})$$

The $V \rightarrow 0$ limit is uninteresting because without endowment shocks or overconfidence, illiquidity is infinite.

As $V \rightarrow \infty$, $\lambda_{\psi=1} \rightarrow \frac{M}{(M-1)\eta(\tau_p + \tau_s)}$ and $\frac{d\lambda}{d\tau_s}_{\psi=1} \rightarrow \frac{-M}{(M-1)\eta(\tau_p + \tau_s)^2} < 0$. Under infinite supply variance, liquidity trading swamps informed trading so trades carry no information. Thus, only the supply channel is operative, and the supply illiquidity channel always decreases as information (public or private) increases.

For interim values of V , λ starts off as solely a supply effect: $\lim_{\tau_s \rightarrow 0} \lambda_{\psi=1} = \frac{M}{(M-1)\eta\tau_p}$. As τ_s increases, the supply illiquidity channel decreases, but the belief illiquidity channel increases at least initially. For large V , the decreasing supply channel is more powerful. For small V , the increasing belief channel is more powerful. Specifically, $\lim_{\tau_s \rightarrow 0} \frac{d\lambda}{d\tau_s}_{\psi=1} = \frac{M(\eta^2 \tau_p - V)}{\eta \tau_p^2 (M-1)V}$. For large τ_s , only the belief channel is operative, and $\lim_{\tau_s \rightarrow \infty} \lambda_{\psi=1} = \frac{\eta}{(M-1)V}$. Note that this is a positive constant whereas $\lim_{\tau_s \rightarrow \infty} \lambda = 0$ when $\psi > 1$. The belief channel consistently increases with τ_s when V is small, but when V is large, τ_s eventually decreases the belief channel, thereby decreasing overall illiquidity as well. Specifically, $\text{sign} \left[\lim_{\tau_s \rightarrow \infty} \frac{d\lambda}{d\tau_s}_{\psi=1} \right] = \text{sign} [\eta^2 \tau_p - M^2 V]$. Another point of interest is to compare illiquidity at the two limits of τ_s : $\frac{\lim_{\tau_s \rightarrow \infty} \lambda_{\psi=1}}{\lim_{\tau_s \rightarrow 0} \lambda_{\psi=1}} = \frac{\eta^2 \tau_p}{MV}$.

The overall relationship between private information and illiquidity without overconfidence is as follows: For high supply variance ($V > \eta^2 \tau_p$), private information decreases illiquidity; for low supply variance ($V < \frac{\eta^2 \tau_p}{M^2}$), private information increases illiquidity; and for moderate supply variance ($\frac{\eta^2 \tau_p}{M^2} < V < \eta^2 \tau_p$), illiquidity is a hump-shaped function

of private information. Within the moderate case, τ_s decreases illiquidity overall when $V > \frac{\eta^2 \tau_p}{M}$ and increases illiquidity overall when $V < \frac{\eta^2 \tau_p}{M}$.

B.2 Supplemental Tables

Table B.1: Stock VAR Results

turn and illiq are detrended log turnover and illiq (a measure of illiquidity), respectively. rmrf is the excess return of the CRSP value weighted market return over the risk free rate. turn and illiq were detrended using a Hodrick and Prescott (1997) filter with a penalty value of 14,400. Reported results are for a 2-lag VAR of turn, illiq, and rmrf. Bootstrapped standard errors are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance. Turnover and illiq are equally weighted averages. Sample includes all NYSE stocks with lagged prices greater than \$5 from 1926 to 2011.

	(1) turn	(2) illiq	(3) rmrf
Lag 1			
turn	0.4835*** (0.0392)	-0.1083** (0.0437)	0.0137 (0.012)
illiq	-0.0634 (0.0392)	0.4329*** (0.0507)	0.0225** (0.011)
rmrf	0.8625*** (0.1905)	-1.5128*** (0.1687)	0.1133* (0.0612)
Lag 2			
turn	-0.0059 (0.0432)	0.081** (0.0383)	-0.0049 (0.0094)
illiq	-0.0043 (0.0366)	0.2444*** (0.045)	0.0167 (0.0103)
rmrf	0.3903** (0.1849)	0.0793 (0.164)	0.0161 (0.054)
Constant	-0.0076 (0.007)	0.0089 (0.0067)	0.0053*** (0.0018)
R-Squared	0.38	0.52	0.05

Table B.2: Stock Panel VAR Results

turn and illiq are monthly stock-level log turnover and illiq (a measure of illiquidity), respectively. ret is the monthly individual stock returns. ret_ind is the monthly return on the stock's industry. Industries are defined using the 10 industry groups on Ken French's website. Reported results are for a 2-lag VAR of turn, illiq, ret, and ret_ind. Bootstrapped standard errors controlling for cross-sectional correlation are in parentheses. * represents 10% significance, ** represents 5% significance, *** represents 1% significance. Sample includes all NYSE stocks with lagged prices greater than \$5 from 1951 to 2011.

	(1) turn	(2) illiq	(3) ret	(4) ret_ind
Lag 1				
turn	0.2295*** (0.0312)	-0.1645*** (0.0333)	0.0214* (0.0125)	0.0007 (0.0035)
illiq	-0.1209 (0.0803)	0.2187*** (0.0696)	0.025 (0.0226)	0.0006 (0.0055)
ret	0.0558 (0.0935)	-0.2166** (0.0873)	-0.1021*** (0.0278)	-0.0001 (0.0066)
ret_ind	0.1776*** (0.0638)	-0.1159 (0.074)	0.1119** (0.0486)	0.0515 (0.0713)
Lag 2				
turn	-0.0196 (0.0204)	0.0192 (0.0199)	0.008 (0.007)	0.0004 (0.0019)
illiq	-0.041 (0.0343)	0.0626** (0.0297)	0.0139 (0.0097)	0.0005 (0.0024)
ret	-0.0116 (0.025)	-0.0036 (0.0249)	-0.0325*** (0.009)	-0.0018 (0.0021)
ret_ind	0.084** (0.0403)	-0.0388 (0.0463)	0.0054 (0.0293)	-0.0212 (0.0413)
Stock FE	Yes	Yes	Yes	Yes
Time FE	Yes	Yes	Yes	Yes

Appendix C

Appendix to Chapter 3

C.1 Setup and General Pricing Equations

The representative agent has the augmented Epstein-Zin preferences described by equation (3.1):

$$U_t = \max_{C_t} \left[\lambda_t C_t^{1-1/\psi} + \delta (U_{t+1}^*)^{1-1/\psi} \right]^{1/(1-1/\psi)}$$

where $U_{t+1}^* = \left\{ E_t \left[U_{t+1}^{1-\gamma} \right] \right\}^{1/(1-\gamma)}$ is the certainty equivalent of future utility. Optimization is subject to budget constraint:

$$W_{t+1} = R_{w,t+1} (W_t - C_t) \tag{C.1}$$

where W_t is wealth at time t and $R_{w,t+1}$ is the return on the overall wealth portfolio, which is a claim to all future consumption.

AER use standard techniques from the Epstein-Zin preference literature to show that the preferences represented by equation (3.1) imply the log stochastic discount factor (sdf) presented in equation (3.2):

$$m_{t+1} = \theta \log \left(\delta \frac{\lambda_{t+1}}{\lambda_t} \right) - \frac{\theta}{\psi} \Delta c_{t+1} + (\theta - 1) r_{w,t+1}$$

This sdf should not be surprising. It is just the standard Epstein-Zin sdf with time-varying time discounting (i.e., $\delta \frac{\lambda_{t+1}}{\lambda_t}$ instead of δ).

Using $0 = E_t [m_{t+1} + r_{i,t+1}] + \frac{1}{2} (\sigma_m^2 + \sigma_i^2 + 2\sigma_{mi})$ (the log version of $1 = E_t [M_{t+1}R_{i,t+1}]$), we calculate the expected return for any asset as:

$$\begin{aligned} E_t [r_{i,t+1}] + \frac{1}{2}\sigma_i^2 = & -\theta \log \left(\delta \frac{\lambda_{t+1}}{\lambda_t} \right) + \frac{\theta}{\psi} E_t [\Delta c_{t+1}] + (1 - \theta) E_t [r_{w,t+1}] \\ & - \frac{1}{2} \left(\frac{\theta}{\psi} \right)^2 \sigma_c^2 - \frac{1}{2} (1 - \theta)^2 \sigma_w^2 + \frac{\theta}{\psi} (\theta - 1) \sigma_{wc} \\ & + \frac{\theta}{\psi} \sigma_{ic} + (1 - \theta) \sigma_{iw} \end{aligned} \quad (C.2)$$

The $\frac{1}{2}\sigma_i^2$ on the left hand side of equation (C.2) is a Jensen's inequality correction for log returns.

The risk free rate is of particular interest:

$$\begin{aligned} r_{f,t+1} = & -\theta \log \left(\delta \frac{\lambda_{t+1}}{\lambda_t} \right) + \frac{\theta}{\psi} E_t [\Delta c_{t+1}] + (1 - \theta) E_t [r_{w,t+1}] \\ & - \frac{1}{2} \left(\frac{\theta}{\psi} \right)^2 \sigma_c^2 - \frac{1}{2} (1 - \theta)^2 \sigma_w^2 + \frac{\theta}{\psi} (\theta - 1) \sigma_{wc} \end{aligned} \quad (C.3)$$

Differencing equations (C.2) and (C.3) yields the risk premia of equation (3.7):

$$E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2}\sigma_i^2 = \frac{\theta}{\psi} \sigma_{ic} + (1 - \theta) \sigma_{iw}$$

which is exactly the same expression as in standard Epstein-Zin models. Substituting $E_t [r_{w,t+1}]$ from equation (3.7) into equation (C.3), yields equation (3.6):

$$r_{f,t+1} = -\log \left(\delta \frac{\lambda_{t+1}}{\lambda_t} \right) + \frac{1}{\psi} E_t [\Delta c_{t+1}] - \frac{1 - \theta}{2} \sigma_w^2 - \frac{\theta}{2\psi^2} \sigma_c^2$$

which is the same as standard Epstein-Zin models except that δ is replaced by $\delta \frac{\lambda_{t+1}}{\lambda_t}$.

C.2 Substituting out Consumption (The ICAPM)

Following Campbell (1993) we log linearize the budget constraint to yield equation (3.8):

$$r_{w,t+1} - E_t [r_{w,t+1}] = (E_{t+1} - E_t) \sum_{j=0}^{\infty} \rho^j \Delta c_{t+1+j} - (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{w,t+1+j}$$

where $\rho = 1 - \exp(\overline{c - w})$ is a log-linearization constant ($\overline{c - w}$ is the average log

consumption-wealth ratio). Rearranging equation (3.8), we can express current consumption shocks as:

$$\begin{aligned}\Delta c_{t+1} - E_t [\Delta c_{t+1}] &= r_{w,t+1} - E_t [r_{w,t+1}] \\ &\quad + (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j r_{w,t+1+j} \\ &\quad - (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \Delta c_{t+1+j}\end{aligned}\tag{C.4}$$

So far, we have only made use of modified Epstein-Zin preferences and the budget constraint. We now use assumptions about consumption and time preference innovations for the first time. Due to our homoskedasticity assumption, risk premia (equation 3.7) do not change over time, and the riskfree rate (equation 3.6) only changes in response to time preference and consumption growth innovations. Thus, innovations to expected returns can be decomposed as:

$$\begin{aligned}(E_{t+1} - E_t) r_{w,t+1+j} &= (E_{t+1} - E_t) r_{f,t+1+j} \\ &= (E_{t+1} - E_t) \log \left(\frac{\lambda_{t+j}}{\lambda_{t+j+1}} \right) + \frac{1}{\psi} (E_{t+1} - E_t) [\Delta c_{t+j+1}]\end{aligned}\tag{C.5}$$

for $j \geq 1$.

Substituting equation (C.5) into equation (C.4) yields:

$$\begin{aligned}\Delta c_{t+1} - E_t [\Delta c_{t+1}] &= r_{w,t+1} - E_t [r_{w,t+1}] \\ &\quad - \left(1 - \frac{1}{\psi} \right) (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \Delta c_{t+1+j} \\ &\quad + (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \log \left(\frac{\lambda_{t+j}}{\lambda_{t+j+1}} \right)\end{aligned}\tag{C.6}$$

Substituting out consumption shock covariance (σ_{ic}) from equation (3.7) yields risk premia as a function of covariances with market returns and innovations to future time

preferences and consumption growth:

$$\begin{aligned}
E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2}\sigma_i^2 &= \gamma\sigma_{iw} \\
&+ (\gamma - 1) \frac{1}{\psi} \text{cov}_t \left(r_{i,t+1}, (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \Delta c_{t+1+j} \right) \\
&+ \frac{\theta}{\psi} \text{cov}_t \left(r_{i,t+1}, (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \log \left(\frac{\lambda_{t+j}}{\lambda_{t+j+1}} \right) \right) \quad (C.7)
\end{aligned}$$

Equation (3.9) expresses this as:

$$E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2}\sigma_i^2 = \gamma\sigma_{iw} - \frac{\gamma - 1}{\psi - 1} \sigma_{ih(\lambda)} + (\gamma - 1) \sigma_{ih(c)}$$

where

$$\sigma_{ih(\lambda)} = \text{cov}_t \left(r_{i,t+1}, (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \log \left(\frac{\lambda_{t+j}}{\lambda_{t+j+1}} \right) \right) \quad (C.8)$$

and

$$\sigma_{ih(c)} = \frac{1}{\psi} \text{cov}_t \left(r_{i,t+1}, (E_{t+1} - E_t) \sum_{j=1}^{\infty} \rho^j \Delta c_{t+1+j} \right) \quad (C.9)$$

are the two different types of interest rate news covariance.

C.3 Substituting out Wealth Returns (The Generalized CCAPM)

We can also use the budget constraint to substitute out wealth portfolio return covariance (σ_{iw}) from equation (3.7) by rearranging equation (C.6) and using it to decompose σ_{iw} , thereby yielding equation (3.11):

$$E_t [r_{i,t+1}] - r_{f,t+1} + \frac{1}{2}\sigma_i^2 = \gamma\sigma_{ic} + (\gamma\psi - 1) \sigma_{ih(c)} - \frac{\gamma\psi - 1}{\psi - 1} \sigma_{ih(\lambda)}$$

C.4 Disciplining Parameter Values

In a three period setting with $\lambda_0 = \lambda_1 = \delta = 1$, Epstein-Zin Utility (equation 3.1) can be expressed as:

$$U_0 = \max_{C_0} \left\{ C_0^{1-1/\psi} + \left(E_0 \left[\max_{C_1, C_2} \left\{ C_1^{1-1/\psi} + \lambda_2 C_2^{1-1/\psi} \right\}^{\frac{1-\gamma}{1-1/\psi}} \right] \right)^{\frac{1-1/\psi}{1-\gamma}} \right\}^{1/(1-1/\psi)} \quad (C.10)$$

The Euler equation for an Arrow-Debreu security that pays off in state s is:

$$\begin{aligned} P_s C_0^{-1/\psi} = & \left[\pi_L \left(C_1^{1-1/\psi} + \lambda_L C_2^{1-1/\psi} \right)^{\frac{1-\gamma}{1-1/\psi}} + \pi_H \left(C_1^{1-1/\psi} + \lambda_H C_2^{1-1/\psi} \right)^{\frac{1-\gamma}{1-1/\psi}} \right]^{\frac{\gamma-1/\psi}{1-\gamma}} \\ & * \pi_s \left(C_1^{1-1/\psi} + \lambda_L C_2^{1-1/\psi} \right)^{\frac{1/\psi-\gamma}{1-1/\psi}} * C_1^{-1/\psi} \end{aligned} \quad (C.11)$$

where P_s is the state price for state s , π_s is the probability of state s , and λ_s is the value of λ_2 in state s .

Under our assumption that $C_0 = C_1 = C_2 = C$, equation (C.11) reduces to:

$$P_s = \pi_s (1 + \lambda_s)^{\frac{1/\psi-\gamma}{1-1/\psi}} \left[\pi_L (1 + \lambda_L)^{\frac{1-\gamma}{1-1/\psi}} + \pi_H (1 + \lambda_H)^{\frac{1-\gamma}{1-1/\psi}} \right]^{\frac{\gamma-1/\psi}{1-\gamma}} \quad (C.12)$$

Equation (C.12) immediately implies the state price ratio given by equation (3.16):

$$\frac{P_L}{P_H} = \frac{\pi_L}{\pi_H} \left(\frac{1 + \lambda_L}{1 + \lambda_H} \right)^{-\frac{\gamma-1/\psi}{1-1/\psi}}$$